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2 **Faster-haplodiploid evolution under divergence-with-gene-flow: simulations and empirical**
3 **data from pine-feeding hymenopterans**

4 *Short Running Title: Adaptive divergence under haplodiploidy*

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22 **Abstract**

23 Although haplodiploidy is widespread in nature, the evolutionary consequences of this mode of
24 reproduction are not well characterized. Here, we examine how genome-wide hemizyosity and
25 a lack of recombination in haploid males affects genomic differentiation in populations that
26 diverge via natural selection while experiencing gene flow. First, we simulated diploid and
27 haplodiploid “genomes” (500-kb loci) evolving under an isolation-with-migration model with
28 mutation, drift, selection, migration, and recombination; and examined differentiation at neutral
29 sites both tightly and loosely linked to a divergently selected site. So long as there is divergent
30 selection and migration, sex-limited hemizyosity and recombination cause elevated
31 differentiation (i.e., produce a “faster-haplodiploid effect”) in haplodiploid populations relative
32 to otherwise equivalent diploid populations, for both recessive and codominant mutations.
33 Second, we used genome-wide SNP data to model divergence history and describe patterns of
34 genomic differentiation between sympatric populations of *Neodiprion lecontei* and *N. pinetum*, a
35 pair of pine sawfly species (order: Hymenoptera; family: Diprionidae) that are specialized on
36 different pine hosts. These analyses support a history of continuous gene exchange throughout
37 divergence and reveal a pattern of heterogeneous genomic differentiation that is consistent with
38 divergent selection on many unlinked loci. Third, using simulations of haplodiploid and diploid
39 populations evolving according to the estimated divergence history of *N. lecontei* and *N.*
40 *pinetum*, we found that divergent selection would lead to higher differentiation in haplodiploids.
41 Based on these results, we hypothesize that haplodiploids undergo divergence-with-gene-flow
42 and sympatric speciation more readily than diploids.

43

44 **Introduction**

45 In terms of both species richness and biomass, haplodiploid organisms account for a
46 substantial proportion of terrestrial biodiversity (Forbes et al., 2018; Hölldobler & Wilson,
47 1990). Haplodiploidy (arrhenotoky)—a reproductive mode in which females develop from
48 fertilized eggs and are diploid, while males develop from unfertilized eggs and are haploid—has
49 evolved repeatedly in diverse arthropod lineages and is present in an estimated 12% of extant
50 animal species (Blackmon et al., 2017; de la Filia et al., 2015; Hedrick & Parker, 1997; Normark,
51 2003). From a theoretical perspective, most work on haplodiploidy has focused on the evolution
52 of eusociality (Hamilton, 1964a, 1964b, 1972; Rautiala et al., 2019, but see Hartl, 1972; and de
53 la Filia et al., 2015). However, haplodiploid transmission genetics can have many other
54 important evolutionary consequences. For example, when haplodiploid populations hybridize,
55 only female hybrids are produced in the first generation and hybrid males are produced in the
56 subsequent generation. This asymmetry may lead to higher rates of mitochondrial introgression
57 compared to nuclear introgression (Linnen & Farrell, 2007; Patten et al., 2015) and may have
58 consequences for the evolution of postzygotic isolation (Bendall et al., 2020; see also Ghenu et
59 al., 2018; Nouhaud et al., 2020). Haplodiploidy is also expected to impact the evolution of
60 sexually selected traits (Kirkpatrick & Hall, 2004; Reeve & Pfennig, 2003), mating systems
61 (Boulton et al., 2015; Werren, 1993), parental care (Davies & Gardner, 2014; Gardner, 2012),
62 sex ratios (Hamilton, 1967), and the outcomes of intra- and inter-locus conflicts (Klein et al.,
63 2021; Hitchcock et al., 2022; Kraaijeveld, 2009). However, formal theory and empirical tests for
64 the evolutionary consequences of haplodiploidy remain rare (de la Filia et al., 2015).

65 Here, we focus on how haplodiploidy affects genomic differentiation in diverging
66 populations and species. Similarities in transmission genetics between haplodiploid genomes and

67 X (or Z) chromosomes make it possible to draw on faster-X theory to generate predictions for
68 haplodiploids (Hartl, 1972; Avery, 1984; Hedrick & Parker, 1997; Kraaijeveld, 2009). Within
69 populations, hemizyosity in XY and haplodiploid males will expose recessive or partially
70 recessive mutations to selection, thereby hastening the removal of deleterious alleles and the
71 fixation of beneficial alleles (Avery, 1984; Charlesworth, et al., 1987; Hedrick & Parker, 1997).
72 More efficient selection on novel hemizygous alleles will also impact linked variation via
73 hitchhiking (Betancourt et al., 2004) and background selection (Charlesworth, 2012), and these
74 effects will be exacerbated by a lack of recombination in XY and haplodiploid males (Betancourt
75 et al., 2004; Lester & Selander, 1979; Owen, 1986). So long as adaptation is driven primarily by
76 new mutations that are at least partially recessive, faster-X theory predicts higher adaptive
77 substitution rates and greater genetic divergence at linked sites on sex chromosomes and
78 haplodiploid genomes relative to diploid autosomes when populations or species diverge in
79 isolation (Presgraves 2018, but see Wright et al., 2015).

80 Conversely, models of divergence-with-gene-flow via common genetic variants suggest
81 that adaptive differentiation occurs more readily for sex-linked (or hemizygous) loci than for
82 autosomal loci, regardless of dominance (Lasne et al., 2017). Instead, the magnitude of the
83 faster-X effect on local adaptation depends on the rate of migration of the heterogametic sex
84 relative to the homogametic sex. This is because when the genetic variants under selection are
85 common, the efficiency of selection against maladapted immigrant alleles becomes more
86 important than fixation of rare mutations (Lasne et al., 2017). Although effects on linked
87 variation have not, to our knowledge, been explored in the context of primary divergence-with-
88 gene-flow models (e.g., Lasne et al. 2017), secondary contact models reveal that sex-limited
89 hemizyosity and recombination can reduce effective migration rates at neutral loci linked to loci

90 involved in local adaptation and/or hybrid incompatibilities (Fraisse & Sachdeva, 2021; Fusco &
91 Uyenoyama, 2011; Muirhead & Presgraves, 2016). Together, these models suggest that so long
92 as gene flow accompanies divergence, sex chromosomes and haplodiploid genomes will tend to
93 exhibit greater differentiation at selected and linked sites compared to autosomal chromosomes.

94 Consistent with faster-X theory, comparative and population genomic data from diverse
95 taxa suggest that faster-X effects (i.e., elevated differentiation, divergence, and substitution rates
96 on sex chromosomes) are widespread in nature (Irwin, 2018; Meisel & Connallon, 2013;
97 Presgraves, 2018). However, these patterns are not necessarily caused by sex-limited
98 recombination and hemizyosity. Indeed, there are many other differences between sex
99 chromosomes and autosomes that can also produce differences in genetic differentiation,
100 including: differences in effective population size (N_e), mutation rate, recombination rate, gene
101 content, sex-limited gene expression, and susceptibility to meiotic drive, sexual conflict, and
102 sexual selection (Frank, 1991; Hurst & Pomiankowski, 1991; Meiklejohn et al., 2018; Patten,
103 2018). Because they lack sex chromosomes, haplodiploids are potentially powerful models for
104 investigating the impact of sex-limited hemizyosity and recombination on genomic
105 differentiation independent of sex-chromosome specific factors. However, because they also lack
106 anything analogous to diploid autosomes, haplodiploids do not have a built-in benchmark for
107 quantifying “faster-haplodiploid” effects, which we define as greater differentiation or
108 divergence in haplodiploids relative to comparable diploids. Fortunately, increasingly
109 sophisticated tools for simulating genomic datasets evolving under complex demographic and
110 ecological scenarios (Hoban et al., 2012; Haller & Messer 2019; Hart et al., 2021) offer a
111 strategy for evaluating the potential for faster-haplodiploid effects: simulate a benchmark diploid
112 dataset with equivalent demographic history, recombination, and mutation under neutral and

113 adaptive scenarios. We note that analogous to the usage of the term “faster-X effect” (Meisel and
114 Connallon 2013), we are using the term “faster-haplodiploid effect” to refer to an empirical
115 pattern, without making assumptions about the underlying evolutionary mechanisms.

116 To better understand the impact of haplodiploidy on genomic differentiation, we combine
117 simulations of haplodiploid and diploid genomes evolving under divergence-with-gene-flow
118 with an empirical case study of a haplodiploid species pair for which we have extensive
119 knowledge regarding the drivers of divergent selection and reproductive isolation, as well as
120 basic life history knowledge to parameterize simulations. *Neodiprion pinetum* (white pine
121 sawfly) and *N. lecontei* (redheaded pine sawfly) are sister species with overlapping distributions
122 in eastern North American (Linnen & Farrell, 2008, 2010). Because both species are pests of
123 economically important pines, their basic ecology and life history are well described (Benjamin,
124 1955; Rauf & Benjamin, 1980; Coppel & Benjamin, 1965; Knerer & Atwood, 1973; Wilson et
125 al., 1992). Reproductive adults emerge in spring after overwintering as prepupae in cocoons.
126 Females fly to their preferred host and attract haploid males via a sex pheromone. Mating takes
127 place on the host plant, and females use their saw-like ovipositor to embed their full complement
128 of eggs within the needles of a single pine branch. Larvae emerge and feed on pine needles
129 before dispersing to the soil to spin a cocoon.

130 While *N. pinetum* and *N. lecontei* share many similarities, *N. pinetum* feeds exclusively
131 on white pine (*Pinus strobus*) and *N. lecontei* tends to avoid this host. Differences between their
132 hosts likely generate divergent selection on many different larval and adult traits (Coppel &
133 Benjamin, 1965; Codella & Raffa, 2002; Lindstedt et al., 2022; Bendall et al., 2017). For
134 example, differences in needle chemistry and thickness between the preferred hosts of *N.*
135 *lecontei* and *N. pinetum* are associated with differences in egg size, female ovipositor

136 morphology, and female egg-laying behaviors. These traits, which together determine the
137 reproductive success of adult females, act as an ecological barrier to gene exchange in sympatric
138 populations (Bendall et al., 2017). This previous work suggests that many regions of the genome
139 are likely to be under divergent selection between these species. Moreover, a coalescent-based
140 analysis revealed evidence of historical mitochondrial introgression, suggesting that this species
141 pair has diverged with gene flow (Linnen & Farrell, 2007).

142 We hypothesize that adaptation to different pines and speciation-with-gene-flow in *N.*
143 *lecontei* and *N. pinetum* was facilitated by sex-limited hemizyosity and recombination. To
144 evaluate this possibility, we: (1) simulate diploid and haplodiploid “genomes” (500-kb loci)
145 evolving under mutation, drift, divergent selection, migration, and recombination; (2) model the
146 divergence history and characterize patterns of genomic differentiation in sympatric populations
147 of *N. lecontei* and *N. pinetum*; and (3) use our estimated divergence history and other system-
148 specific details to parameterize simulations of haplodiploid and diploid genomes evolving under
149 varying levels of selection. Our data support a faster-haplodiploid effect in *Neodiprion* sawflies,
150 and based on our results, we suggest that such effects may have promoted adaptation and
151 speciation in haplodiploid taxa.

152

153 **Methods**

154 *Simulation of haplodiploid and diploid chromosomes under divergence-with-gene-flow*

155 To evaluate the effects of hemizygous selection and sex-limited recombination on
156 genomic differentiation patterns, we simulated populations of diploid autosomes and
157 haplodiploid chromosomes (Figure 1). We used SLiM v3 (Haller & Messer, 2019) to simulate
158 500-kilobase (kb) chromosomes evolving via mutation, drift, migration, and selection, using X-

159 chromosomes to mimic haplodiploids and autosomes to mimic diploids. We considered an
160 isolation-with-migration model with two populations that diverged at some time (t_{div}) from an
161 ancestral population, with symmetric gene flow (Figure 1b). Simulations consisted of two
162 phases. First, to enable the ancestral population to reach mutation-drift equilibrium, we simulated
163 neutral evolution of an ancestral population with an effective size of 1500 ($2N_e$), a mutation rate
164 of 2.5×10^{-7} /bp/generation, and a recombination rate of 2.5×10^{-7} /bp/generation for 10,000
165 generations ($>4N_e$ generations). Second, to simulate divergence-with-gene-flow, the ancestral
166 population splits into two equally sized populations ($2N_e$) that exchange migrants at a constant
167 and symmetrical migration rate ($m=m_{12}=m_{21}$). The timing of this split coincides with the onset of
168 divergent natural selection on a polymorphic site (initial frequency of derived allele a denoted as
169 q_0) located at the middle of the chromosome (250-kb). We modeled selection under a “parallel
170 dominance” fitness model in which the derived allele a is favored in population 1 and allele A
171 (ancestral allele) is favored in population 2, its dominance is the same irrespective of the
172 population (Figure 1a, as in Moran (1959); Lasne et al., (2017)). We chose this model to
173 facilitate comparison with previous work (Lasne et al. 2017) and because this model is consistent
174 with biochemical mechanisms underlying dominance (Curtis et al., 1994; Rosenblum et al.,
175 2010). Furthermore, we assumed identical selection coefficients (s) and dominance (h) in
176 diploids and haplodiploids, but because of direct selection in hemizygous males, the efficiency of
177 selection might differ (Supplemental Methods). Our model assumes there are separate sexes,
178 with equal numbers of diploid males and diploid females (diploid case) or equal numbers of
179 haploid males and diploid females (haplodiploid case). Our model also assumes equal migration
180 rates, similar distributions of offspring numbers for males and females, and that the fitness of

181 hemizygous males (A or a) is equal to the fitness of corresponding homozygous females (AA or
182 aa). Following the onset of selection, populations evolve for an additional 2000 generations.

183 To control for factors other than hemizygous selection and sex-limited recombination that
184 might also cause differences in genomic differentiation between diploids and haplodiploids, our
185 simulations were scaled so that haplodiploid and diploid chromosomes experience equivalent
186 effective levels of drift (same effective size - N_e), migration (m), and recombination (r) (i.e., have
187 identical scaled mutation rate ($\theta=4N_e\mu L$), scaled recombination rate ($\rho=4N_e rL$), and scaled
188 migration rate ($2N_e m$) (Supplementary Table S1)). Thus, we adjusted the N_e to ensure that both
189 the diploid and haplodiploid chromosomes have $2N_e=1500$, which is the N_e of a hemizygous
190 locus with $N=1000$ individuals (500 females with two copies and 500 males with one copy). This
191 corresponds in the diploid case to $N_D=750$ individuals, obtained as $N_D=xN$ individuals, where x
192 is a scaling factor that is $3/4$ for 0.50 sex-ratio (Supplementary Methods). Because a haplodiploid
193 chromosome spends $2/3$ of the time in the sex in which it recombines (Kong et al., 2002; Wilfert
194 et al., 2007), to ensure identical average recombination rates in diploids and haplodiploids we
195 scaled the SLiM diploid recombination rate as $2/3$ of the recombination rate specified in SLiM
196 for haplodiploids (because males do not recombine). To confirm our scaling, we verified that the
197 values of several summary statistics measuring diversity, differentiation, and linkage
198 disequilibrium were identical for neutral simulations for haplodiploid and diploid chromosomes,
199 and that they converged to the expected values under neutrality (Supplementary Figure S1). The
200 parameter values above are identical to a scaled mutation rate ($\theta=4N_e\mu L$) and recombination rate
201 ($\rho=4N_e rL$) of a 500-kb chromosome in a population with an effective size of $2N_e=100,000$ and a
202 mutation rate of 2.5×10^{-9} bp/generation. We used a smaller effective population size of 1500 and
203 scaled the other parameters accordingly to reduce the computational burden of forward

204 simulations, as is usually done when using SLIM (e.g., Phung et al., 2016). Our chosen
205 divergence time correspond to a divergence with a scaled time $T_{div}/(4N_e)=2/3$, which is within the
206 range of values estimated for pairs of closely related populations and species across many taxa
207 (Hey & Pinho, 2012; Pinho & Hey, 2010), but lower than the threshold of $T_{div}/(4N_e)>1$ (and
208 $2N_em<1$) proposed by Hey and Pinho (2012) as a diagnostic for fully independent species.

209 We simulated diverging populations under all possible combinations of seven selection
210 coefficients (scaled $2N_es \sim 0, 10, 20, 40, 80, 100, 200$), four migration rates (scaled $2N_em \sim 0.0,$
211 $0.5, 2.5, 5.1$), two dominance coefficients (recessive $h=0.01$ and codominant $h=0.50$), and four
212 different starting allele frequencies ($q_0 = 1/(2N_e), 0.01, 0.10,$ and 0.50 ; Supplementary Table S1).
213 These parameters were chosen to capture a range of selection coefficients and migration rates,
214 including the neutral case ($s=0$) and the no-migration case ($m=0$). Our values of $2N_em$ were
215 chosen such that they fell both below and above the threshold for divergence via drift $2N_em = 1$
216 (Hey and Pinho, 2012). Our values of $2N_es$ range from 10x the threshold for selection to be
217 considered “nearly neutral” ($2N_es=1$) to 200x that threshold, corresponding to moderate to strong
218 selection (Lasne et al. 2017). For the populations we modeled, these are equivalent to $s = 0.007 -$
219 0.133 , which correspond well to empirical estimates of s from natural populations (Thurman &
220 Barrett, 2016). The starting allele frequencies ranged from new ($q_0=1/(2N_e)$) or rare ($q_0=0.01$)
221 mutations to common variants ($q_0=0.10$ and 0.50). To investigate the impact of recombination
222 rate on linked variation we repeated a subset of these conditions (with $q_0=0.10$ and 0.50) under a
223 lower recombination rate ($r=0.1\mu= 2.5\times 10^{-8}$ /bp/generation). For each unique combination of
224 parameters, we performed 1000 simulations.

225 For each replicate, we followed the trajectories of allele frequencies at the selected site in
226 both populations, which were used to compute the number of simulations that retained the

227 derived allele a in population 1. To investigate patterns of variation in samples rather than at the
228 population level, in the last generation we sampled 20 chromosomes of 500 kb from each
229 population. For each parameter combination, we computed average nucleotide diversity, D_{xy} and
230 weighted F_{ST} across simulations using the Hudson estimator (Bhatia et al., 2013), averaged
231 across all SNPs at three scales: (1) a 20-kb window centered on the selected site (“20-kb”); (2)
232 across the 500-kb chromosome (“500-kb”); and (3) scan of contiguous non-overlapping 20-kb
233 windows (“genome scan”). We used these two window sizes to investigate the effects of
234 haplodiploidy on sites closely linked to the selected site and on a chromosomal level in a manner
235 that would mimic an empirical dataset used for genome wide scans. To measure patterns of
236 linkage disequilibrium, we computed average r^2 between all pairs of SNPs within 20-kb
237 windows. To evaluate the effect of loss of the derived allele a , we used two approaches: in the
238 “all simulations” approach, the mean of summary statistics (e.g., F_{ST}) was computed across all
239 simulations, whereas in the “conditional” approach, the mean of summary statistics is computed
240 only across simulations where the derived allele was retained in population 1 (Figure 1c). Thus,
241 the “conditional” approach removes the effect of allele loss. Parameter combinations for which
242 fewer than 10 simulations were retained were treated as missing data.

243 Empirical data: estimating divergence history in a haplodiploid species pair

244 *Population sampling*

245 We sampled 23 *N. pinetum* larvae and 44 *N. lecontei* larvae from Kentucky
246 (Supplementary Table S2). Larvae tend to be found in gregarious colonies of siblings in both
247 species. To ensure we were not sampling close relatives, each individual was collected from a
248 different colony. To maximize our chances of sequencing diploid female larvae, which tend to be
249 larger than haploid male larvae, we extracted DNA from large larvae and verified sex with

250 heterozygosity estimates. To evaluate whether there is ongoing hybridization between these
251 species, we also sampled 3 individuals from Kentucky with intermediate larval pigmentation
252 (suspected hybrids) and one lab-reared female F₁ hybrid as a positive control (Supplementary
253 Table S2). An additional 18 *N. lecontei* samples from an allopatric population in Michigan
254 (Supplementary Table S2) and 1 *N. virginiana* from Blackstone, VA (37°06'47.2"N,
255 78°01'37.4"W) were sequenced for use in demographic analyses.

256 *DNA sequencing*

257 We extracted DNA using a CTAB/phenol-chloroform-isoamyl alcohol method (Chen,
258 Rangasamy, Tan, Wang, & Siegfried, 2010). We visualized the DNA on a 0.8% agarose gel to
259 confirm quality. To quantify the DNA, we used a Quant-iT High-Sensitivity DNA Assay Kit
260 (Invitrogen – Molecular Probes, Eugene, OR, USA). For *N. pinetum*, *N. lecontei*, and hybrids,
261 we used a modified ddRAD sequencing protocol from Bagley et al. (2017) and Peterson et al.
262 (2012). We fragmented the DNA using NlaIII and EcoRI. We assigned each individual along
263 with additional samples from other projects to one of eight libraries. During adapter ligation, we
264 assigned each sample one 48 unique in-line barcodes (Supplementary Table S2). We used the 5-
265 10 bp variable length barcodes used in Burford Reiskind et al. (2016). We then pooled each
266 group of samples and size selected for a 379-bp fragment (+/- 76bp) on a PippinPrep (Sage
267 Science, Beverly, MA). We did 12 rounds of high-fidelity PCR amplification (Phusion High-
268 Fidelity DNA Polymerase, NEB, Ipswich, MA) using PCR primers that included one of 12
269 unique Illumina multiplex read indices (Supplementary Table S2). To allow for the detection of
270 PCR duplicates, we included a string of 4 degenerate bases next to the Illumina read index
271 (Schweyen et al., 2014). We used a Bioanalyzer 2100 (Agilent, Santa Clara, CA) to check

272 library quality. The libraries were sequenced at the University of Illinois' Roy J. Carver
273 Biotechnology Center, using two lanes of Illumina HiSeq 4000 and 150-bp single-end reads.

274 For *N. virginiana*, which we used as an outgroup, we used 150-PE reads generated on an
275 Illumina Nextseq at the University of Georgia Genomics Facility (Vertacnik, 2020). Library
276 preparation and whole-genome shotgun sequencing were both completed at the sequencing
277 facility. We removed the adapters using cutadapt 1.16 and contaminants using the standard and
278 pine databases in Kraken (Martin, 2011; Wood & Salzberg, 2014).

279 *DNA processing and variant calling*

280 We aligned demultiplexed ddRAD reads to the *N. lecontei* reference genome (Nlec1.1
281 GenBank assembly accession number- GCA_001263575.2; Linnen et al., 2018; Vertacnik &
282 Linnen, 2015) using the very sensitive setting in bowtie2 (Langmead & Salzberg, 2012). We
283 only retained reads that aligned to one locus in the reference genome and had a Phred score
284 greater than 30. For the ddRAD dataset, we removed PCR duplicates using a custom script. We
285 called SNPs in samtools (Li et al., 2009). Male and female larvae are morphologically
286 indistinguishable. To identify putative haploid males, which are expected to have unusually low
287 heterozygosity, we computed per-individual heterozygosity (as in Bagley et al., 2017). No
288 individuals were excluded based on heterozygosity. We required all sites to have a minimum of
289 7x coverage and 50% missing data or less. We also removed SNPs with significantly more
290 heterozygotes than expected under Hardy-Weinberg equilibrium (an indicator of
291 genotyping/mapping error). We removed any individual that was missing more than 70% of the
292 data. We performed all filtering in VCFtools v0.1.13 (Danecek et al., 2011).

293 We created several datasets with subsets of individuals and additional filtering for each of
294 the population genetic analyses. We generated three data sets with minor allele filtering (MAF,

295 SNPs <0.01 removed): 1) sympatric *N. pinetum* and *N. lecontei* for genome-wide patterns of
296 divergence (36,935 SNPs), 2) sympatric *N. pinetum*, *N. lecontei*, and hybrids for admixture
297 analysis (35,649 SNPs), and 3) sympatric *N. pinetum*, *N. lecontei*, allopatric *N. lecontei*, and
298 outgroup *N. virginiana* for ABBA- BABA tests (12,905 SNPs). We also generated a down-
299 sampled dataset (described below) without a MAF filter for estimating site-frequency spectra
300 (SFS) that included sympatric *N. pinetum*, *N. lecontei*, and *N. virginiana* for demographic
301 analyses.

302 *Population structure, demographic analysis, and genomic differentiation*

303 To confirm that our suspected hybrids were genetically admixed, we used Admixture
304 v1.3.0 (Alexander et al., 2009) to estimate the proportion of ancestry for each individual
305 collected in Kentucky (*N. lecontei*, *N. pinetum*, lab-reared hybrids, and suspected field-caught
306 hybrids) from K populations for $K = 1- 5$. We ran 100 replicates per K and chose the K with the
307 lowest cross-validation (CV) score (Supplementary Table S3). Additionally, to test for
308 introgression between sympatric *N. lecontei* (P1) and *N. pinetum* (P3), we performed an ABBA-
309 BABA test (Patterson et al., 2012) with Kentucky *N. lecontei* (P1), Michigan *N. lecontei*
310 (allopatric population, P2), Kentucky *N. pinetum* (P3) and *N. virginiana* (outgroup, P4). We used
311 custom R script to compute the ABBA-BABA assuming that the outgroup is not fixed for the
312 ancestral allele (Patterson et al., 2012), assessing significance with block-jackknife resampling
313 dividing data into 645 blocks of ~20 SNPs.

314 To evaluate the timing and magnitude of gene flow between *N. lecontei* and *N. pinetum*,
315 we performed demographic modeling based on the site frequency spectrum (SFS) using the
316 composite likelihood method implemented in fastsimcoal2 v2.6 (Excoffier et al., 2013). For this
317 analysis, we used ddRAD data from sympatric populations of *N. lecontei* and *N. pinetum* filtered

318 as described above, with additional filters applied to satisfy analysis assumptions. First, to
319 minimize the impact of linked selection on demographic history estimates, we used the NCBI
320 *Neodiprion lecontei* Annotation Release 100 (updated to GCA_001263575.2) to exclude SNPs
321 that were in or within 1 kb of the start or end of a gene, thereby generating a set of putatively
322 neutral markers. Furthermore, to reduce bias in the SFS, we applied more stringent depth-of-
323 coverage filters, requiring a minimum depth of 10x and a maximum depth less than 2x the
324 median depth of coverage per individual. To build the 2D-SFS without missing data, each
325 scaffold was divided into non-overlapping 50-kb blocks, and we kept only blocks where the
326 median distance between SNPs was larger than 2bp. SNPs without missing data were obtained
327 for each block by downsampling four and six females from *N. pinetum* and *N. lecontei*,
328 respectively. This resulted in a downsampled dataset with 9,994 SNPs. To polarize the
329 ancestral/derived state of alleles and obtain the unfolded 2D-SFS we used data from *N.*
330 *virginiana*. To obtain the number of invariant sites in the 2D-SFS we assumed that the proportion
331 of SNPs removed because of extra filters was the same for invariant sites. Given a proportion of
332 number of SNPs to number of invariant sites before extra filters of ~0.046, the number of
333 invariant sites in the 2D-SFS after filters was set to 215,283.

334 We tested five alternative demographic scenarios: (1) divergence without gene flow, (2)
335 divergence with continuous bidirectional migration, (3) divergence in isolation followed by a
336 single bout of secondary contact (bidirectional gene flow), (4) divergence with bidirectional
337 migration that stops before divergence is complete, and (5) divergence in isolation followed by
338 continuous secondary contact (bidirectional). All models except the model of continuous gene
339 flow had an equal number of parameters, so we compared their likelihoods directly. We ran each
340 model 100 times starting from different parameter combinations, each run with 50 optimization

341 cycles (-150) and approximating the expected SFS with 100,000 coalescent simulations (-
342 n100000). We selected the run with the highest likelihood to estimate parameter values.

343 To examine genome-wide patterns of genetic divergence, we computed F_{ST} and π in 100-
344 kb non-overlapping windows for *N. lecontei* and *N. pinetum* in VCFtools on the non-
345 downsampled dataset. To identify regions of the genome that were more or less differentiated
346 than expected under neutrality, we simulated 10,000 datasets under the inferred demographic
347 history for sawflies using coalescent simulations implemented in the R package *scrm* (Staab et
348 al., 2015). For each simulation, we computed F_{ST} as for the *Neodiprion* dataset (see above).
349 Outlier windows were defined as those above or below the 95% CI for F_{ST} obtained from the
350 10,000 simulations. Simulations were done assuming no recombination, 50% missing data (i.e.,
351 female samples sizes of 0.5×23 for *N. pinetum* and 0.5×44 for *N. lecontei*), and scaling theta
352 ($4N\mu$) such that the average number of SNPs per window across simulations were similar to the
353 observed in *Neodiprion* dataset.

354 Comparison of empirical haplodiploid data to simulated diploids and haplodiploids

355 To evaluate the potential influence of haplodiploidy on genomic differentiation between
356 *N. lecontei* and *N. pinetum*, we used SLiM v3 to simulate haplodiploid and diploid “genomes”
357 evolving under divergent selection and the demographic history estimated for our focal species
358 pair. Because *N. pinetum* is on the derived host plant (Linnen & Farrell, 2010), we modeled *N.*
359 *pinetum* as population 1 (where derived allele *a* is favored), and *N. lecontei* as population 2. For
360 these simulations, we also assumed a sex ratio of 70 females:30 males based on previously
361 published sex ratios for *N. lecontei* and *N. pinetum* (Craig & Mopper, 1993; Harper et al., 2016).
362 As in our first set of simulations, we scaled our simulations to ensure equivalent levels of drift,
363 migration, mutation rates and recombination between diploids and haplodiploids.

364 To reduce the computational burden of forward SLiM simulations we re-scaled
365 parameters such that under neutrality, the SFS obtained with SLiM was identical to the expected
366 SFS obtained under the demographic history inferred with fastsimcoal2. This was achieved by
367 ensuring that the scaled mutation rate $4N_A\mu L$ for L sites was identical in both cases, where N_A is
368 the ancestral effective size and μ is the mutation rate per site per generation. By considering a
369 mutation rate two orders of magnitude higher ($\mu=3.50\times 10^{-7}$ rather than the 3.50×10^{-9}
370 /bp/generation used for SFS-based inference) and that $L=5\times 10^5$ sites in SLiM corresponds to
371 $L=5\times 10^4$ sites in the 2D-SFS used for fastsimcoal2 (including SNPs and invariant sites), the
372 haploid effective population sizes were three orders of magnitude lower (328 for *N. pinetum*,
373 1093 for *N. lecontei* and 1982 for the ancestral population) and migration rates three orders of
374 magnitude higher (3.64×10^{-4} into *N. pinetum*, 1.71×10^{-5} into *N. lecontei*). The times of split were
375 scaled accordingly, resulting in 1548 generations (rather than 1.54×10^6). To obtain the number of
376 individuals N in SLiM that correspond to the above haploid effective sizes, we had to account for
377 the sex-ratio of 70 females:30 males (Supplementary Methods). Given the average of 19.02
378 SNPs in *Neodiprion* 100-kb windows (with gaps due to sparse ddRAD loci), the average number
379 of SNPs in SLiM simulations under neutrality of 2,257 would correspond to ~10Mb of a similar
380 ddRAD dataset. We considered recombination rate r to be three times higher than mutation rate
381 ($r=1.05\times 10^{-6}$) using an estimate of 3.43 cM/Mb based on a linkage map for *N. lecontei*
382 constructed from an inter-population cross (Linnen et al., 2018). To ensure the same average
383 recombination rate for diploids and haplodiploids, the rate given as input in SLiM for diploids
384 was scaled by (2/3) as done for the simulation study (see above). Because the per-locus selection
385 estimate is unknown, we simulated differentiation and under a wide range of selection
386 coefficients s from 0.0 to 0.3. We also simulated all combinations of two dominance coefficients

387 ($h = 0.01$ and 0.50) and one starting allele frequency ($q_0 = 0.10$) (Supplementary Table S4). We
388 computed mean F_{ST} across all 1000 simulations for each starting allele frequency, dominance,
389 and selection coefficient combination. These combined simulations can be thought of as a
390 divergence history in which, on average, there is a divergently selected site every 10Mb.

391

392 **Results**

393 *Faster-haplodiploid effects on genomic differentiation with migration*

394 Across all parameter combinations and for both window sizes (20-kb and 500-kb), we
395 found that F_{ST} between haplodiploid populations was always equal to or greater than F_{ST} between
396 diploid populations (Figure 2). Migration and selection were both required for haplodiploid F_{ST}
397 to exceed diploid F_{ST} , and the ratio of haplodiploid F_{ST} : diploid F_{ST} was close to 1 for many
398 regions of parameter space. For both window sizes, we found that faster-haplodiploid effects
399 (i.e., ratio of haplodiploid F_{ST} : diploid $F_{ST} > 1$) were more pronounced in the recessive case
400 (Figure 2a-d) than in the codominant case (Figure 2e-h). For each dominance coefficient, the
401 regions of parameter space that *maximized* faster-haplodiploid effects depended on the window
402 size used to calculate F_{ST} . For sites tightly linked to the selected site (20-kb window), faster-
403 haplodiploid effects were maximized when migration was high ($2N_e m \geq 2.5$) and selection was
404 moderate ($10 \leq 2N_e s \leq 40$) (Figures 2b and 2f). By contrast, when we considered much larger
405 windows of 500-kb, relative differences between haplodiploid and diploid differentiation levels
406 were maximized at higher selection coefficients ($2N_e s \geq 40$) but at similar migration rates
407 ($2N_e m \geq 2.5$). The same trend—faster-haplodiploid effects maximized at higher selective
408 coefficients for the 500-kb windows than for the 20-kb windows—was found for all initial
409 frequencies of the derived allele a for the codominant case and for $q_0=0.5$ for the recessive case

410 (Supplementary Figure S2). However, for new ($q_0=1/(2N)$) or rare ($q_0=0.01$) recessive alleles,
411 faster-haplodiploid effects were always maximized at the highest selection coefficients,
412 regardless of window size (Supplementary Figure S2).

413 One mechanism leading to greater differentiation in haplodiploids was differential allele
414 retention. Simulations of haplodiploid populations had a higher probability of retaining the
415 derived allele across a wide range of parameter combinations (Figure 3, Supplementary Figure
416 S3). For recessive alleles, differences in allele retention between haplodiploids and diploids were
417 dependent on both starting allele frequency and selection strength, but relatively insensitive to
418 migration rate (Figure 3a; Supplementary Figure S3). By contrast, outside of a slightly elevated
419 probability of retaining the derived allele at lower selection coefficients ($10 \leq 2N_e s \leq 20$, inset
420 panel in Figure 3b), differences in allele retention between haplodiploid and diploid populations
421 were minimal for the codominant case (Figure 3b). For both recessive and codominant cases,
422 increasing migration had a limited but consistent effect, leading to a lower probability of allele
423 retention.

424 To investigate the impact of haplodiploidy on genomic differentiation via mechanisms
425 other than differential allele retention, we computed average F_{ST} for each parameter combination
426 conditional on retaining the derived allele at the selected locus. For the recessive case,
427 controlling for the impact of differential allele retention decreased the magnitude of faster-
428 haplodiploid effects across all parameter combinations (Figure 4a vs. 2b and Figure 4e vs. 2d),
429 indicating that the increased retention of the derived allele in haplodiploids contributed to faster-
430 haplodiploid effects. Compared to the recessive case, conditioning on allele retention had much
431 less of an impact on the magnitude of faster-haplodiploid effects for the codominant case
432 (Supplementary Table S5). The heatmaps in Figure 5a and 5e are nearly identical to those in

433 Figure 2f and 2h, respectively. This is unsurprising since differences in allele retention were
434 minimal in the codominant case (Figure 3). Once we conditioned on retaining the derived allele,
435 starting allele frequency had little impact on patterns of faster-haplodiploid evolution
436 (Supplementary Figure S4; for comparison see Supplementary Figure S2). Finally, as expected,
437 decreasing the recombination rate increased the magnitude of faster-haplodiploid effects on
438 linked variation (Supplemental Figure S5).

439 The observation that haplodiploid F_{ST} tends to exceed diploid F_{ST} even after conditioning
440 on retaining the derived allele (Figure 4a,b,e,f; Figure 5a,b,e,f) indicates that mechanisms other
441 than differential allele retention contribute to elevated differentiation in haplodiploids. To
442 explore these mechanisms, we examined allele trajectories (Figure 4c,d; Figure 5c,d) and
443 chromosome-wide F_{ST} patterns (Figure 4g,h; Figure 5g,h) under high migration ($2Nm=5.1$) and
444 two selection intensities (moderate: $2Ns=40$ and strong: $2Ns=200$). These plots revealed two
445 sources of faster-haplodiploid effects in addition to differential allele retention (see Supplemental
446 Results for additional explanation of these mechanisms). First, during the initial stages of
447 divergence, haplodiploids reached migration-selection equilibrium faster than diploids:
448 approximately $\sim 3x$ faster for the recessive case (Figure 4c,d) and $\sim 1.2x$ faster for the codominant
449 case (Figure 5c,d). The faster time to equilibrium in the codominant, strong-selection case
450 resulted in a chromosome-wide faster-haplodiploid effect even though there was no difference in
451 F_{ST} at the selected site (Figure 5h). Second, once migration-selection equilibrium was reached,
452 haplodiploids tended to be more efficient than diploids at eliminating maladapted immigrant
453 alleles in one or both populations (Figure 4c,d; Figure 5c), resulting in elevated differentiation at
454 sites tightly linked to the selected site (Figure 4 g,h; Figure 5g). Under strong selection and
455 codominance, however, both haplodiploids and diploids were efficient at removing maladapted

456 immigrant alleles from both populations (Figure 5d), resulting in similar differentiation levels at
457 the selected site (Figure 5h).

458 Overall, our simulations suggest so long as there is migration, haplodiploidy will lead to
459 elevated differentiation at selected sites and linked neutral sites when populations diverge via
460 divergent selection. This “faster-haplodiploid effect” is produced under a wide range of selection
461 coefficients; regardless of whether selection acts on new mutations, rare standing genetic
462 variation, or common standing genetic variation; and regardless of whether selection acts on
463 recessive or codominant alleles (Figure 2, Supplementary Figure S2). Finally, while the effects
464 of hemizygous selection and sex-limited recombination tend to be most pronounced at selected
465 sites and tightly linked neutral sites (20-kb windows), faster-haplodiploid effects can extend far
466 beyond the selected site (500-kb windows, which translates to ~4.4 cM in our simulations).

467

468 *Demography and genomic differentiation in pine sawflies*

469 *Neodiprion lecontei* and *N. pinetum* differ in many host-related traits (Figure 6A). Our
470 admixture analysis of *N. lecontei*, *N. pinetum*, a lab-reared F₁ hybrid, and three suspected wild-
471 caught hybrids supported two distinct genetic clusters (K=2; Supplementary Table S3). Putative
472 wild hybrids were indistinguishable from the lab-reared hybrid, and all four individuals were
473 genetically admixed with approximately equal contributions from *N. pinetum* and *N. lecontei*
474 (Figure 6B). The only other admixed individual detected was morphologically indistinguishable
475 from *N. pinetum*, but an estimated ~13% of its genome came from *N. lecontei*. In addition to
476 finding evidence of recent admixture, an ABBA-BABA test revealed evidence of historical
477 introgression between sympatric *N. pinetum* and *N. lecontei* populations ($D=0.18$; $P = 2.12 \times 10^{-15}$).
478 Finally, demographic models that had no migration or only a single burst of admixture were

479 far less likely than models that included continuous migration (Table 1). Together, these results
480 support a divergence-with-gene-flow scenario for *N. lecontei* and *N. pinetum* (Figure 6C).

481 Comparing three different models that included migration (starting after divergence,
482 stopping before the present day, or continuous migration), our SFS data were most likely under
483 the model that had the fewest parameters: a continuous migration model (Table 1). Maximum
484 likelihood parameter estimates under this model suggest that *N. pinetum* and *N. lecontei* diverged
485 $\sim 1.5 \times 10^6$ generations ago. Assuming 1-3 generations per year for KY populations of these
486 species (Benjamin 1955; Rauf and Benjamin 1980; CL, personal observation), this estimate
487 suggests that *N. pinetum* and *N. lecontei* likely diverged between 0.5 and 1.5 million years ago.
488 Our parameter estimates also suggest that *N. pinetum* has a smaller N_e than *N. lecontei*, and that
489 migration rates have been asymmetric, with more migration from *N. lecontei* to *N. pinetum* than
490 the reverse (Figure 6C, Table 1). Importantly, this model provides a good fit to the observed SFS
491 and other summary statistics (Supplementary Figure S6).

492 Despite continuous migration throughout divergence, genome-wide average F_{ST} was high
493 ($F_{ST} = 0.63$). However, differentiation levels varied widely across the genome, with localized
494 regions of both very high and very low F_{ST} (Figure 7). Using simulations according to the
495 inferred demographic history to generate 95% confidence intervals for F_{ST} under neutrality
496 revealed evidence of both high- F_{ST} and low- F_{ST} outliers in our empirical dataset (Figure 7).
497 These regions are candidates for divergent selection and adaptive introgression, respectively.
498 Nucleotide diversity (π) for both *N. pinetum* and *N. lecontei* also varied across the genome, but
499 *N. lecontei* had a higher average π (2.71×10^{-5}) than *N. pinetum* (1.95×10^{-5}), which is consistent
500 with the differences in effective population size between the two species (Table 1). Overall,
501 demographic modeling and genomic differentiation patterns are consistent with the hypothesis

502 that this species pair diverged with substantial gene flow, while experiencing divergent selection
503 at many unlinked locations throughout the genome.

504 *Expectations for faster-haplodiploid effects under inferred demographic model*

505 There were several differences between our simulations and our empirical system,
506 including lower migration rates and asymmetries in both effective population size and migration
507 rate (Table 1) as well as female-biased sex ratios (Harper et al., 2016). To capture some of these
508 system-specific characteristics, we simulated haplodiploid and diploid populations evolving
509 under the demographic model we estimated from our sawfly data. A comparison between our
510 observed summary statistics (SFS, F_{ST} , Π , D_{xy} , and r^2) for the putatively neutral intergenic
511 regions and summary statistics obtained from neutral simulations ($2N_s = 0$) shows that the
512 demographic model implemented in SLiM is working as expected, and that our simulated diploid
513 and haplodiploid chromosomes do not differ under neutrality (Supplementary Figure S6).

514 When we included divergent natural selection in our sawfly-parameterized simulations of
515 diploid and haplodiploid genomes, we once again observed faster-haplodiploid effects on the
516 “genome-wide” mean F_{ST} for both dominant and recessive alleles under a range of selection
517 coefficients (Figure 8). As observed for simulations under the simpler isolation-with-migration
518 model, the magnitude of this effect was highest for recessive alleles and moderate-to-strong
519 selection. These simulations also demonstrate that faster-haplodiploid effects can be observed
520 with female-biased sex ratios and with asymmetric migration.

521

522 **Discussion**

523 Haplodiploid taxa are numerous and ecologically diverse (Forbes et al., 2018; Hölldobler
524 & Wilson, 1990). While haplodiploid diversity could be due to low transition rates between

525 haplodiploidy and diploidy, it is also possible that haplodiploidy increases speciation rates
526 (Blackmon et al., 2017; Koevoets & Beukeboom, 2008; Lohse & Ross, 2015; Patten et al.,
527 2015). Here we explore one avenue through which haplodiploidy may facilitate speciation: by
528 increasing genomic differentiation and linkage disequilibrium between populations that diverge
529 with gene flow. Specifically, our simulations reveal that with both selection and migration,
530 haplodiploid populations will maintain higher levels of differentiation than comparable diploid
531 populations. This is true not only at the selected site, but also up to ~20 cM away. With the
532 sawfly empirical data, we identify a potential case of sympatric divergence via adaptation to
533 different hosts. Here, we discuss implications of these results for faster-X theory, evolution in
534 haplodiploids, and models of sympatric speciation. We also discuss some limitations of our
535 models and data and highlight priorities for future work.

536

537 *Faster-haplodiploid effects under divergence-with-gene-flow and relevance to faster-X theory*

538 Overall, our simulations demonstrate multiple mechanisms through which genomic
539 differentiation in haplodiploids is increased relative to diploids when populations diverge with
540 gene flow. Given similarities between the transmission genetics of haplodiploid genomes and X
541 chromosomes, these findings are also relevant to faster-X theory. As described below, our
542 simulations recapitulate several key results from previous work on faster-X theory, albeit in
543 some additional corners of parameter space (e.g., divergence-with-gene-flow via new or rare
544 mutations; *c.f.* Lasne et al., 2017). Based on our simulations, we can group faster-haplodiploid
545 effects and mechanisms into three distinct phases. In the first phase, the dynamics of a
546 divergently selected, low-frequency allele is mostly determined by the risk of loss due to drift
547 (Figure 3, Supplementary Figure S3). The increased efficacy of selection and the high

548 probability of allele retention under haplodiploidy and a divergence-with-gene-flow scenario is
549 analogous to classical faster-X divergence among isolated populations in which dominance has a
550 large impact on the outcomes (e.g., Charlesworth et al., 1987; Vicoso and Charlesworth 2009;
551 Meisel and Connallon 2013; Charlesworth et al., 2018). However, assuming sufficient
552 recombination, differential allele retention during phase 1 has a minimal impact on
553 differentiation at linked neutral sites (e.g., compare Figures 2d and 2h to Figures 4e and 5e,
554 respectively).

555 Once populations escape phase 1 without losing the divergently selected allele, there is a
556 second transitional phase during which the increased efficacy of selection against locally
557 maladaptive alleles reduces effective migration rates and causes haplodiploid loci to differentiate
558 more rapidly than comparable diploid loci (Figures 4 and 5). Again, this is in line with classical
559 faster-X theory demonstrating shorter sojourn times for beneficial X-linked alleles in isolated
560 populations (Avery, 1984; Betancourt et al., 2004). Reduced sojourn times in phase 2 also reduce
561 opportunities for recombination between locally adaptive and maladaptive haplotypes, thereby
562 affecting linked variation (Figures 4 and 5), analogous to predictions for X-linked variation in
563 isolated populations (Betancourt et al., 2004; Owen, 1988).

564 Once diverging populations approach equilibrium between selection, migration, and drift,
565 they enter phase 3. In this phase, haplodiploidy increases the efficacy of selection against locally
566 maladapted immigrant alleles, resulting in higher allele frequency differences at hemizygous loci
567 compared to diploid loci (Figures 4 and 5). Consistent with deterministic results obtained under
568 similar demographic models (Lasne et al., 2017), we find that when populations remain
569 connected by gene flow, faster-haplodiploid effects occur irrespective of dominance. These
570 findings contrast with classical faster-X theory that has been developed for divergence in

571 isolation, which predicts increased substitution rate only when beneficial mutations are recessive
572 (e.g., Charlesworth et al., 1987; Vicoso & Charlesworth 2006; Meisel & Connallon 2013;
573 Charlesworth et al., 2018) or when codominance is accompanied by deviations from 50:50 sex
574 ratio (Vicoso & Charlesworth, 2009). Additionally, efficient selection against maladapted
575 migrant alleles in Phase 3 causes reduced opportunities for recombination in haplodiploids. This
576 mechanism produces faster-haplodiploid effects at neutral sites linked to both recessive and
577 codominant alleles (Figures 4 and 5). These results are also consistent with predictions from
578 deterministic continent-island models of secondary-contact for X-linked markers (Fraisie &
579 Sachdeva, 2021; Fusco & Uyenoyama, 2011; Muirhead & Presgraves, 2016). Despite several
580 important differences between our model and these secondary contact models, including
581 divergence scenario, migration direction, and the presence of drift, we reach qualitatively similar
582 conclusions. These similarities suggest that in the long term, after migration-selection-drift
583 equilibrium is reached, the impact of the initial phases is negligible.

584 Where our work departs most from previous faster-X theory is that—to better connect
585 theory to data—we have explicitly modeled the effects of sex-limited hemizyosity and
586 recombination on population genomic datasets. Here, a couple of surprises have emerged. First,
587 under some parameter combinations, faster-haplodiploid effects can be observed in loosely
588 linked neutral sites without corresponding effects at the selected site and tightly linked sites
589 (Figure 5h). These patterns, which are dependent on recombination rate, emerge when
590 haplodiploid populations diverge more rapidly than diploid populations, but ultimately reach the
591 same equilibrium allele frequency. In essence, more rapid differentiation and reduced
592 opportunities for recombination between divergently selected haplotypes in haplodiploids locks
593 linked variation into place, and moderate to strong selection prevents erosion of linkage even

594 with migration. In other words, haplodiploidy leads to larger genomic regions around the
595 selected site with reduced effective migration rate. One important implication of this finding is
596 that haplodiploidy can facilitate the establishment of other beneficial mutations that appear in
597 such genomic regions (Yeaman et al., 2016, see below).

598 Second, while previous work demonstrates that hemizygous selection will give rise to
599 faster-X effects at selected and linked sites, there has been some uncertainty as to how much of
600 the genome is likely to be impacted when there is recurrent migration (Presgraves, 2018). Here,
601 we show that with strong selection ($2Ns > 100$) and high migration ($2Nm \sim 5$), regions of elevated
602 differentiation in haplodiploid chromosomes will be higher and wider than in corresponding
603 diploid chromosomes. Moreover, divergent selection at a single haplodiploid locus can reduce
604 gene flow relative to the diploid case even at neutral sites more than 250-kb away, corresponding
605 to >4.40 cM in simulations under the symmetric isolation-with-migration model (Figures 4 and
606 5), or >21.5 cM in simulations with sawfly-specific parameters (Figure 8). Additionally, the
607 continent-island models of Fusco & Uyenoyama (2011) and Muirhead & Presgraves (2016)
608 predict that selection at X-linked (and, analogously, haplodiploid) sites can also impact unlinked
609 neutral markers. Assuming that at equilibrium, adaptive divergence-with-gene-flow dynamics
610 can be reasonably well approximated by the continent-island model, we speculate that localized
611 reductions in gene flow surrounding hemizygous loci could extend to the chromosome-wide
612 level.

613 Although our work better connects theory to empirical data, our models make several
614 simplifying assumptions that could impact patterns of faster-haplodiploid differentiation.
615 Relaxing these assumptions and creating more complex, but realistic, models are therefore
616 potentially fruitful avenues for future research. First, the genetic architecture of adaptation to

617 novel niches is likely much more complex than the simple single-locus model considered here
618 (i.e., adaptation is likely due to many loci with variable effect sizes, dominance coefficients, and
619 non-additive interactions). Although there has been some work on how divergent selection on
620 multiple, possibly interacting, loci impact genomic differentiation (e.g., Yeaman et al., 2016;
621 Aeschbacher et al., 2017), this has not been investigated in the context of hemizyosity (but see
622 Fusco & Uyenoyama 2011; Fraïsse & Sachdeva 2021). Second, the divergence model we
623 considered was also relatively simple, ignoring sex-specific effects such as sex-biased migration,
624 sex-specific selection, and the absence of dosage compensation. For instance, Lasne et al. (2017)
625 predicted that sex-specific migration has a large impact on faster-X effects in models with strong
626 migration ($m \gg s$). Third, we have considered a parallel dominance fitness landscape and the
627 magnitude of faster-X effects might differ for other models, although Lasne et al. (2017) found
628 similar results for both parallel and reversal dominance models. Fourth, we assumed that the
629 fitness of haploid males was equivalent to that of diploid homozygotes. Whether or not this is the
630 case depends on mechanisms of dosage compensation and allelic effects in haploid males, which
631 are not well understood (Gardner 2012; Hitchcock et al., 2022; but see Aron et al., 2005;
632 Dearden et al., 2006; Glastad et al., 2014). Finally, we have ignored the effects that removing
633 deleterious mutations with similar effects across populations may have on patterns of
634 differentiation in haplodiploids and diploids (Charlesworth et al., 1993; Charlesworth et al.,
635 1997). Making precise predictions about chromosome-wide levels in population genomic
636 datasets will require modeling these more complex scenarios, as well as considering local
637 variation in mutation and recombination rate.

638

639 *Implications for speciation in haplodiploids*

640 One of the longest running debates in evolutionary biology is over the plausibility and
641 prevalence of sympatric speciation, the evolution of reproductive isolation in absence of
642 geographical isolation (Berlocher & Feder, 2002; Bolnick & Fitzpatrick, 2007; Foote, 2018; Via,
643 2001). Because of their pronounced host specialization and lifelong association with their host
644 plants, *Neodiprion* sawflies have been hypothesized to undergo sympatric speciation (Bush,
645 1975a, 1975b; Knerer & Atwood, 1973; Linnen & Farrell, 2010). Although gene flow has been
646 ubiquitous throughout *Neodiprion* divergence (Linnen & Farrell, 2007) and *N. pinetum*'s range is
647 nested within *N. lecontei*'s range, species ranges have changed too much to reconstruct the
648 geographic context of speciation from present day range overlap (Linnen & Farrell, 2010). Here,
649 demographic modeling revealed that the model that best explains patterns of genomic variation
650 in *N. lecontei* and *N. pinetum* does not include a period of isolation (Table 1; Figure 6C).
651 However, distinguishing between models of sympatric divergence and secondary contact is
652 difficult (Sousa & Hey, 2013). This difficulty appears to be true for *N. lecontei* and *N. pinetum*
653 as well: models that included continuous migration either starting after a brief period of isolation
654 (~64000 generations) or ending right before the present day (~2000 generations) explained the
655 data nearly as well as a continuous migration model (Table 1). Although we cannot definitively
656 say speciation was sympatric, our top three models and ML parameter estimates all point to a
657 scenario in which gene flow was present throughout all or most of the divergence history of these
658 two species.

659 Previous work also demonstrates that differences in the pines that *N. lecontei* and *N.*
660 *pinetum* use are likely to generate divergent selection on many different types of traits, including
661 female oviposition traits, correlated male traits, and larval physiology (Bendall et al., 2020, 2017;
662 Benjamin, 1955; Coppel & Benjamin, 1965; Rauf & Benjamin, 1980; Wilson et al., 1992).

663 Consistent with a “multifarious” or “multidimensional” model of divergent selection (Feder &
664 Nosil, 2010; Rice & Hostert, 1993; White & Butlin, 2021), multiple unlinked loci exceeded
665 expected levels of differentiation under neutrality (Figure 7). We also observed multiple regions
666 of unusually low differentiation, which could be explained by adaptive introgression. We
667 acknowledge, however, that other mechanisms besides divergent selection and adaptive
668 introgression can cause dips and valleys in genome scans (Cruickshank & Hahn, 2014; Ravinet
669 et al., 2017). Thus, interpretation of these genome scans would be improved by characterizing
670 the genomic landscape of recombination and gene density, as well as mapping loci underlying
671 divergently selected traits.

672 Together with previous work characterizing reproductive barriers in this species pair
673 (Bendall et al., 2017), our demographic modeling and genome scan results support a scenario in
674 which adaptation to different pine trees drove the evolution of reproductive isolation in the
675 presence of substantial gene flow. There is little debate that, given sufficiently strong selection,
676 genetic and phenotypic differences, such as divergently selected host-use traits, can be
677 maintained in the face of gene flow. Instead, the primary objection to sympatric speciation has
678 been that gene flow and recombination will tend to break up associations among favorable
679 combinations of alleles and between divergently selected loci and loci that confer other
680 components of reproductive isolation (Felsenstein, 1981). Multiple mechanisms can help
681 overcome this “selection-recombination” antagonism, thereby aiding the evolution of
682 reproductive isolation when there is gene flow, including pleiotropy (“magic traits” wherein loci
683 underlying local adaptation also confer reproductive isolation (Servedio et al., 2011)) and
684 genomic features that reduce recombination (e.g., chromosomes inversions (Kirkpatrick &
685 Barton, 2006; Ravinet et al., 2017)). Because *Neodiprion* mate on the host plant, it is possible

686 that alleles underlying divergent host preferences also produce habitat isolation (Linnen &
687 Farrell, 2010). However, there is minimal evidence of chromosomal rearrangements that would
688 reduce recombination in *N. lecontei*-*N. pinetum* hybrids (Geib and Sim, personal
689 communication).

690 Even in the absence of “magic traits” and inversions, divergent selection can also
691 facilitate the evolution of reproductive isolation through effects on linked variation (divergence
692 hitchhiking; Via, 2009; Via & West, 2008) and, when there are multiple divergently selected
693 loci, via a genome-wide reduction in the effective migration rate (genome hitchhiking; Barton &
694 Bengtsson, 1986; Feder et al., 2012a,b; Flaxman et al., 2012, 2013). By simulating genomic
695 differentiation under divergent selection, our estimated demographic model, and other system-
696 specific details (sex ratio, recombination rate), we show that haplodiploid inheritance in *N.*
697 *lecontei* and *N. pinetum* likely increased differentiation at selected and linked loci relative to a
698 comparable diploid scenario (Figure 8). The impact of haplodiploidy was most pronounced for
699 recessive mutations and at intermediate selection coefficients, with effects extending over sizable
700 regions of the genome (comparable to ~10Mb). By increasing differentiation at linked sites,
701 haplodiploidy could facilitate both divergence hitchhiking and genome hitchhiking, thereby
702 promoting speciation-with-gene-flow. This hypothesis could be tested more directly via
703 simulations that examine the impact of haplodiploidy on non-neutral linked variation and
704 interactions between multiple loci (Feder et al., 2012b; Feder & Nosil, 2010; Flaxman et al.,
705 2012; Nosil & Feder, 2012; Via, 2012; Yeaman & Whitlock, 2011; Yeaman et al., 2016).

706

707 Conclusions

708 Overall, our work suggests that sex-limited hemizygosity and recombination, both of
709 which are maximized in Hymenoptera and other haplodiploid clades, can have substantial effects
710 on genomic differentiation in wild populations. One potential implication of this work is that
711 haplodiploid taxa are more likely to undergo sympatric speciation and can withstand greater
712 levels of gene flow during divergence, which may ultimately give rise to higher rates of local
713 adaptation and speciation. A comparative analysis of divergence history between diploids and
714 haplodiploids would be an informative step in testing this hypothesis. More generally, there are
715 potentially numerous evolutionary consequences of haplodiploidy that may shed light on patterns
716 of biodiversity and have implications that extend to non-haplodiploid taxa.

717

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1051 **Data accessibility statement**

1052 All the scripts used for SLiM v3 simulations (bash and Slim input files) and analysis of SLiM
1053 results (R scripts) are available on VCS's GitHub page (https://github.com/vsousa/EG_cE3c)
1054 ([dataset] Bendall et al., 2021a). *Neodiprion* sequencing reads are available via the NCBI SRA,
1055 accession numbers: SAMN23893940-SAMN23893944, SAMN23893948, SAMN23893960-
1056 SAMN23893963, SAMN23893965, and SAMN25157024-SAMN25157101 ([dataset] Bendall et
1057 al., 2021b). All VCF files, custom scripts, and input files for the analysis of sawfly data are
1058 available on DRYAD (<https://doi.org/10.5061/dryad.fbg79cnwx>) ([dataset] Bendall et al.,
1059 2021c).
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1062 **Author contributions**

1063 EEB, VCS, and CRL designed the research; EEB, VCS, RKB, and CRL performed the research;
1064 EEB, VCS, and CRL analyzed the data; EEB, VCS, and CRL wrote the paper, with input from
1065 all authors.

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Table 1. Maximum likelihood values and maximum-likelihood parameter estimates for the five demographic models tested.

| Parameters | No migration | Secondary contact - one burst of migration | Continuous migration that starts after divergence | Continuous migration that ends before present day | Continuous migration |
|---|---------------|--|---|---|----------------------|
| # of parameters estimated | 7 | 7 | 7 | 7 | 6 |
| Ancestral population size | 2075281 | 1962052 | 1971660 | 2006404 | 1982187 |
| <i>N. pinetum</i> population size | 645779 | 369032 | 322897 | 337579 | 328311 |
| <i>N. lecontei</i> population size | 1057278 | 1052921 | 1104528 | 1075336 | 1093739 |
| Time since divergence (generations) | 1010864 | 1255392 | 1542789 | 1553120 | 1548690 |
| <i>N. pinetum</i> bottleneck size | 717 | NA | NA | NA | NA |
| <i>N. lecontei</i> bottleneck size | 470 | NA | NA | NA | NA |
| Time since bottle neck | 1010854 | NA | NA | NA | NA |
| Admixture proportion from <i>N. pinetum</i> to <i>N. lecontei</i> | NA | 0.0060941 | NA | NA | NA |
| Admixture proportion from <i>N. lecontei</i> to <i>N. pinetum</i> | NA | 0.118292 | NA | NA | NA |
| Time since admixture | NA | 115046 | NA | NA | NA |
| Migration rate from <i>N. lecontei</i> to <i>N. pinetum</i> | NA | NA | 3.94E-07 | 3.63E-07 | 3.65E-07 |
| Migration rate from <i>N. pinetum</i> to <i>N. lecontei</i> | NA | NA | 1.64E-08 | 1.83E-08 | 1.71E-08 |
| Number of <i>N. pinetum</i> migrants | NA | NA | 0.1273259 | 0.1226254 | 0.1196984 |
| Number of <i>N. lecontei</i> migrants | NA | NA | 0.0181423 | 0.0196645 | 0.018665 |
| Time since migration started | NA | NA | 901891 | NA | NA |
| Time since migration ended | NA | NA | NA | 1906 | NA |
| Estimated maximum likelihood (log 10) | -33034.2 | -32805.5 | -32794.6 | -32795 | -32794.3 |
| Maximum observed likelihood (log 10) | -32727.9 | -32727.9 | -32727.9 | -32727.9 | -32727.9 |
| Maximum Likelihood (est-obs) | -306.3 | -77.6 | -66.7 | -67.1 | -66.4 |

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1071 **Figure Legends**

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1073 **Figure 1. Overview of simulation approach for evaluating faster-haplodiploid effects on**
1074 **genomic differentiation. A.** Fitness models for diploid chromosomes (diploid autosomes and
1075 haplodiploid females) and haploid chromosomes (haplodiploid males). This is a parallel
1076 dominance model in which the fitness of heterozygotes depends on the dominance of allele a ,
1077 which is assumed to be the same in both populations. Population 1 is the population where the
1078 derived allele is beneficial. **B.** Overview of stochastic simulations under an isolation-with-
1079 migration model. An ancestral population with an effective size of $2N_e=1500$ gene copies (i.e., a
1080 haplodiploid locus with 500 females and 500 males or a diploid locus with 375 females and 375
1081 males) of a 500-kb chromosome (dark grey bar) evolves for 10,000 generations to reach
1082 mutation-drift equilibrium. This population then splits into two equally sized populations. A
1083 divergently selected site at position 250-kb (red line) with two alleles (A and a) is introduced at
1084 the time of split, with an initial frequency q_0 of allele a in both populations. The populations
1085 evolve for $T_{div}=2000$ generations, experiencing symmetric migration at a constant rate. For each
1086 parameter combination, 1000 simulations were run. **C.** Two approaches were used to summarize
1087 simulation results. In the “all”-simulations approach, mean F_{ST} is computed across all
1088 simulations (i.e., including simulations in which the derived allele a was lost due to drift). In the
1089 “conditional” approach, mean F_{ST} is computed only using simulations for which the derived
1090 allele a was retained.

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1092 **Figure 2. Faster-haplodiploid effects as a function of strength of divergent selection,**
1093 **migration rate and dominance. (a, e, c, g)** Differentiation (F_{ST}) for haplodiploids and diploids
1094 with scaled migration rate $2Nm=5.1$ and varying scaled selective coefficients ($2Ns$) for different
1095 window sizes with selected site in the middle [(a, e) 20-kb, (c, g) 500-kb], and different
1096 dominance coefficients [(a, c) recessive ($h=0.01$) and (e, g) codominant ($h=0.50$)]. The points
1097 correspond to mean F_{ST} and the whiskers to the interquartile range based on 1000 simulations.
1098 (b, d, f, h) Heatmap of the ratio of haplodiploid to diploid (H/D) mean F_{ST} for different
1099 combinations of selective coefficients and migration rates for different window sizes [(b, f) 20-
1100 kb and (d, h) 500-kb], and dominance coefficients [(b, d) recessive ($h=0.01$) and (f, h)
1101 codominant ($h=0.50$)]. Results were obtained with 1000 simulations for each parameter
1102 combination with an initial frequency $q_0=0.10$, sampling 20 females from each population. The
1103 gray boxes and lines indicate the correspondence of mean differentiation values shown in (a, c, e,
1104 g) to heatmap F_{ST} ratios shown in (b, d, f, h). For heatmaps of the ratio of F_{ST} we considered that
1105 values between 0.95 and 1.05 to be 1.00 (i.e., no difference between haplodiploids and diploids).

1106

1107 **Figure 3. Effect of haplodiploidy on retaining the derived allele at the site under divergent**
1108 **selection.** Probability of retaining - Prob(retention) - the derived allele a for haplodiploid and
1109 diploid simulations at the two extremes of migration rates considered: no migration ($2Nm=0$;
1110 solid lines) and high migration ($2Nm=5.1$, dotted lines), for **a)** recessive ($h=0.01$), and **b)**
1111 codominant ($h=0.50$) mutations. In **b)**, inset shows a zoom for $2Ns$ values between 0 and 40.
1112 Probability of allele retention is calculated as the proportion out of 1000 simulations that retained
1113 the derived allele a in population 1 (where a is favored). 95% confidence intervals are Clopper-
1114 Pearson CI for proportions. These results are for an initial allele frequency of 0.10 ($q_0=0.10$).

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1116 **Figure 4. Faster-haplodiploid effects for a recessive ($h=0.01$) derived allele after removing**
1117 **the effect of differential allele loss. (a, e)** Heatmap of ratio of haplodiploid (H) to diploid (D)
1118 mean F_{ST} for a combination of selective coefficients and migration rates for different window
1119 sizes with the selected site at the middle: **(a)** 20-kb and **(e)** 500-kb. For heatmaps of the ratio of
1120 F_{ST} we considered that values between 0.95 and 1.05 to be 1.00 (i.e., no difference between
1121 haplodiploids and diploids). Labels **i** and **ii** indicate the two cases selected to illustrate allele
1122 trajectories and scans of differentiation. **(b, f)** F_{ST} for haplodiploids and diploids with high
1123 migration ($2Nm=5.1$) and varying selective coefficients ($2N_s$), for different window sizes: **(b)** 20-
1124 kb and **(f)** 500-kb. Points correspond to mean F_{ST} and whiskers to interquartile ranges. Labels **i**
1125 and **ii** indicate the two cases selected to illustrate allele trajectories and scans of differentiation.
1126 **(c, d)** Trajectories of allele frequencies at the site under divergent selection in both populations,
1127 for: **(c)** moderate selection ($2N_s=40$), and **(d)** strong selection ($2N_s=200$). Note that the time
1128 scale is different because equilibrium differentiation is reached faster under strong selection. **(g,**
1129 **h)** Scan of mean F_{ST} along the 500-kb chromosome in non-overlapping 20-kb windows, obtained
1130 for: **(g)** moderate selection ($2N_s=40$), and **(h)** strong selection ($2N_s=200$). Mean and interquartile
1131 F_{ST} are based on the simulations out of 1000 that kept the derived allele a in population 1 at the
1132 site under divergent selection. Results are for simulations with an initial frequency $q_0=0.10$,
1133 sampling 20 females from each population.

1134
1135 **Figure 5. Faster-haplodiploid effects for a codominant ($h=0.50$) derived allele after**
1136 **removing the effect of differential allele loss. (a, e)** Heatmap of ratio of haplodiploid (H) to
1137 diploid (D) mean F_{ST} for a combination of selective coefficients and migration rates for different
1138 window sizes with the selected site at the middle: **(a)** 20-kb and **(e)** 500-kb. For heatmaps of the
1139 ratio of F_{ST} we considered that values between 0.95 and 1.05 to be 1.00 (i.e., no difference
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1142 migration ($2Nm=5.1$) and varying selective coefficients ($2N_s$), for different window sizes: **(b)** 20-
1143 kb and **(f)** 500-kb. Points correspond to mean F_{ST} and whiskers to interquartile ranges. Labels **i**
1144 and **ii** indicate the two cases selected to illustrate allele trajectories and scans of differentiation.
1145 **(c, d)** Trajectories of mean allele frequencies at the site under divergent selection in both
1146 populations, for: **(c)** moderate selection ($2N_s=40$), and **(d)** strong selection ($2N_s=200$). Note that
1147 the time scale is different because equilibrium differentiation is reached faster under strong
1148 selection. **(g, h)** Scan of mean F_{ST} along the 500-kb chromosome in non-overlapping 20-kb
1149 windows, obtained for: **(g)** moderate selection ($2N_s=40$), and **(h)** strong selection ($2N_s=200$).
1150 Mean and interquartile F_{ST} are based on the simulations out of 1000 that kept the derived allele a
1151 in population 1 at the site under divergent selection. Results are for simulations with an initial
1152 frequency $q_0=0.10$, sampling 20 females from each population.

1153
1154 **Figure 6. Divergent selection and divergence-with-gene-flow in pine sawflies (*N. pinetum***
1155 **and *N. lecontei*). A.** *N. pinetum* (bottom row) and *N. lecontei* (top row) differ in multiple
1156 oviposition traits, such as host preference, oviposition stance (first column), ovipositor
1157 morphology (second column), and spacing and number of eggs per needle (last column),
1158 resulting in strong extrinsic postzygotic isolation. These oviposition traits along with additional
1159 host-use adaptations likely result in multiple independent regions of the genome experiencing
1160 divergent selection. **B.** Representative pictures of *N. pinetum*, *N. lecontei*, and F_1 hybrid larvae
1161 above an Admixture plot ($K=2$) of individuals sampled from Kentucky. *N. pinetum* ancestry is in

1162 white; *N. lecontei* ancestry is in grey. Lab-reared (N=1) and field-caught (N=3) hybrids are
1163 genetically admixed with approximately half of their ancestry coming from each species. **C.** *N.*
1164 *pinetum* and *N. lecontei* have diverged with continuous but asymmetric gene flow. Diagram is
1165 based on an estimated demographic model for this species pair, with width of boxes proportional
1166 to population size and width of arrows is proportional to migration rate (see Table 1).

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1168 **Figure 7. Genome scans of differentiation and diversity for *N. pinetum* and *N. lecontei*.**
1169 Genetic differentiation (F_{ST}) and genetic diversity (nucleotide diversity π) for *N. lecontei* and *N.*
1170 *pinetum* calculated in 100-kb windows. The red lines mark the 95% confidence interval obtained
1171 from data simulated under neutrality and the demographic model estimated for this species pair.

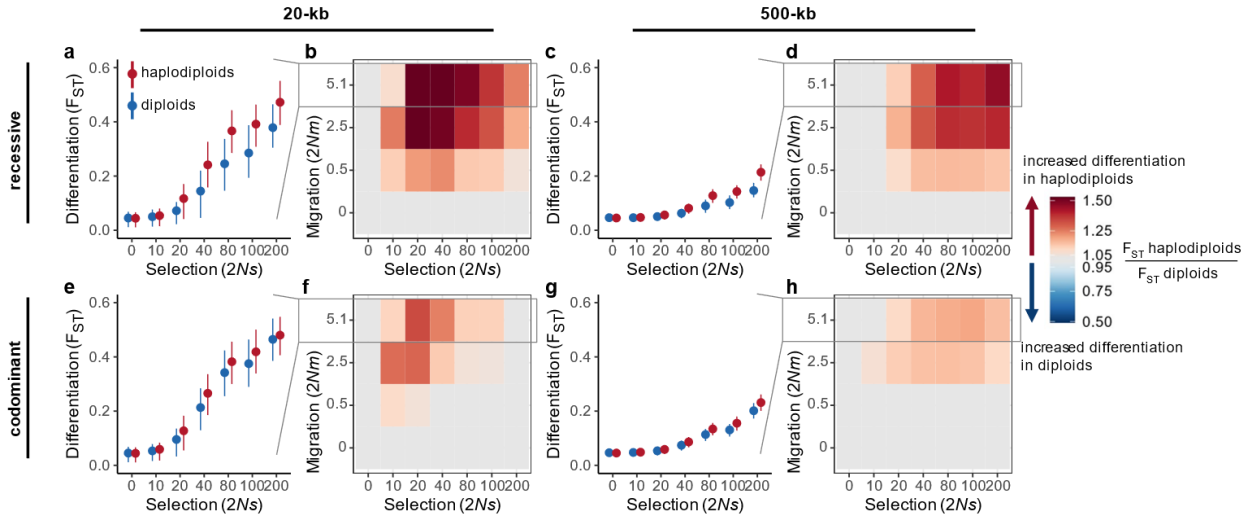
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1173 **Figure 8. Effect of haplodiploidy and divergent selection on differentiation under inferred**
1174 **demographic history of *Neodiprion* sawflies.** Results from simulations performed assuming a
1175 sex-ratio with a proportion of 0.7 females and 0.3 males. **(a-b, d-e)** Mean F_{ST} and interquartile
1176 range for diploid and haplodiploid populations as a function of selective coefficient for recessive
1177 **(a-b)** and codominant **(d-e)** mutations, for different window sizes centered at the selected site
1178 **(a,d)** 100-kb, **(b,e)** 10Mb. **(c, f)** Genome scan of F_{ST} for diploid and haplodiploid for recessive **(c)**
1179 and codominant **(f)** mutations, obtained with $s = 0.16$ and initial frequency of 0.1. Solid line
1180 corresponds to mean F_{ST} and shaded area indicates interquartile 0.25-0.75 range. Dashed lines in
1181 **(a-b, d-e)** indicate the selective coefficient used in genome scan shown in **c, f**. Note that in this
1182 model the two populations have different effective sizes (Supplementary Table S4) and hence the
1183 selection coefficients in the x-axis are not scaled by N_e . For $s=0.16$ this corresponds to scaled
1184 selective coefficients of approximately $2N_s=50$ for *N. pinetum* (where the derived allele is rare
1185 initially), and $2N_s=170$ for *N. lecontei*.

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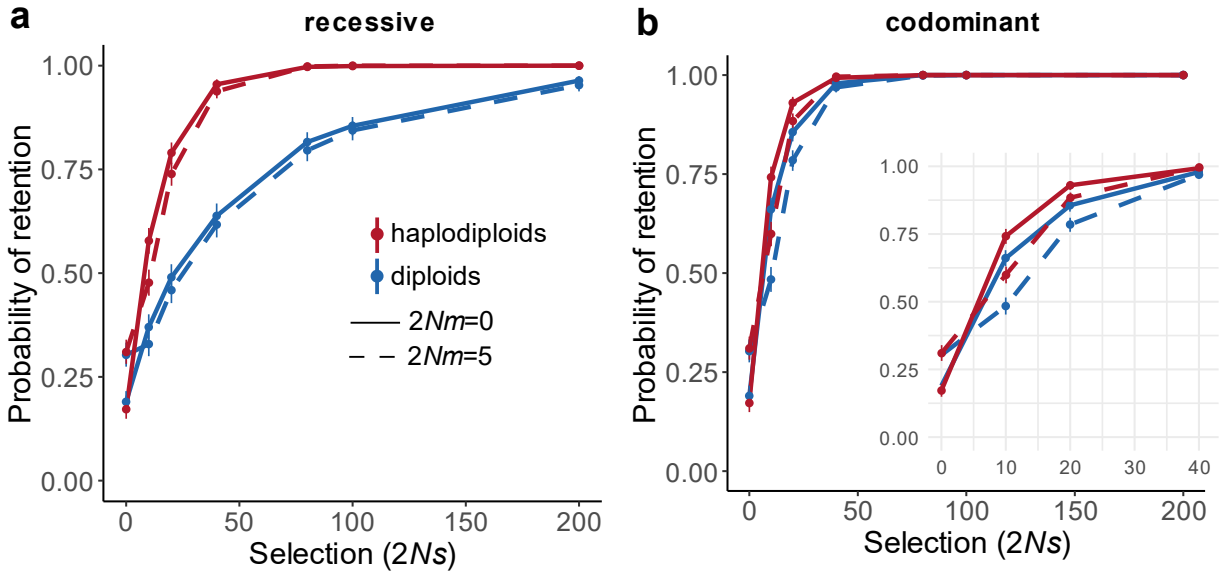
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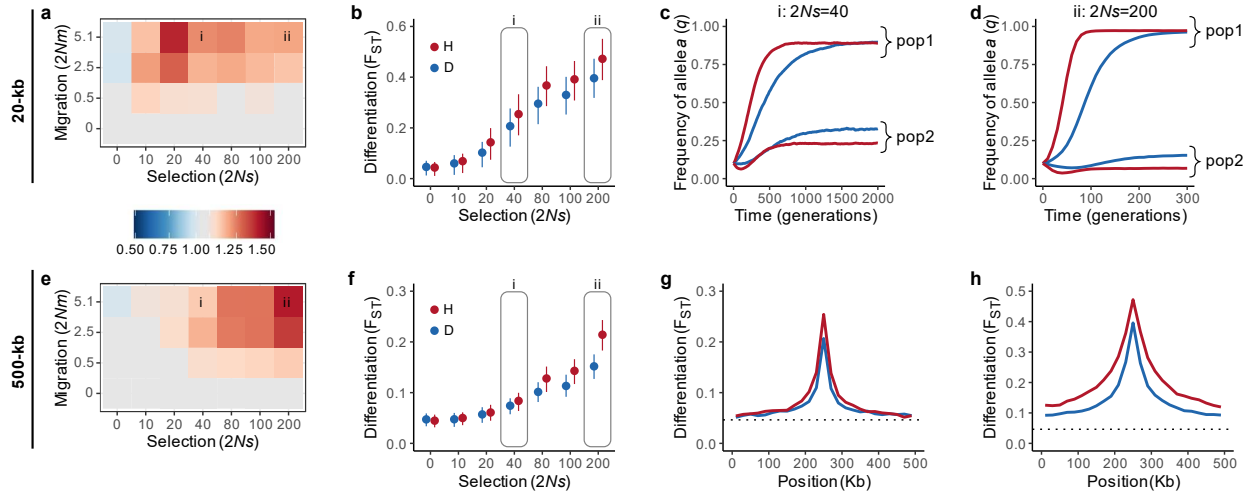


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 1219 (b, d, f, h) Heatmap of the ratio of haplodiploid to diploid (H/D) mean F_{ST} for different
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 1223 combination with an initial frequency $q_0=0.10$, sampling 20 females from each population. The
 1224 gray boxes and lines indicate the correspondence of mean differentiation values shown in (a, c, e,
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 1226 values between 0.95 and 1.05 to be 1.00 (i.e., no difference between haplodiploids and diploids).
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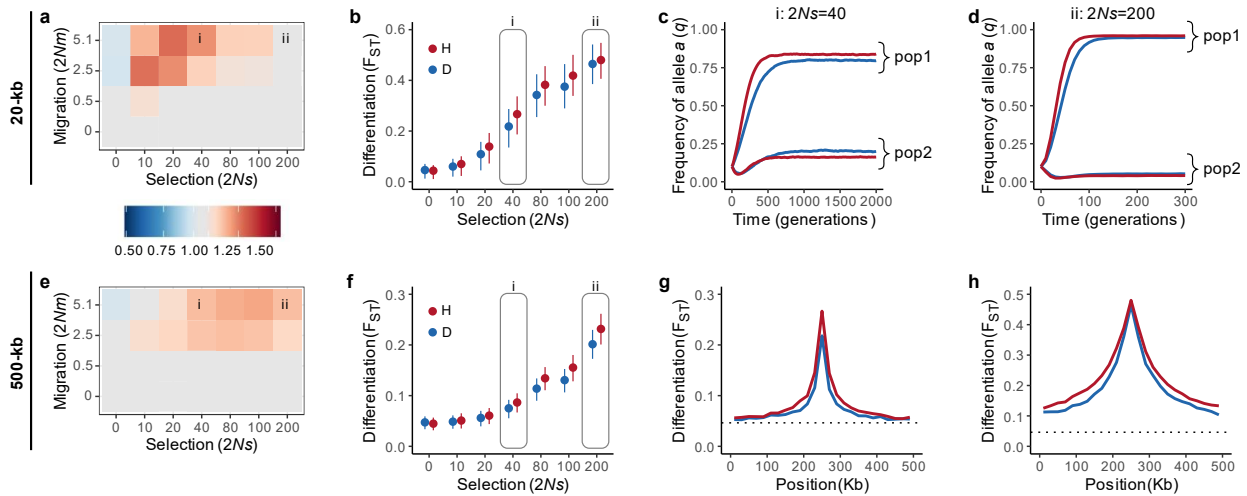
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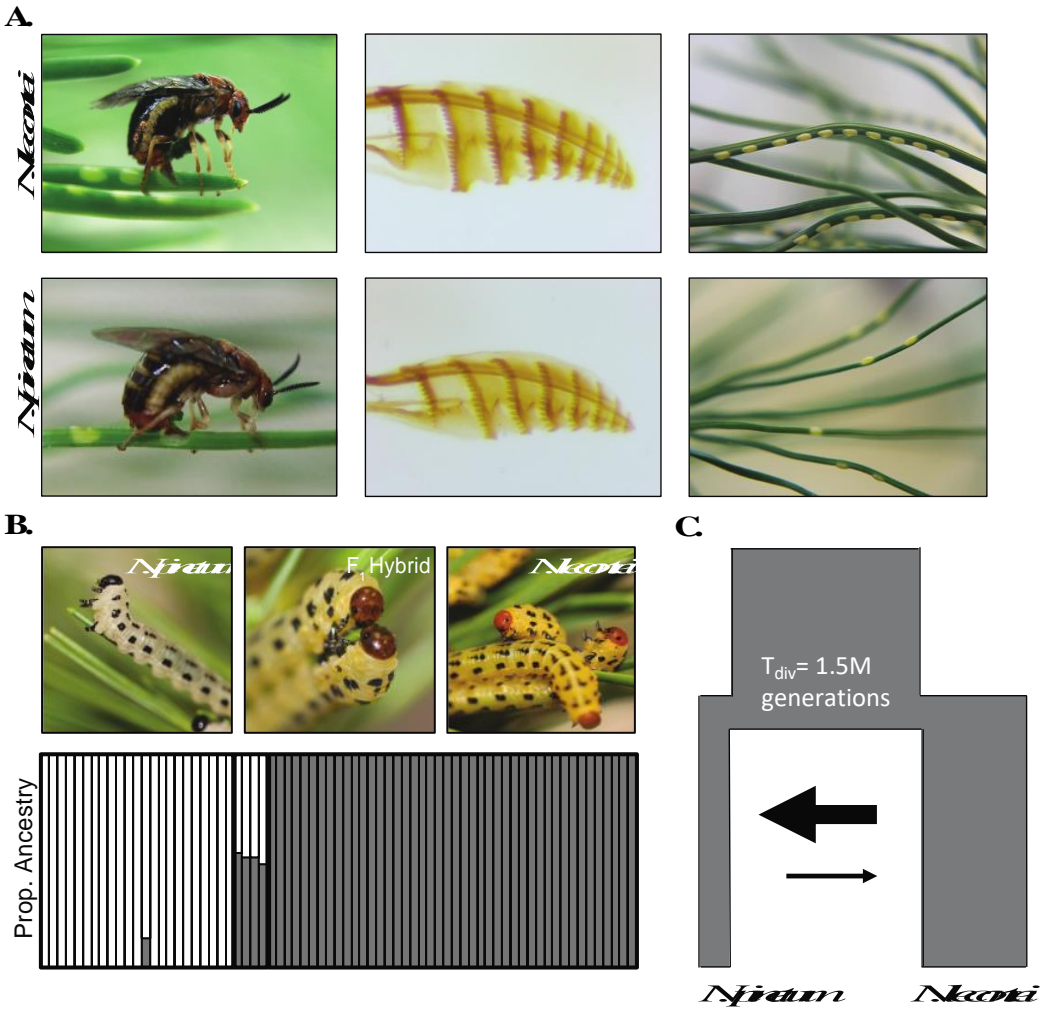
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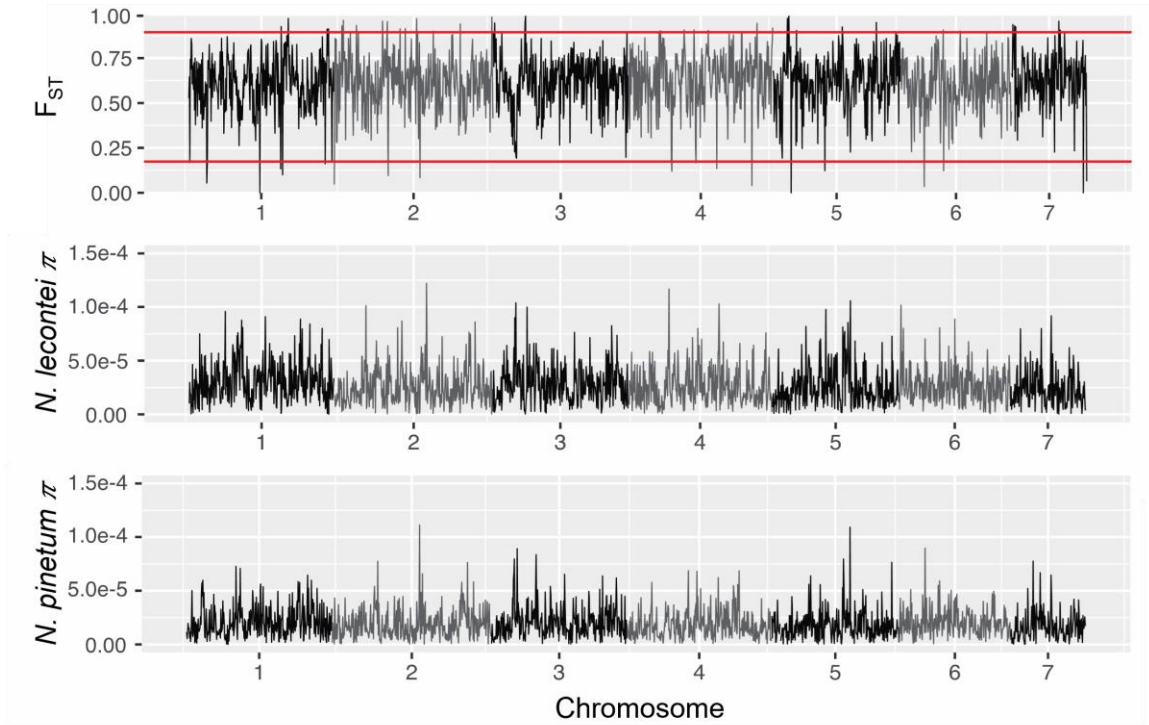
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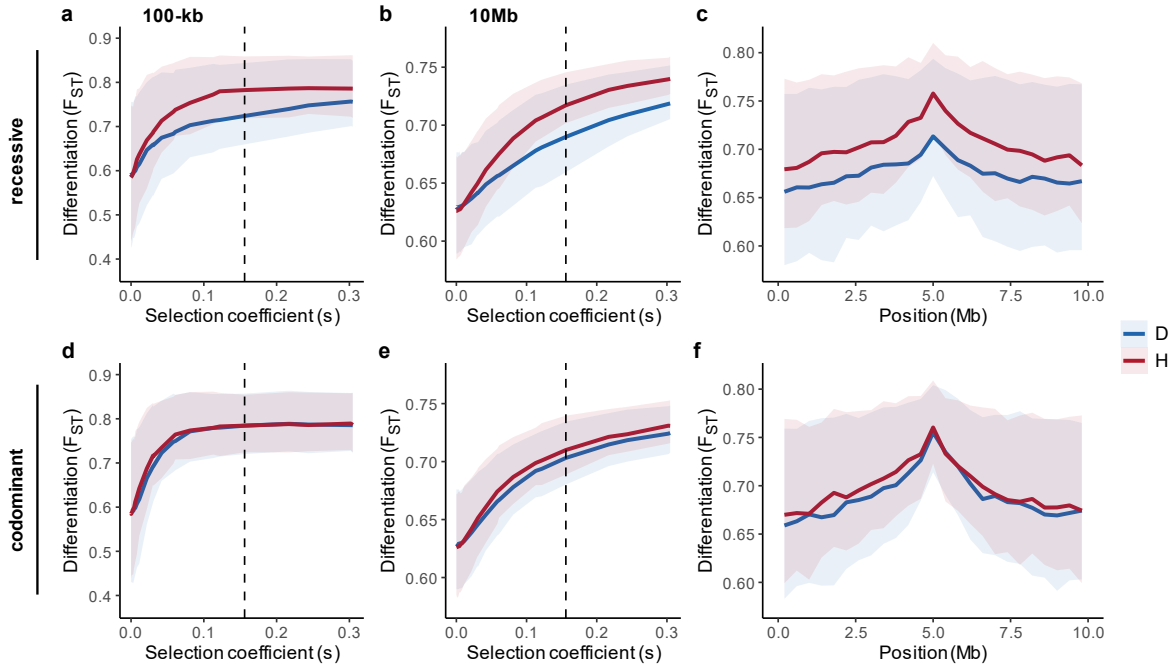


1279
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 1281 **and *N. lecontei*).** **A.** *N. pinetum* (bottom row) and *N. lecontei* (top row) differ in multiple
 1282 oviposition traits, such as host preference, oviposition stance (first column), ovipositor
 1283 morphology (second column), and spacing and number of eggs per needle (last column),
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Figure 7. Genome scans of differentiation and diversity for *N. pinetum* and *N. lecontei*. Genetic differentiation (F_{ST}) and genetic diversity (nucleotide diversity π) for *N. lecontei* and *N. pinetum* calculated in 100-kb windows. The red lines mark the 95% confidence interval obtained from data simulated under neutrality and the demographic model estimated for this species pair.



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 1304 **Figure 8. Effect of haplodiploidy and divergent selection on differentiation under inferred**
 1305 **demographic history of *Neodiprion* sawflies.** Results from simulations performed assuming a
 1306 sex-ratio with a proportion of 0.7 females and 0.3 males. **(a-b, d-e)** Mean F_{ST} and interquartile
 1307 range for diploid and haplodiploid populations as a function of selective coefficient for recessive
 1308 **(a-b)** and codominant **(d-e)** mutations, for different window sizes centered at the selected site
 1309 **(a,d)** 100-kb, **(b,e)** 10Mb. **(c, f)** Genome scan of F_{ST} for diploid and haplodiploid for recessive **(c)**
 1310 and codominant **(f)** mutations, obtained with $s = 0.16$ and initial frequency of 0.1. Solid line
 1311 corresponds to mean F_{ST} and shaded area indicates interquartile 0.25-0.75 range. Dashed lines in
 1312 **(a-b, d-e)** indicate the selective coefficient used in genome scan shown in **c, f**. Note that in this
 1313 model the two populations have different effective sizes (Supplementary Table S4) and hence the
 1314 selection coefficients in the x-axis are not scaled by N_e . For $s=0.16$ this corresponds to scaled
 1315 selective coefficients of approximately $2N_s=50$ for *N. pinetum* (where the derived allele is rare
 1316 initially), and $2N_s=170$ for *N. lecontei*.

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