

UNIVERSIDADE DE LISBOA
FACULDADE DE CIÊNCIAS
DEPARTAMENTO DE MATEMÁTICA

INSTITUTO SUPERIOR DE CIÊNCIAS
DO TRABALHO E DA EMPRESA
DEPARTAMENTO DE FINANÇAS



**Ciências
ULisboa**



CONSUMER CREDIT ANALYSIS: A VAR/ VECM METHODOLOGY

Inês Fernandes Claudina

Mestrado em Matemática Financeira

Dissertação orientada por:
Professora Doutora Diana Aldea Mendes

UNIVERSIDADE DE LISBOA
FACULDADE DE CIÊNCIAS
DEPARTAMENTO DE MATEMÁTICA

INSTITUTO SUPERIOR DE CIÊNCIAS
DO TRABALHO E DA EMPRESA
DEPARTAMENTO DE FINANÇAS



**Ciências
ULisboa**



CONSUMER CREDIT ANALYSIS: A VAR/ VECM METHODOLOGY

Inês Fernandes Claudina

Mestrado em Matemática Financeira

Dissertação orientada por:
Professora Doutora Diana Aldea Mendes

ACKNOWLEDGMENTS

A sincere thank you to the following people.

I would like to start thanking to the faculty members of the master's in financial mathematics for what they have taught me, and specially, to my thesis advisor Professor Diana Aldea Mendes. The door to Prof. Mendes office was always open whenever needed, she allowed this paper to be my own work but guided me in the right the direction whenever she thought I needed it.

I also want to thank to my colleagues Mariana, João and Francisco to help me through my Master, without all the study sessions, ideas exchange and companionship this experience would have been much harder and not so enjoyable. Then, I want to thank Nuno, that always encouraged me and kept me motivated through this process.

Finally, I must express my very profound gratitude to my parents for the continuous encouragement they have always given me, not only throughout my years of study and through the process of researching and writing this thesis, but at all times in my life, good or bad. This accomplishment would not have been possible without them. Thank you.

ABSTRACT

The main objective of this dissertation is to present an empirical analysis that is able to describe the credit channel for households in Portugal, focusing on the disparities caused by the 2008 crisis. For this purpose, it was analysed a set of four times series including GDP (GDP), 3 months Euribor rate (EURIBOR), Inflation Rate (CPI) and Households Consumer Credit (CC) between the first quarter of 2003 to the last quarter to 2018. The data used was taken from Pordata website.

The subject in question begins with the study of the stationarity of the time series and the significance of the same followed by the implementation of the VEC model to answer several questions around this topic. It will be done an Impulse response function analysis for the most appropriate estimated model to assess the effect of an impulse (or shock) to the time series.

The main interest in the use of these models is the possibility of separate the endogenous and exogenous components of monetary policy to study the dynamic of time series in the long-term and measuring the response of variables to unexpected shocks.

Keywords: Time series; Consumer Credit; VAR; VECM

RESUMO

O principal objectivo desta dissertação é apresentar uma análise empírica capaz de descrever o canal de crédito do sector privado em Portugal, com foco nas disparidades causadas pela crise de 2008. Para este propósito analisou-se um conjunto de quatro séries temporais, o Produto Interno Bruto (PIB), a taxa Euribor a 3 meses (Euribor), a taxa de inflação (IPC) e o crédito ao consumo do setor privado (CC) entre o primeiro trimestre de 2003 e o último trimestre de 2018. Os dados utilizados foram obtidos no site Pordata.

Começa-se com o estudo da estacionaridade das séries temporais e a significancia das mesmas, seguido pela implementação do modelo VEC para responder a várias questões. Posteriormente será feita uma análise da função Impulso-resposta para o modelo estimado mais apropriado para avaliar o efeito de um impulso (ou choque) na série temporal.

O principal interesse no uso desses modelos é a possibilidade de separar os componentes endógenos e exogenas da política monetária para estudar a dinâmica das séries temporais a longo prazo e medir a resposta das variáveis a choques inesperados.

Palavras-chave: Séries Temporais, Crédito ao Consumo; VAR; VECM

CONTENTS

INTRODUCTION	1
1. THEORETICAL FRAMEWORK	2
1.1 CREDIT CHANNEL THEORY	4
1.2 THE PORTUGUESE ECONOMY	4
1.3 LITERATURE REVIEW	6
2. MACROECONOMETRICS: CONCEPTS AND MODELS	7
2.1 TIME SERIES	7
2.2 VAR MODEL	10
2.3 VEC MODEL	12
2.4 ADF, PP AND KPSS TESTS	13
2.5 COINTEGRATION AND GRANGER CAUSALITY	14
2.5.1. ENGLE-GRANGER TEST	15
2.5.2. JOHANSEN TEST	16
2.5.3. GRANGER CAUSALITY	17
2.5.4. IMPULSE RESPONSE FUNCTION	18
3. DATA AND RESULTS	19
3.1 EMPIRICAL ANALYSIS	20
CONCLUSION	33
REFERENCES	35
APPENDIX A	37
APPENDIX B	41
APPENDIX C	45
APPENDIX D	47

LIST OF FIGURES

Figure 1 – The Circular Flow of Income	2
Figure 2 – Transmission mechanism of monetary policy	4
Figure 3 – Stationary time series (Juselius, 2006)	7
Figure 4 – Non-stationary time series (Juselius, 2006)	8
Figure 5 – Non-stationary behaviour	9
Figure 6 – VAR Model (Lutkepohl, 2005)	11
Figure 7 – Time Series logGDP, EURIBOR, CIP and logCC	20
Figure 8 – Time series consumer credit	21
Figure 9 – Histograms of the Series logGDP, EURIBOR, CIP and logCC	21
Figure 10 – Granger Causality Test	22
Figure 11 – Graphics of the first differences of the Series logGDP, EURIBOR, CIP and logCC	23
Figure 12 – Histograms of the first differences of the Series logGDP, EURIBOR, CIP and logCC	24
Figure 13 – VEC Residual Portmanteau Test for Autocorrelations	26
Figure 14 – VEC Residual Heteroskedasticity Test (Levels and Squares)	27
Figure 15 – VEC Residuals	28
Figure 16 – Cointegration relationship	29
Figure 17 – Impulse Response Function EURIBOR	30
Figure 18 – Impulse Response Function LCC_TOTAL	32

LIST OF TABLES

Table 1 – Bank lending channel conditions	3
Table 2 – ADF, PP and KPSS Test Hypothesis	10
Table 3 – Linear correlation coefficients between variables.....	22
Table 4 – Results for ADF, PP and KPSS Tests	23
Table 5 – Unit Root Test for the variables	24
Table 6 – Linear regression between variables.....	25
Table 7 – Johansen Trace Test	25
Table 8 – Normalized cointegration coefficients.....	28
Table 9 – Unit Root Test ADF of the variable LGDP in level.....	37
Table 10 – Unit Root Test PP of the variable LGDP in level.....	37
Table 11 – Stationarity Test KPSS of the variable LGDP in level	37
Table 12 – Unit Root Test ADF of the variable EURIBOR in level.....	38
Table 13 – Unit Root Test PP of the variable EURIBOR in level	38
Table 14 – Stationarity Test KPSS of the variable EURIBOR in level	38
Table 15 – Unit Root Test ADF of the variable CIP in level	39
Table 16 – Unit Root Test PP of the variable CIP in level.....	39
Table 17 – Stationarity Test KPSS of the variable CIP in level	39
Table 18 – Unit Root Test ADF of the variable LCC_TOTAL in level	40
Table 19 – Unit Root Test PP of the variable LCC_TOTAL in level.....	40
Table 20 – Stationarity Test KPSS of the variable LCC_TOTAL in level	40
Table 21 – Unit Root Test ADF of the variable LGDP - first difference	41
Table 22 – Unit Root Test PP of the variable LGDP - first difference	41
Table 23 – Stationarity Test KPSS of the variable LGDP - first difference	41
Table 24 – Unit Root Test ADF of the variable EURIBOR - first difference	42
Table 25 – Unit Root Test PP of the variable EURIBOR - first difference.....	42
Table 26 – Stationarity Test KPSS of the variable EURIBOR - first difference.....	42
Table 27 – Unit Root Test ADF of the variable CIP - first difference.....	43
Table 28 – Unit Root Test PP of the variable CIP - first difference	43
Table 29 – Stationarity Test KPSS of the variable CIP - first difference	43
Table 30 – Unit Root Test ADF of the variable LCC_TOTAL - first difference.....	44

Table 31 – Unit Root Test PP of the variable LCC_TOTAL - first difference	44
Table 32 – Stationarity Test KPSS of the variable LCC_TOTAL - first difference	44
Table 33 – R1: lcc_total c cpi	45
Table 34 – R2: lcc_total c euribor	45
Table 35 – R3: lcc_total c cpi	45
Table 36 – R4: cpi c euribor	46
Table 37 – R5: cpi c lgdp	46
Table 38 – R6: euribor c lgdp	46
Table 39 – Test Lags information criteria of Schwartz	47
Table 40 –VECM	48

ABBREVIATIONS

CPI – Consumer Price Index

EBF – European Banking Federation

ECB – European Central Bank

EFAP – Economic and Financial Assistance Programme

EU – European Union

EURIBOR – Euro Interbank Offered Rate

GDP – Gross Domestic Product

IMF – International Monetary Fund

HICP – Harmonized Index of Consumer Prices

LHS – Left Hand Side

LR – Likelihood Ratio

MLE – Maximum Likelihood Estimation

OECD - Organisation for Economic Co-operation and Development

OLS – Ordinary Least Squares

RHS – Right Hand Side

VAR – Vector Autoregressive

VECM – Vector Error Correction Model

INTRODUCTION

The constantly growing need for economic and financial information has been a major subject of study for investor groups, governments and even individuals participating in the financial markets that are looking for a basis for all their decisions. Forecasting economic indicators it is essential to the benefit of those directly or indirectly related to the local and international financial markets. Monetary policy can be a powerful instrument for the Central Banks and a subject of interest for economist and policymakers due its significant influence in achieving price stability (low and stable inflation) and to help to manage economic fluctuations.

We live in a period of time characterized by change, both economic and social. The world changed more since the beginning of the XXI century than in the last seventy years. These permanent changes need an active response as a way of survival. Financial innovation emerges in a continuous process as a consequence of the transformations that the business world suffered.

As stated by Brinkmeyer (2014) the recent crisis of 2008 has presented a major challenge to banks, monetary policymakers and the stability of the financial system as whole all over the world. The latter phases are still ongoing and with different repercussions in different economies. The present master thesis, having in mind this point, will analyse the consumption credit behaviour in the case of Portugal, in the time period between 2003 and 2018

This dissertation is organized in 3 chapters. Chapter 1 is an introduction to the economic and financial concepts in the context of the recent crisis, and also makes a brief review to the literature relating the relationship between these concepts and the macroeconometrics models that will be used. Chapter 2 explores the concepts of time series, stationarity, cointegration and causality focused on the VAR/VECM model. The empirical data and the process implemented with the help of Eviews software in order to obtain the results are described in Chapter 3. The thesis is finalized with the presentation of the conclusions.

1. THEORETICAL FRAMEWORK

The global economic and financial crisis of 2008 that originated in the United States and the bankruptcy of the American investment bank Lehman Brothers in September of the same year had negative effects on several financial institutions worldwide, a process that became known as the subprime crisis. The subprime lending crisis had a domino effect in the economy and originated a global financial crisis, a banking crisis and sovereign debt crisis. The recent crises have changed the way that banks and monetary policymakers work, especially when it refers to the grant of credit.

One of the most important functions of a bank in an economy (and the most significant source of income for a bank) it's their lending capacity and the crisis marked after the collapse of the bank Lehman Brothers putted it at risk and so the lending business had to be reevaluated from the Banks and monetary policymaker's perspective point of view with the ultimate goal to maintain price stability to reassure the effectiveness of monetary policy. The crises and all the economic, political and social issues that emerged from it raised several issues and questions on how banks will act in the future concerning lending restrictions and how to protect their volatility against Market anomalies/ discrepancies and captures the impact of the crisis on the role which bank characteristics play in the context of bank lending.

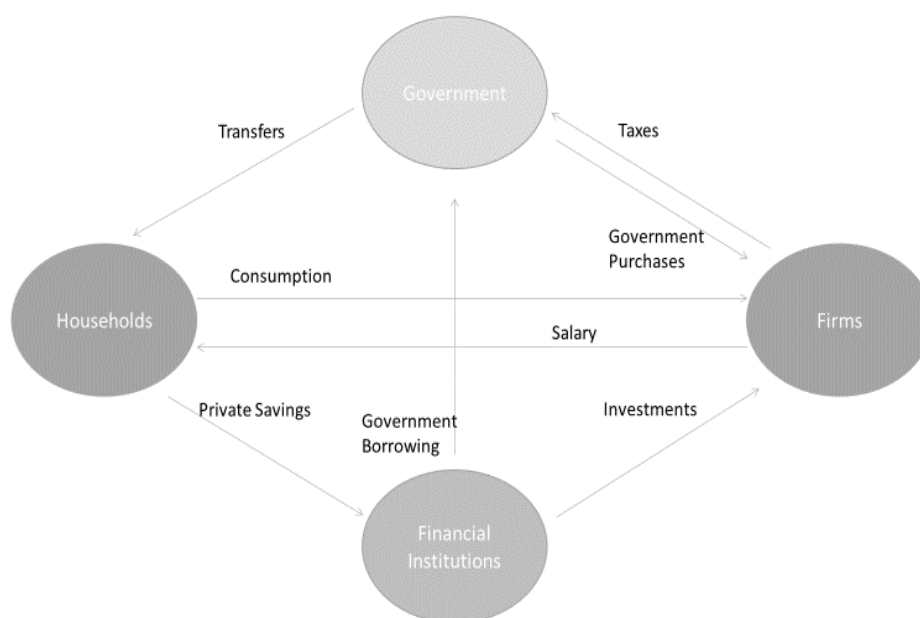


Figure 1- The Circular Flow of Income

Figure 1 illustrates the circular flow of income, which represent a macroeconomic model that try to explain how money is distributed within an economy.

The Transmission channel of monetary policy is the process through which monetary policy decisions affect the economy and the price level. A State should be able to achieve macroeconomics objectives with the control of inflation, consumption, growth and liquidity as it is related to borrowing, consumption and spending by individuals and private.

There are several transmission channels of monetary policy decisions such as change in official interest rates, that affects banks and money-market interest rates, expectations, the asset prices, savings and investment decisions, the supply credit that leads to a change in aggregate demand and prices, that affects the supply of bank loans. The interest-rate channel it's the one with the biggest impact as explains the effect of monetary policy on aggregate spending through changes in interest rates and assumes that the central bank can affect the short-term nominal interest rate given its monopoly power over the issuing of money and that investment and consumption expenditures are sensitive to changes in the real interest rate.

The bank lending channel suggests that banks play a special role in the transmission of monetary policy, this works by affecting banks' assets (loans) and banks' liabilities (deposits). The bank lending channel requires three conditions (Table 1) to be operational in the transmission of monetary policy (see, e.g., Bernanke and Blinder, 1988; and Kashyap and Stein 1994). The first one is that the central banks must be able to affect the supply of bank loans. Second, loans and bonds must not be perfect substitutes as a source for bank loans, describing firms' dependence on bank-intermediated loans, there two conditions distinguish the bank lending view from the money view. The third condition states that prices must not be adjusted instantaneously after monetary policy changes – money is not neutral.

	Condition 1	Condition 2	Condition 3
	Central bank must be able to affect supply scheme of bank loans	Publicly issued debt and non-bank intermediated loans must not be perfect substitutes for bank loans	Prices must not adjust instantaneously (monetary policy must not be neutral)
Explanation	Banking sector must not be able to or willing to completely insulate lending portfolio from monetary policy shocks, either by: <ul style="list-style-type: none"> - Switching from deposits to others forms of funding or - Selling securities (liquid assets) 	It must not be the case that firms are able to offset the decline in the supply of bank loans completely, i.e. without incurring additional cost, by borrowing more directly from household sector in public markets	Frictionless price adjustments would imply that policy rate changes immediately translate into price adjustments of an equal proportion and this must not be the case

Table 1 – Bank lending channel conditions

1.1. CREDIT CHANNEL THEORY

The transmission mechanism of monetary policy may be defined as the process by which asset prices and general economic conditions are affected because of monetary policy decisions. The modern financial system identified four channels of transmission of monetary policy: The Interest Rate Channel, the Asset Price Channel, the Exchange Rate Channel and the Credit Channel, which includes the Bank Lending Channel and the Balance Sheet Channel.

While the Bank Lending Channel focus on the importance of banks loans in the financial system, especially for certain borrowers that will not have access to the credit markets unless they borrow from banks (e.g. small firms and particulars), the Balance Sheet Channel operates through the balance-sheet positions of business firms, i.e. the loan borrower's capacity to obtain loans. Figure 2 shows the transmission mechanism of monetary policy through the Credit Channel Theory. The Rise in output and higher aggregate demand are due to banks' special role as lenders to classes of bank borrowers and the decrease in adverse selection and moral hazard problems, respectively.

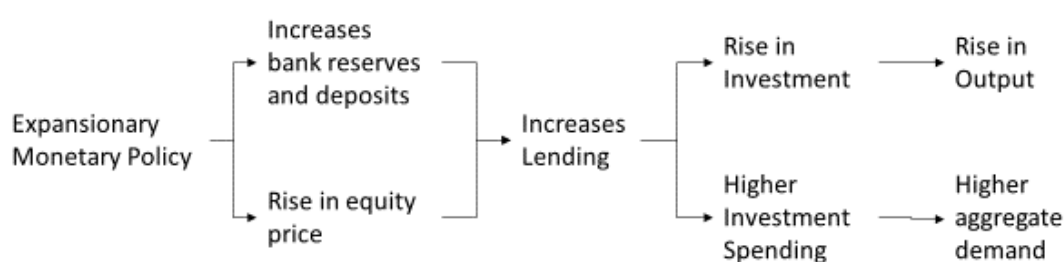


Figure 2- Transmission mechanism of monetary policy

1.2. THE PORTUGUESE ECONOMY

The subprime crisis was the Biggest European crisis since the Great Depression (1929-1930) and became the crisis of sovereign debts, giving rise to the Greek and Irish bailout in May and November of 2010, respectively, and in April 2011 in Portugal held by Troika (the European Union (EU), the European Central Bank (ECB) and the International Monetary Fund (IMF)) leaving Portugal under the Economic and Financial Assistance Programme (EFAP) until May 2014.

At the time of the crisis the Portuguese economic situation was already problematic due to the excessive consumption growth, lower investment and savings from households, problems of international competitiveness, a growing public indebtedness and high current account deficits were reflected in a low economic growth. All that led Portugal quite vulnerable to the high volatility in the financial markets, the increase of the spread of the Portuguese sovereign debt was

so big that Portuguese banks no longer had access to foreign credit. The bailout reflected in several austerity measures applied, labour market reforms and reduced spending on education, health and pensions for Portugal.

The international financial crisis has demonstrated the seriousness of the imbalances accumulated over the previous decades and the barrier they represent for the growth of the Portuguese economy advent of the new millennium. The high unemployment and public debt, low wages, budget deficits, unsustainability of Social Security and constraints imposed to business and households by high debt level helped to create a snowball effect of the economic growth stagnation since the beginning of the XXI century.

This stagnation period from 2001 to 2014 can then be divided in two periods. From 2001 to 2007, before the national crisis that reflects the low economic growth and between 2008 to 2014, reflecting the impact of the international financial crisis and the euro area sovereign debt crisis and the resulting adjustment period, having as result the fall in the GDP.

1.3. LITERATURE REVIEW

The study of the transmission of the monetary policy is crucial for an economy and its interest was renewed after the 2008 crisis, inquiring the effectiveness and the determinants of the transmission channels.

The operating of monetary transmissions channels differs across different countries/ economic groups due to differences in the level of development of capital markets, the central bank autonomy and the country's specific structural economic conditions. A quantitative approach can be a complement to historical event/data as it permits the measurement of the impact of monetary policy.

Jacobson et al. (2001) say that the two reasons behind the increase interest in empirical research of transmission mechanism of monetary policy was due to the deregulation of financial markets made monetary policy more oriented towards open markets operations than regulatory measures and that in many countries the emphasis in monetary policy has shifted towards explicit use of policy rules and monetary targeting.

The VAR model has received much attention as an instrument for modelling the monetary policy channels as it treats all linear relationships between variables as endogenous and the past values of these variables without imposing restrictions if they are dependent or independent, and, if necessary, it also allows exogenous variables on the model. furthermore, the VAR model allows to infer the effects from an impulse response function to one of the variables on all the other variables.

Several authors applied the VAR model in order to study the monetary policy channels: see for example, Canh (2016) and Lavally (2015), between others. ~

“Since the seminal work of Sims (1980), it has become a common practice to estimate the effects of the monetary policy on the real sector using vector autoregressions (VAR). This methodology avoids the problem of specifying the whole structural model of an economy and allows for the study of the dynamics of monetary policy shocks on the real economy. (...) The key aspect in applying the VAR methodology is the identification of the monetary policy shock.” (Aslandi, 2007).

This work aims to obtain impulse response functions that conform to the theoretical expectations, regarding the existence of the credit channel in the transmission of monetary disturbances, and are in line with the quantitative data previous obtained through the several tests.

2. MACROECONOMETRICS: CONCEPTS AND MODELS

2.1. TIME SERIES

A time series is a set of observations on the values of a variable timely ordered. A time series can refer to only one dependent or endogenous variable, if it refers to a univariate model, or to a set of observations if it is a multivariate model. The time series can be deterministic, when the output of the model is fully determined by the parameter values and the initial conditions or stochastic when randomness is present and variable states are not described by unique values, but rather by probability distributions. While linear regression requires a linear model and a linear equation has one basic form, a nonlinear equation can take many different forms. A relationship is spurious when two or more variables are associated but not causally related, this can be due to a third variable, known as the common response variable, or, it can just be a mere coincidence.

A time series it is called stationary if the mean, variance and covariance are all constant for each given time lag and do not show any trending behaviour (Figure 3), i.e., a stochastic process $\{X(t), t \in T\}$ it is second order stationary if, $\forall t \in T$, we have:

1. $E(X(t)) = \mu$
2. $Var(X(t)) = \sigma^2 < +\infty$
3. $Cov(X(t_1), X(t_2)) = \gamma(t_1, t_2) = \gamma(|t_2 - t_1|)$, $t_1, t_2 \in T$

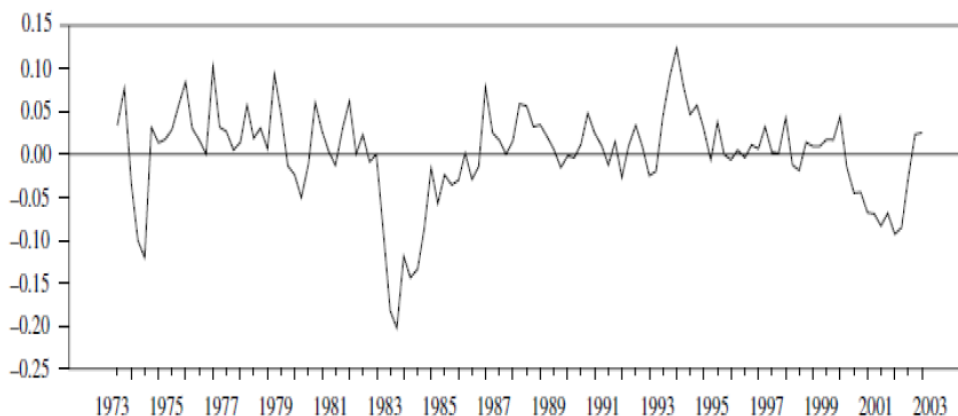


Figure 3 - Stationary time series (Juselius, 2006)

A non-stationary time series refers to unpredictable data that cannot be modelled or forecasted as the results may have a spurious correlation. The data can be non-stationary if the

mean increases over time (the series should not be a function of time); the variance change with the time (heteroscedasticity) and the covariance is not constant as the spread becomes closer as the time increases. A typical non-stationary time series (with linear trend and non-constant variance) can be observed in figure 4.

The non-stationarity tests are very important and it's essential that variables that are non-stationary be treated differently from those that are stationary as it can strongly influence its behaviour and properties and the use of non-stationary data can lead to spurious regressions. To have relevant results the non-stationary data needs to be transformed into stationary data, since the most of econometric/macroeconomic models are given for stationary data.

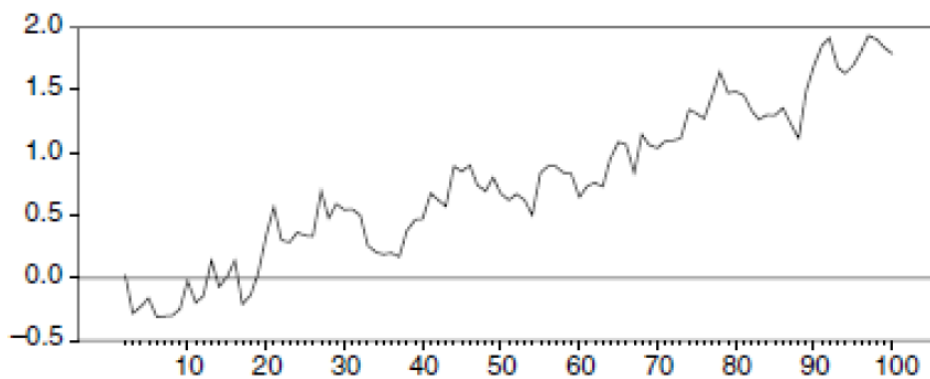


Figure 4 – Non-stationary series (Juselius, 2006)

Non-stationary behaviours can contain trends, cycles, random walks or combinations of the three (see Figure 5). Random walk is the simplest example of a non-stationary time series. It is defined as the process where the current value of a variable is composed of the past value plus an error term defined by white noise (that is, a stochastic variable with null mean, variance one and zero autocorrelations) and it implies that the best prediction of the next period is the current value.

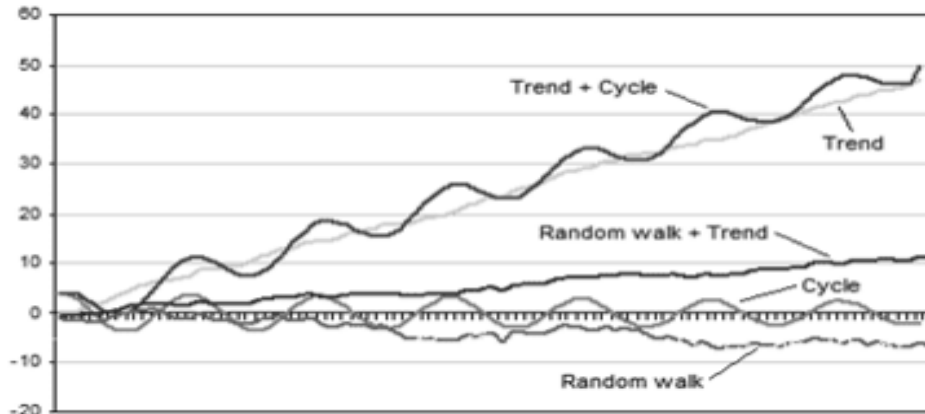


Figure 5 - Non stationary behaviour

The Random walk process it is also a well-known hypothesis about how financial prices move and can be formally stated as:

$$\gamma_t = \gamma_{t-1} + \varepsilon_t$$

where γ_t is the price observed at the beginning of time t and ε_t is the white noise error term. ε_t can be described as the price change, that is:

$$\varepsilon_t = \Delta\gamma_t = \gamma_t - \gamma_{t-1}$$

and is independent of past price changes. The accumulation of all past errors (below) can be written by successive backward substitution, highlighting that the price is indeed generated by the accumulation of purely random changes:

$$\gamma_t = \sum_{i=1}^t \varepsilon_t$$

The random walk is a difference stationary series since the first difference of γ_t is stationary:

$$\gamma_t - \gamma_{t-1} = (1 - L)\gamma_t = \varepsilon_t$$

We can deduce that the non-stationarity of a time-series generally can be induced by the trend (non-constant mean), and then we have a trend-stationary (or deterministic non-stationary) process or by the variance (and mean) and then we say that we have a stochastic non-stationary time series.

A deterministic non-stationary process can be transformed in a stationary one (or stabilized) by detrending the time series. In order to stabilize a stochastic non-stationary time series, we use the difference operator, that is

$$\Delta\gamma_t = \gamma_t - \gamma_{t-1}, \Delta^2\gamma_t = \gamma_t - \gamma_{t-2}, \dots$$

If the time series is non-stationary in levels $\{\gamma_t\}$ but turns to become stationary after using the difference operator, then we say that the time series it is integrated of order d , $I(d)$, where d is the order of integration.

The order of integration is also the number of unit roots contained in the series. For the random walk above, there is one-unit root, so it is an $I(1)$ series. Similarly, a stationary series is $I(0)$.

2.2. VAR MODEL

Vector Autoregressive model (VARs) were popularised by Sims (1980) in *Macroeconomics and Reality* as an extension of the univariate autoregression model to the analysis of multivariate time series data describing the dynamic interrelationship among stationary variables. It is a multi-equation system where all the variables are treated as dependent (endogenous) and has three purposes: forecasting economic time series; designing and evaluating economic models; evaluating the consequences of alternative policy actions. Vector autoregressive processes are quite popular in econometrics and it became a standard framework due to its flexibility and simple models for multivariate time series data being advocated as an alternative to large-scale simultaneous equations structural models.

The bivariate VAR is the simplest example of this Model, where there are only two variables, y_{1t} and y_{2t} . Each of whose current values is dependent on different combinations of the previous k values of both variables and error terms.

$$Y_{1t} = \beta_{10} + \beta_{11}y_{1t-1} + \dots + \beta_{1k}y_{1t-k} + \alpha_{11}y_{2t-1} + \dots + \alpha_{1k}y_{2t-k} + u_{1t},$$

$$Y_{2t} = \beta_{20} + \beta_{21}y_{1t-1} + \dots + \beta_{2k}y_{1t-k} + \alpha_{21}y_{2t-1} + \dots + \alpha_{2k}y_{2t-k} + u_{2t},$$

where u_{it} is a white noise disturbance term with $E(u_{it}) = 0$, ($i=1,2$), $E(u_{1t}u_{2t}) = 0$. The system can be expanded to include g variables, $y_{1t}, y_{2t}, y_{3t}, \dots, y_{gt}$, each of which has an equation.

There are two important assumptions that must be considered from the time series data to set up a VAR model: stationary (that can be tested through Unit Root Test) and the error normality and independence.

Steps to perform a VAR:

1. Test stationarity of data and degree of integration
2. Determination of lag length
3. Test the Granger causality
4. Estimation of VAR
5. Variance decomposition
6. Forecasting

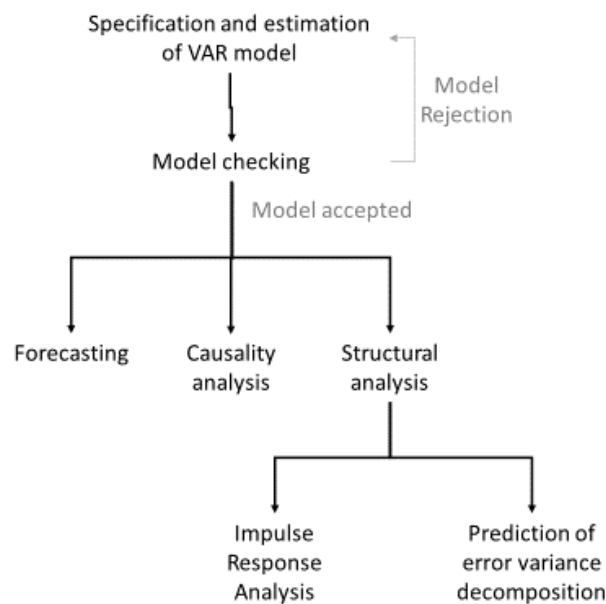


Figure 6- VAR Model (Lutkepohl, 2005)

Advantages of VAR modelling:

- Easy to estimate and good forecasting capabilities;
- There's no need to indicate which variables are endogenous or exogenous - it considers that all variables are endogenous. This is a very important point due to the constraints to identify certain variables as exogenous;
- Easy to test for Granger non-causality;
- It allows the value of a variable to depend on more than just its own lags or combinations of white noise terms, making VARs more flexible than the standard univariate AR models – implying that they may be able to capture more features of the data;
- Pre-determined variables include all exogenous variables and lagged values of the endogenous variables – it is possible to simply use OLS separately on each equation confirmed that there are no contemporaneous terms on the RHS of the equations;

Problems of VAR modelling:

- VARs are a-theoretical, since they use little economic theory information about the relationships between the variables to guide the specification of the model. Thus, VARs cannot be used to obtain economic policy prescriptions;
- Not clear the appropriate lag length for the VAR to be determined;

- A lot of parameters. If there are K equations, one for each K variables and p lags of each of the variables in each equation, $(K + pK^2)$ parameters will have to be estimated. For relatively small sample sizes, degrees of freedom will rapidly be used up, implying large standard errors and therefore wide confidence intervals for model coefficients.
- It is essential that all the components in the VAR are stationary, however many advocates of the VAR approach recommend that differencing to induce stationarity should not be done as will toss information on any long-run relationships between the series away.

There are two methods that are used to choose the optimal lag length: cross-equation restrictions that uses block F-test and information criteria that uses the likelihood ratio (LR).

2.3. VEC MODEL

In the case that the time series are not stationary the VECM (Vector Error Correction Model) should be used instead as allows consistent estimation of the relations among the series and can consider any cointegrating relations among the variables as it has the coefficient of the error correction term incorporated into the model.

Given a VAR(p) of $I(1)$: $x_t = \phi_1 x_{t-1} + \dots + \phi_p x_{t-p} + \epsilon_t$,

The Error correction representation form is:

$$\Delta x_t = \sum_{i=1}^{p-1} \phi_i \Delta x_{t-i} + \epsilon_t,$$

where $\phi_j = -\sum_{i=j+1}^p \phi_i$, $j=1, \dots, p-1$

and $\Pi = -(I - \phi_1 + \dots + \phi_p) = -\phi(1)$

Steps performs an VECM

1. Determination of lag length
2. Test the Granger causality
3. Cointegration degree test
4. Estimation of VECM
5. Variance decomposition

The error correction term becomes more difficult to interpret, as it is not obvious which variable it affects following a shock.

2.4. ADF, PP AND KPSS TESTS

The stationarity will be tested through the unit root tests, like Augmented Dickey-Fuller (ADF) and Phillips-Perron (PP), and stationarity test, Kwiatkowski-Phillips-Schmidt-Shin (KPSS). The ADF Test is one of the best known and frequently used unit root tests and it is based on the model of the first-order autoregressive process (Box, Jenkins, 1970), that is:

$$y_t = \phi_1 y_{t-1} + \varepsilon_t, t= 1, \dots, T$$

where ϕ_1 is the autoregression parameter, ε_t is the non-systematic component of the model that fits the characteristics of the white noise process.

The null hypothesis of the ADF and PP test is:

$$H_0: \phi_1 = 1$$

Which is expressed as an I(1), meaning that the process is non-stationary as it contains a unit root.

The alternative process is

$$H_1: |\phi_1| < 1,$$

and it's expressed as I(0), i.e., the process does not contain a unit root and it is stationary. The PP Test it's an improvement from ADF Test as it incorporates an automatic correction to allow for autocorrelated residuals, considering breaks structures and volatility. The two tests provide similar conclusions.

The KPSS Test shows if a series is stationary around a mean or linear trend or is non-stationary due to a unit root. The null hypothesis is

$$H_0: \phi_1 = 0$$

for the test is that the data is stationary and the alternate hypothesis for the test

$$H_1: |\phi_1| < 0$$

is that the data is not stationary. This test is a linear regression:

$$x_t = r_t + \beta_t t + \varepsilon_t,$$

breaking up the series into three parts: a deterministic trend (t), a random walk (r_t) and a stationary error (ε_t).

The use of stationarity and unit root tests are known as confirmatory data analysis. The null and alternative hypotheses under each testing approach are as follow (Brooks(2012)):

ADF/ PP	KPSS
$H_0: yt \sim I(1)$	$H_0: yt \sim I(0)$
$H_1: yt \sim I(0)$	$H_1: yt \sim I(1)$

Table 2 - ADF, PP and KPSS Test Hypothesis

There are four possible outcomes:

- a) Reject H_0 and Don't Reject H_0
- b) Don't Reject H_0 and Reject H_0
- c) Reject H_0 and Reject H_0
- d) Don't Reject H_0 and Don't Reject H_0

To have a relevant conclusion we should have outcome a) or b), which would be the case when both tests concluded that the series is stationary or non-stationary, respectively. Otherwise it would mean that there's a conflict in the results.

2.5. COINTEGRATION AND GRANGER CAUSALITY

We say that we are in the presence of cointegration if there is at least one stable, long-term, non-spurious relationship between a set of non-stationary time series. Cointegration considers the long-term properties (behaviour) of the model, not explicitly dealing with short-term dynamics. For this purpose, error correction models (ECM and VECM) have become very popular in the last decades. The dynamics part of the VECM describes the short-run effects and the cointegration relation describes the long-term relation between the non-stationary time series in the model.

The behaviour of cointegrated processes can be easily explained in the following way: treated individually, each process contains a unit root and has shocks with permanent impact. However, when combined with another series, a cointegrated pair will show a tendency to revert towards one another. Cointegration and error correction provide the tools to analyse temporary deviations from long-run equilibria.

Engle and Granger (1987) says that the components of a $(k \times 1)$ vector, Y_t , are cointegrated of order (d,c) , $Y \sim CI(d,c)$ if all Y elements are integrated of order d , $I(d)$ and if exists at least one non-trivial linear combination, z , of this variables, that's like $I(d - c)$, where $d \geq c > 0$, that is:

$$\beta'Y_t = Z_t \sim I(d - c),$$

where β is the cointegration vector and it's usually considered the case with $d = b = 1$. The cointegration level r it's the same as the number of linearly independent cointegration vectors. The cointegration vectors are the columns of the cointegration matrix β' such as:

$$\beta'Y_t = Z_t,$$

if all variables are $I(1)$ and $0 \leq r < k$. For $r = 0$ the elements of vector Y are non-cointegrated.

In this dissertation it will be considered the Engle-Granger and the Johansen cointegration methodologies, since they have been the most commonly used for cointegration analyses. The Ordinary Least Squares (OLS) estimation is used for the Engle-Granger method, while the VECM is estimated by the Maximum Likelihood Estimation (MLE) procedure.

The variables might be not cointegrated in the long-run, but still be related in the short-run – in order to understand short-run interdependence among the variables it will be performed the Granger causality tests. Each one of this topic will be briefly presented in what follows.

2.5.1. ENGLE-GRANGER TEST

The Engle-Granger test is a single-equation method used to determine whether there is a cointegrating relationship between two variables (Engle and Granger, 1987). Supposing that \hat{u}_t are the residuals of the estimated model, the hypotheses for the Engle-Granger test for cointegration are:

- H_0 : $\hat{u}_t \sim I(1)$ – Non-stationary residual and no cointegration between variables.
- H_1 : $\hat{u}_t \sim I(0)$ – Stationary residual and cointegration between variables

Steps to perform Engle-Granger Test:

1. Determine the order of integration of the two variables (based on Unit root tests).
2. If the variables are both integrated of order one, $I(1)$, cointegration is theoretically possible. If the variables have a different order of integration, it can be concluded that cointegration is not possible.
3. Estimate the long-run, static relationship (equilibrium) by running the OLS linear regression, given by the general equation: $Y_t = \beta x_t + u_t$, where Y_t and x_t are the times series in study.

-
4. Test the residuals of the regression for unit root. The variables are cointegrated when the null hypothesis (above) is rejected.
 5. If the variables are cointegrated, estimate an error-correction model.

The major's critics to this method are that it can only identify one cointegration vector at a time and the choice of the dependent variable may guide to different conclusions.

2.5.2. JOHANSEN TEST

This test is an improvement to the Engle-Granger test. The Johansen method relies on a vector autoregression (VAR) model. A VAR is a system regression model which includes more than one dependent variable. Every variable is regressed on a combination of its own lagged values and lagged values of other variables from the system. Here, the simplest form is presented, where k denotes the number of lags included (Brooks, 2008):

$$Y_t = \beta_1 y_{t-1} + \beta_2 y_{t-2} + \dots + \beta_k y_{t-k} + u_t,$$

where Y_t is a vector of variables and y_{t-k} is the lag of order k of the variable Y_t . The VAR model will be differentiated to be transformed into a VECM, that is:

$$\Delta y_t = \Pi y_{t-k} + \Gamma_1 + \Delta y_{t-1} + \Gamma_2 \Delta y_{t-2} + \dots + \Gamma_{k-1} \Delta y_{t-(k-1)} + u_t,$$

where $\Pi = \sum_{j=1}^k \beta_j - I_g$ and $\Gamma_i = \sum_{j=1}^i \beta_j - I_g$. Π is denoted the long-run coefficient matrix and is of type $(g \times g)$. We can decompose the matrix Π as the product $\alpha\beta'$ where $\beta(g \times r)$ contains the cointegrating vectors while $\alpha(g \times r)$ gives the "loadings" of each cointegrating vector in each equation. We denote by r the rank of matrix Π . Now

- (a) If $r = g$, then all-time series in Y_t are stationary (no cointegration)
- (b) If $r = 0$, then there is no long run relationship between the elements of Y_t (no cointegration)
- (c) If $0 < r < g$, then there are multiple cointegrating vectors

The Johansen cointegration test is based on the rank of the matrix Π evaluated via its eigenvalues (rank = number of nonzero eigenvalues). The eigenvalues of the long-run coefficients matrix are denoted by λ_i and are written in descending order, that is:

$$\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_g$$

If the variables Y_t are not cointegrated, then, the rank of matrix Π will not be significantly different from zero, so $\lambda_i = 0 \forall i$.

The test statistics for cointegration are formulated as

$$\lambda_{trace}(r) = -T \sum_{i=r+1}^g \ln(1 - \hat{\lambda}_i)$$

$$\lambda_{max}(r, r + 1) = -T \ln(1 - \hat{\lambda}_{r+1})$$

where $\hat{\lambda}_i$ is the estimated value for the i th ordered eigenvalue from the Π matrix. λ_{trace} tests the null that the number of cointegrating vectors is less than equal to r against an unspecified alternative. $\lambda_{trace} = 0$ when all the $\lambda_i = 0$, so it is a joint test.

λ_{max} tests the null that the number of cointegrating vectors is r against an alternative of $r+1$.

The hypotheses for the Johansen method are:

- H_0 : no cointegration against the alternative of cointegration.
- H_1 : cointegration against the alternative of cointegration.

It's very important to choose the optimal lag length, as the critical values of the method are quite sensitive to the same, and whether a constant term and time trend should be included, or not.

2.5.3. GRANGER CAUSALITY

“Granger causality is a statistical method for studying casual links between [2] random variables” (Granger, 1969), determining whether one time series is useful in forecasting another. The term causality means that there is a correlation between the current value of one variable and that's variable previous values. This test is based on a standard F-test and determinates if changes in one variable cause changes in another variable. If the previous values of X can predict the current value of Y, it's said that variable X “Granger cause” variable Y.

Using a VAR model as an example, that is:

$$Y_t = \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + \dots + \beta_k Y_{t-k} + \alpha_1 X_{t-1} + \alpha_2 X_{t-2} + \alpha_q X_{t-q} + u_t,$$

For this equation if all α – coefficients on lagged values of X are significant it means that “X Granger causes Y”. It's called unidirectional causality if X Granger causes Y and Y doesn't cause X, and bidirectional causality if X causes Y and vice versa (Brooks, 2008). The test statistic

follows a X^2 distribution, with p (the optimal number of lags) degrees of freedom under the null hypothesis.

The hypotheses for the Granger causality test are:

- $H_0: \alpha_1 = \alpha_2 = \dots = \alpha_p = 0$ (“X does not Granger cause Y”)
- H_1 : at least one of α – coefficients $\neq 0$ (“X does Granger cause Y”)

Granger Causality test can only show if two variables have significant impact on each other, it doesn't give any information on how long it will last. An impulse response analysis can give an answer to this.

2.5.4. IMPULSE RESPONSE FUNCTION

Impulse response analysis is widely used in econometric analyses, which uses vector autoregressive models. The Impulse Response Function (IRF) method is used to describe the evolution of a model's variables in reaction to a shock in one or more variables. The impulse responses (IR) are used to get a better understanding of the model's dynamic behaviour. The IRF for a linear VAR model is made through its moving average representation that is also the forecast error impulse response function, that can be mathematically obtained by:

$$\phi_i = \sum_{j=1}^i \phi_{i-1} A_j \quad i=1, 2, \dots$$

with $\phi_0 = I_K$ and $A_j = 0$ for $j > p$, where p is the lag order of the VAR model and K is the number of endogenous variables.

3. Data and Results

The present work consists of the econometric analysis of four time series that characterize the monetary policy in Portugal. The data it is comprised between the first quarter of 2003 and the last quarter of 2018, consists in 64 observations and was downloaded from the Portugal Central Bank site. We are going to apply VAR and VEC models in order to get the reaction of the variables to external shocks, by analysing the associated impulse response function. We are applying the EViews software in all the performed analysis. As it is usual in the Economic field the difference in the price series will be worked in logarithms instead of levels. It will be considered a level of significance of 5%.

Variables:

- **Gross Domestic Product (GDP)** for Constant Prices (in Millions) is the monetary value of all the goods and services produced within the geographic boundaries of a country during a specific period, normally one year. The GDP growth rate is an important indicator of the economic performance of a country (Time Serie: LogGDP).
- **EURIBOR** or the Euro Interbank Offer Rate is based on the interest rates at which a panel of European banks borrow short-term funds from one another, and it's communally used as benchmarked reference for bank loans. This Market interest rate is calculated daily by the European Banking Federation (EBF) and published by Reuters. The oscillation of the EURIBOR interest rates evolves accordingly the reference rate practiced by the ECB but this can be also influenced be others external factors, such as, the demand and supply variation, the economic growth and the inflation rate. It will be considered the 3 months EURIBOR rate (Time Serie: EURIBOR).
- **Inflation Rate:** "Inflation measured by consumer price index (CPI) is defined as the change in the prices of a basket of goods and services that are typically purchased by specific groups of households. Inflation is measured in terms of the annual growth rate and in index" OECD (Time Serie: CPI).
- **Households Consumer credit** or consumer debt (in Millions) is a debt that a person incurs when purchasing a service or good, being the credit card the most common form of consumer credit. We will analyse the loan supply and loan demand data as certain events impact on factors that influence both at the same and to better understand the supply-side or demand-side factors (Time Serie Log CC_total).

3.1 EMPIRICAL ANALYSIS

The first step in our analysis consist in the graphical representation of the 4 economic variables in consideration. From Figure 7 we observe that none of the variables are characterized by a global linear trend, instead of this, several increasing and decreasing patterns are present. The variance it is quite smooth, which is typical to quarterly data.

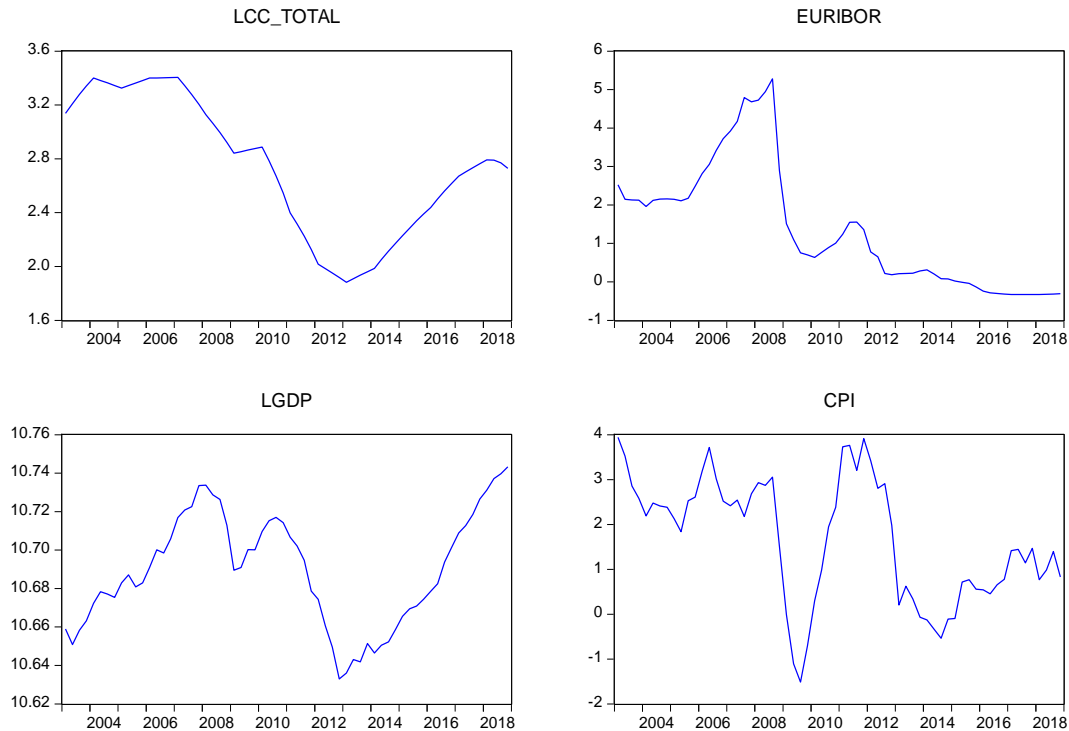


Figure 7 - Time Series logGDP, EURIBOR, CIP and logCC

The variable GDP doesn't show a clear linear trend, since there's a structural break in the last quarter of 2012 followed by a significant growing tendency period until the last quarter of 2018. The EURIBOR time series has an upright break from 2007 to 2008 followed by a decreasing trend which seems to stabilize in the last two years. The CPI time series also shows a break structure in the middle of 2009 and after that some more turbulent behaviour. The graphic of LCC variable it is given by a smooth curve, decreasing during the crises period and showing a recovery tendency beginning with 2014.

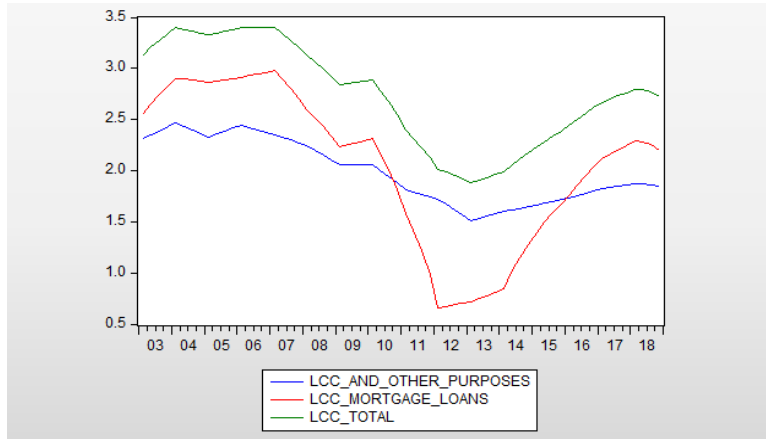


Figure 8 – Time series consumer credit

As it can be seen from Figure 8, the mortgage loans had a bigger variation and impact in the overall consumer credit during the studied period than the consumer credit and other purposes variables.

The next step it is the analysis of the descriptive statistics of the considered variables.

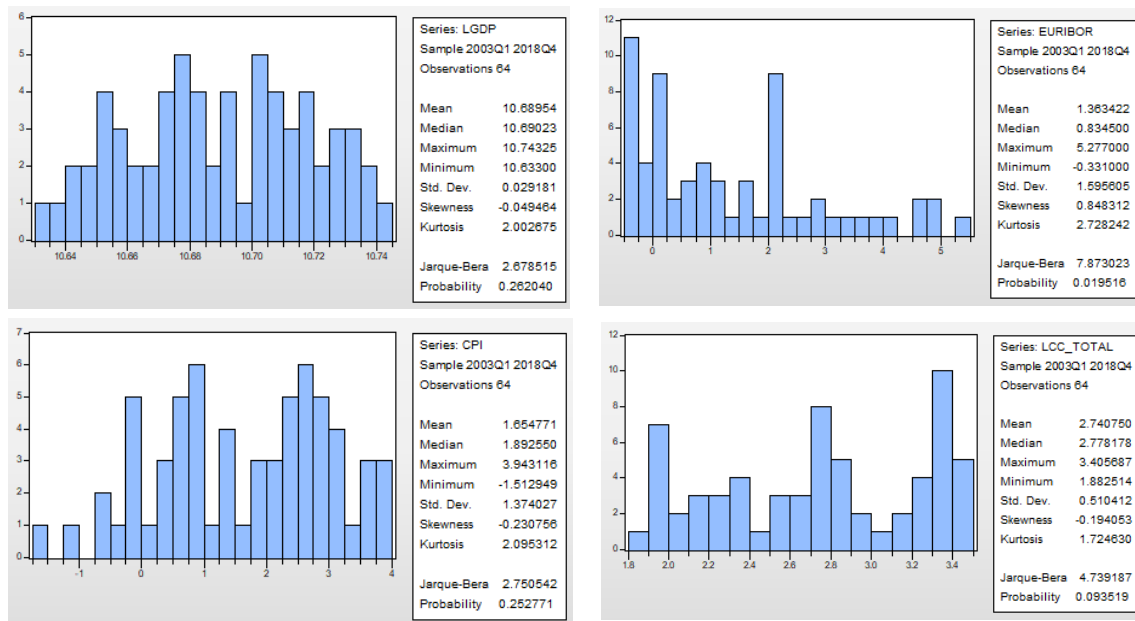


Figure 9 – Histograms of the Series logGDP, EURIBOR, CIP and logCC

We observe that GDP, CPI and CC are normally distributed since we do not reject the null hypothesis of Jarque-Bera. All variables have a platykurtic distribution and small negative skewness, except Euribor, that is moderate positive asymmetric.

As per Jarque-Bera test the variable EURIBOR doesn't follow a normal distribution for a level of significance of 5%, however the distribution is normal for a level of significance of 1% as H_0 is not rejected. As so, it will be considered that all variables are Normally distributed.

We have below the table of linear correlation coefficients between the considered variables. We can observe positive correlation between all variables, with the highest correlation between Euribor and Households Consumer credit (0.6673), followed by Euribor and CPI (0.5881).

	LCC_TOTAL	EURIBOR	LGDP	CPI
LCC_TOTAL	1.000000	0.667392	0.456590	0.383195
EURIBOR	0.667392	1.000000	0.293009	0.588140
LGDP	0.456590	0.293009	1.000000	0.149092
CPI	0.383195	0.588140	0.149092	1.000000

Table 3 – Linear correlation coefficients between variables

Figure 10 shows the Granger causality relation between the time series. It seems to exist several causality relationships between the variables, namely: Lcc_total Granger causes Euribor (for a confidence level of 10%), Lcc_total Granger causes lgdp, Cpi Granger causes Lcc_total, Euribor Granger causes lgdp (for a confidence level of 10%), Euribor Granger causes cpi and Lgdp Granger causes cpi. We observe that GDP and Consumer Credit are the only two variables characterized by a bidirectional Granger causality. We also observe that highly correlated variables are also Granger causal, in this case.

Pairwise Granger Causality Tests

Date: 07/22/19 Time: 22:07

Sample: 2003Q1 2018Q4

Lags: 2

Null Hypothesis:	Obs	F-Statistic	Prob.
EURIBOR does not Granger Cause LCC_TOTAL	62	0.90191	0.4115
LCC_TOTAL does not Granger Cause EURIBOR		2.90085	0.0631
LGDP does not Granger Cause LCC_TOTAL	62	3.88552	0.0262
LCC_TOTAL does not Granger Cause LGDP		8.80795	0.0005
CPI does not Granger Cause LCC_TOTAL	62	3.48921	0.0372
LCC_TOTAL does not Granger Cause CPI		1.69301	0.1931
LGDP does not Granger Cause EURIBOR	62	0.75173	0.4762
EURIBOR does not Granger Cause LGDP		2.63029	0.0808
CPI does not Granger Cause EURIBOR	62	0.10984	0.8962
EURIBOR does not Granger Cause CPI		4.14544	0.0209
CPI does not Granger Cause LGDP	62	1.89877	0.1591
LGDP does not Granger Cause CPI		3.82383	0.0276

Figure 10 – Granger Causality Test

We conclude that exists a short time relationship between the variables, given by the causality effect between each other. In practice, when we establish Granger causality (or not), policy prescriptions might be suggested in order to encourage (or not) the provision of credit.

It will now be tested the stationarity of the series through the Unit Root Tests ADF and PP and the stationary test KPSS. The variables are considered in levels, with Intercept and maximum lags number equal to 4. The results for the three Tests can be find below, in Table 4:

	ADF	PP	KPSS
LGDP	0.4989	0.6383	0.117859*
EURIBOR	0.5756	0.6338	0.723321
CPI	0.0771	0.0964	0.471588
LCC_TOTAL	0.2350	0.6988	0.623313

Table 4 – Results for ADF, PP and KPSS Tests

*H₀ is Rejected with a confidence level $\alpha = 5\%$

For ADF and PP Tests as p-value is bigger than 0.05, H₀ is not rejected and as so the series have a unit root and in consequence are non-stationary. For KPSS Test, for a confidence level of 5% all series are non-stationary, and the null hypothesis is rejected, since the test statistics it is lower than the critical values.

Since all the time series are non-stationary we have to apply the first difference operator and study the returns for the four series.



Figure 11 - Graphics of the first differences of the Series logGDP, EURIBOR, CIP and logCC

From Figure 11 we can observe that the mean is constant, but the variance increases. A negative “outlier” it is observed for the first difference of EURIBOR in mid 2008. Steepest decreasing values are present also for the growth rate of GDP and CPI in mid of 2008.

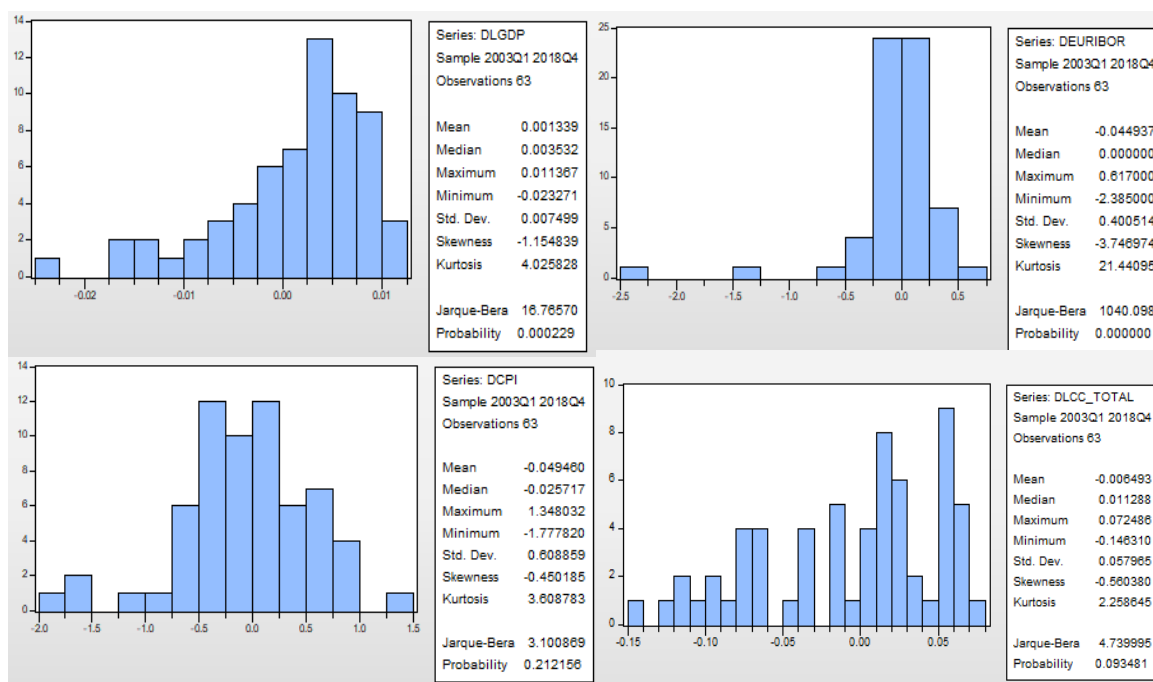


Figure 12 - Histograms of the first differences of the Series logGDP, EURIBOR, CIP and logCC

Figure 12 shows the histograms and the basic statistics of the first difference of the considered variables. CPI and LCC are normally distributed with zero mean, based on the Jarque-Bera test. The GDP is negatively asymmetric and leptokurtic. Finally, the EURIBOR it is also skewed to the right and with a very high kurtosis coefficient. An outlier can be observed.

	ADF	PP	KPSS
LGDP	0.0000	0.0000	0.166573
EURIBOR	0.0000	0.0000	0.070910
CPI	0.0000	0.0000	0.049785
LCC_TOTAL	0.0301	0.0244	0.225301

Table 5 – Unit Root Test for the variables

For the Unit Root Tests ADF and PP, the P-value is smaller than 0.05, H_0 is rejected and so the series don't have unit roots and they are all stationary. For KPSS Test, for a confidence level of 5% all series are stationary, and the null hypothesis is not rejected. We conclude than, that all variables are integrated of order 1, I(1).

In what follows we will study if the time series are cointegrated, or not, using the two methodologies defined by Engle-Granger and by Johansen.

We recall that Engle-Granger methods requires to analyse if the linear combination between two non-stationary variables (that is, the linear regression) produce a stationary time series (that is, the residuals). The output of all the simple linear regression models between the pairs of variables and the unit root test for the associated residuals are presented in Appendix C. Table 6 is the sum of these regressions, showing the p-value of the ADF unit root test applied to the residuals.

lcc_total c cpi	0.4980
lcc_total c euribor	0.2625
lcc_total c lgdp	0.4019
cpi c euribor	0.0072
cpi c lgdp	0.0870
euribor c lgdp	0.7753

Table 6 – Linear regression between variables

It seems that there is a cointegration relationship between the variables *cpi* and *Euribor* as the p-value is smaller than 5% for the residuals unit root test. For the remaining variables, since the p-value is bigger than the test critical values (for all confidence levels) the null hypothesis of unit root is not rejected and so the residuals are non-stationary meaning that there is no additional cointegration relationship between the studied variables.

This statement will be confirmed (or not) by running in EViews the Johansen Trace Test, which is shown in Table 7:

Hypothesized No. of CE(s)	Eigenvalue	Trace Statistic	0.05 Critical Value	Prob.**
None*	0.450527	60.09028	47.85613	0.0024
At most 1	0.235960	24.76135	29.79707	0.1701
At most 2	0.139211	8.882386	15.49471	0.3764
At most 3	0.000643	0.037962	3.841466	0.8455

Trace test indicates 1 cointegration eqn(s) at the 0.05 level

* denotes rejection of the hypothesis at the 0.05 level

** MacKinnon-Haug-Michelis (199) p-values

Table 7 – Johansen Trace Test

At the 5% significance value, the trace test concluded in favour of one cointegration relation among the four variables, that is, there exist only one relationship which drive the long-run behaviour of the system.

Now, since there is one cointegration relationship between the variables, we are going to use a VECM instead of a VAR analyses. The VECM will identify long-run and short-run dynamics of the banking lending. First, we will test for the optimal lag number, which is two in our case, based on the information criteria of Schwartz (see Appendix D). Next the model VECM(4,2) will be estimated by the Maximum Likelihood method and the residuals are checked for independence (Figure 13), homoscedasticity (Figure 14) and normality.

From the VECM output (Appendix D), we can observe the short-run behaviour, that is, about 1% of disequilibrium it is corrected each quarter by changes in the consumer credit. In the same way, 9%, 0.5% and 34% of disequilibrium will be corrected each quarter by changes in the Euribor, GDP and CPI variables, respectively. The coefficients of the error correction term of Consumer Credit, Euribor and GDP variables are almost all insignificant, but the coefficient of CPI are significant. These means that if a disturbance occurs in the system, then, the change of CPI variable will have significant conservative force tending to bring the model back into the equilibrium state when it is going around.

VEC Residual Portmanteau Tests for Autocorrelations
 Null Hypothesis: No residual autocorrelations up to lag h
 Date: 09/01/19 Time: 20:13
 Sample: 2003Q1 2018Q4
 Included observations: 61

Lags	Q-Stat	Prob.*	Adj Q-Stat	Prob.*	df
1	0.768944	---	0.781760	---	---
2	11.09346	---	11.45626	---	---
3	27.44556	0.4941	28.65416	0.4302	28
4	45.84515	0.3955	48.34494	0.3018	44

*Test is valid only for lags larger than the VAR lag order.
 df is degrees of freedom for (approximate) chi-square distribution
 after adjustment for VEC estimation (Bruggemann, et al.
 2005)

Figure 13 – VEC Residual Portmanteau Test for Autocorrelations

From Figure 13 we can see that the residuals are independent up to lag 2, based on the Portmanteau test. We check this by observing the p-values, which are higher than 0.05, and so, we do not reject the null of no residual autocorrelation

Figure 14 illustrates another residual test, namely the heteroscedasticity test. The null hypothesis is: residual variance is constant (or homoscedastic), which it is not rejected, since the p-value is higher than 0.05.

VEC Residual Heteroskedasticity Tests (Levels and Squares)
 Date: 09/01/19 Time: 20:15
 Sample: 2003Q1 2018Q4
 Included observations: 61

Joint test:					
Chi-sq	df	Prob.			
207.9042	180	0.0756			

Individual components:					
Dependent	R-squared	F(18,42)	Prob.	Chi-sq(18)	Prob.
res1*res1	0.275721	0.888260	0.5944	16.81896	0.5356
res2*res2	0.200555	0.585356	0.8901	12.23383	0.8349
res3*res3	0.412854	1.640690	0.0933	25.18407	0.1199
res4*res4	0.177050	0.501995	0.9423	10.80005	0.9026
res2*res1	0.501877	2.350919	0.0114	30.61450	0.0319
res3*res1	0.396522	1.533142	0.1264	24.18783	0.1490
res3*res2	0.174265	0.492431	0.9471	10.63014	0.9094
res4*res1	0.348736	1.249442	0.2692	21.27288	0.2659
res4*res2	0.201738	0.589682	0.8869	12.30599	0.8310
res4*res3	0.215158	0.639664	0.8467	13.12464	0.7841

Figure 14 – VEC Residual Heteroskedasticity Test (Levels and Squares)

The normality assumption cannot be attained because of the outlier present in the Euribor time series. Figure 15 illustrates the residuals of all variables. We can include a dummy variable in order to vanish the outlier, but this way we will improve artificially the model, and, however, the statistical outlier it is not a numerical error, it is a true economical phenomenon.

VEC Residuals

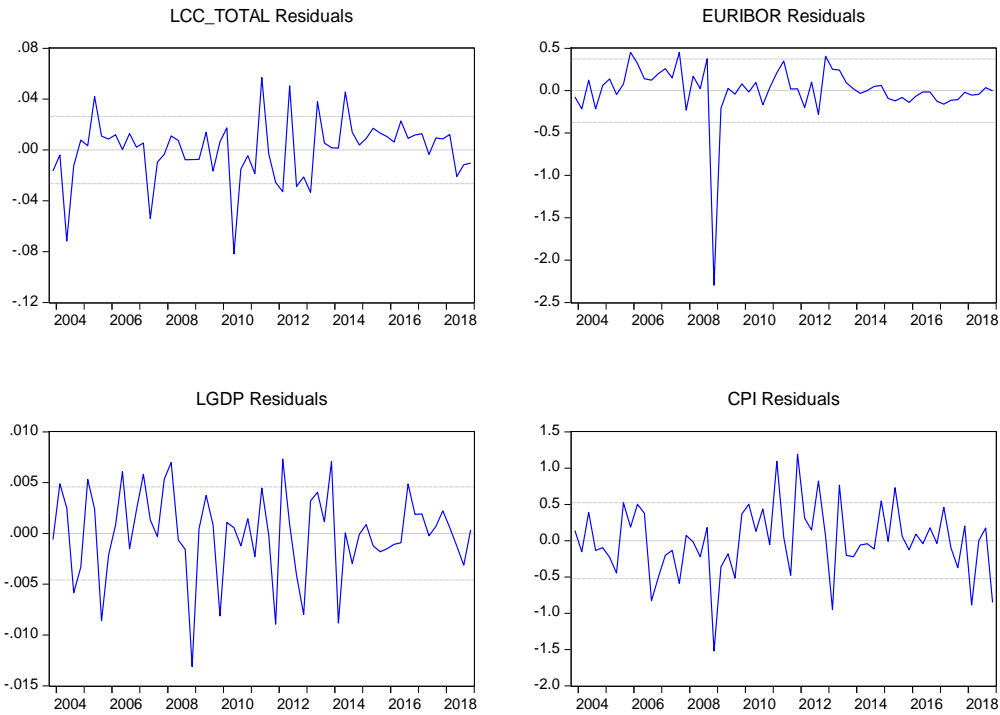


Figure 15 – VEC Residuals

The cointegration relation between CPI and Euribor it is shown in Table 8. The cointegrating vector represents the positive relationship existing in the long-run between the 3-months nominal interest rate and consumer price inflation and the negative relationship with GDP.

This cointegration vector is a Fisher-type equation (that is, defines the one-for-one adjustment of the nominal interest rate to the expected inflation rate). In the euro area institutional framework this vector can be interpreted as a monetary policy reaction function, i.e., a Taylor rule describing the behaviour of the European Central Bank that sets the interest rate with the only objective of stabilizing the rate of consumer price inflation around a given target.

Normalized cointegrating coefficients (standard error in parentheses)

LCC_TOTAL	EURIBOR	LGDP	CPI
1.000000	-0.090580	4.343800	-0.527891
	(0.06871)	(3.83756)	(0.09302)

Table 8 – Normalized cointegration coefficients

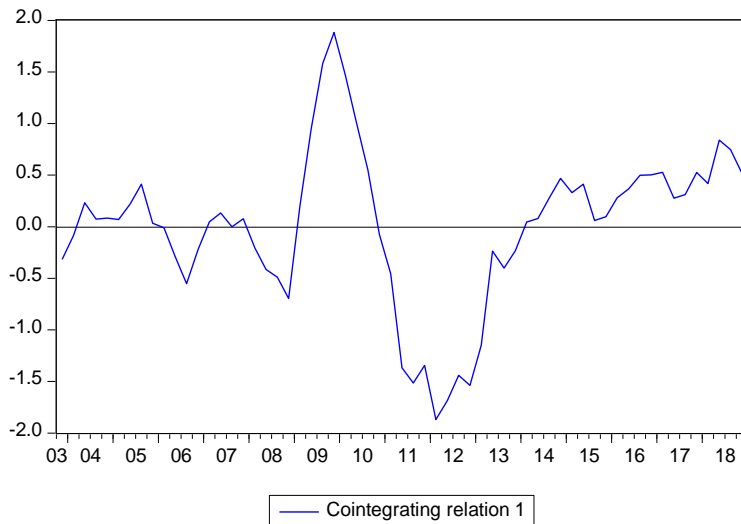


Figure 16 – Cointegration relation

Once we validated the VECM(4,2) we can proceed to the impulse response function analysis to test the effect of perturbations on the variables.

First, we will give one standard deviation shock to the Euribor time series (Figure 17). The responses of GDP time series to the one standard deviation shock on Euribor is reflected by a short-term 0.3% quick increase, followed by a decreasing tendency and finally the turn back to the equilibrium after around three years. The CPI inclines in response to tightened Interest Rate conditions. The effect of Euribor restrictions on CPI reaches a peak after around one year and fades away after around three years.

The response of the Consumer Credit time series to the one standard deviation shock on Euribor it is more volatile. The first reaction observed it is the increase of the consumption credit, with more-less a quarter duration, which can be viewed as the normal reaction to novelty. After a short period of time, the consumer credit will decrease, about 2%, that is, a cautionary reaction of the consumer, and after, will slowly recover, taking around 10 quarters to get back to the stationary level. This confirms the existence of the relationship between interest rates and consumption. Usually, Central banks try to keep the interest rate below some threshold value and this way believes in the increase of the household consumption.

Response to Nonfactorized One S.D. Innovations ± 2 S.E.

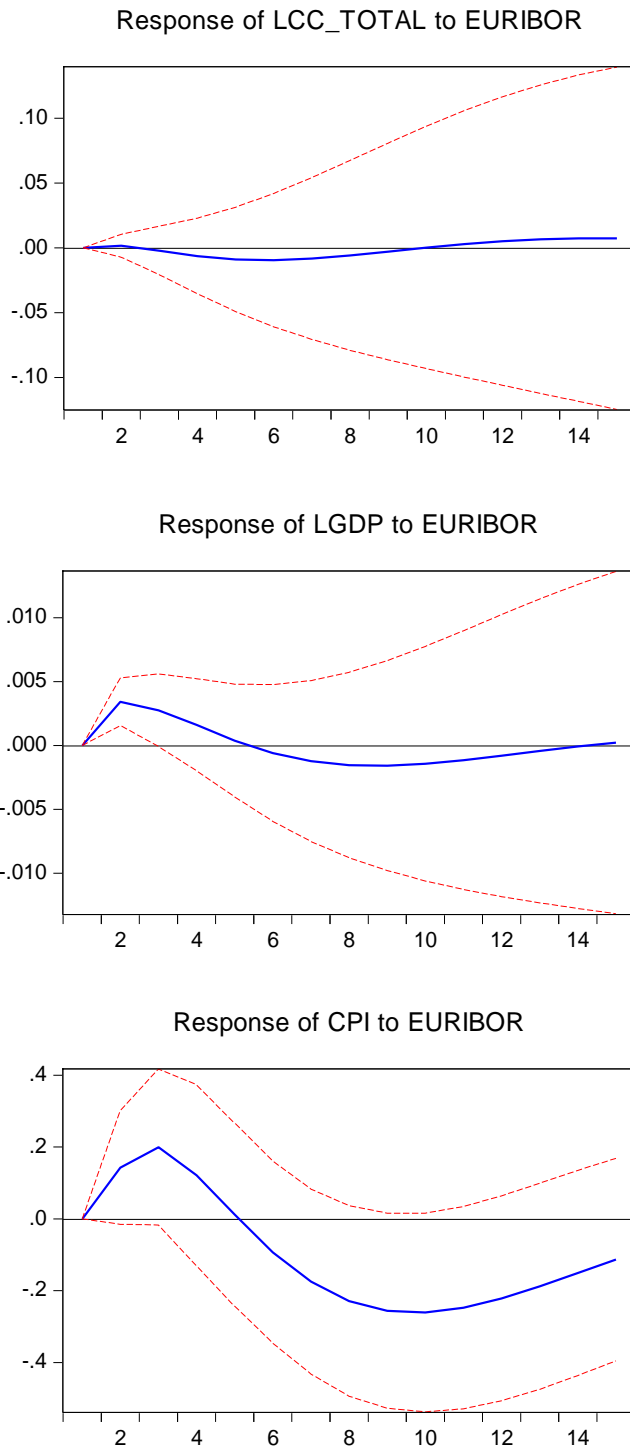


Figure 17 – Impulse Response Function EURIBOR

It will also be applied one standard deviation shock to the Consumption Credit time series. Figure 18 shows that the three-time series behave similarly, with moderate shock variation and they all take around 2 years to get back to equilibrium. The CPI and the Euribor variables initially

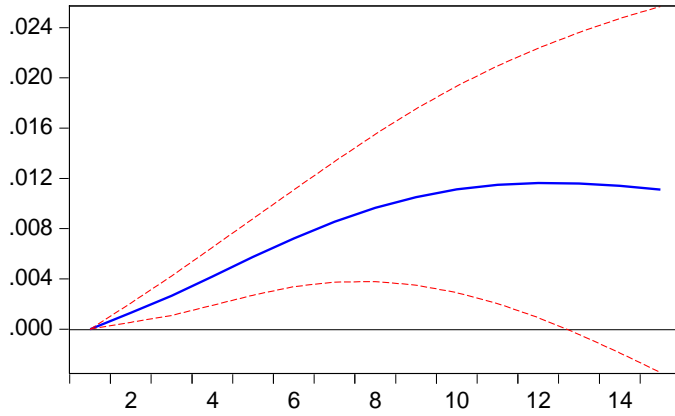
decrease some percentage points as consequence to the shock in the Consumer Credit, that is, a statistically significant reaction can be observed in the model. The one standard deviation shock to Consumption Credit causes the most significant decrease in the CPI time series (around 10%) for a period of 4 quarters after which the effect dissipates and an increasing tendency will be dominant in the next quarters. The maximum impact of the innovation in CC is experienced at quarter 3 and 2 for CPI and Euribor variables, respectively.

These are important pieces of information about the relationships between the time series in the VAR/VECM model. The GDP reaction it is to increase, attaining the maximum value, that is, about 1% at quarter 12, after which it will decrease. This reflects that the impact of consumer credit on output growth is clearly positive in short run. Recall also the bidirectional Granger causality and the high correlation coefficient between these two economic variables, reflecting the contemporary and short-run relation between them.

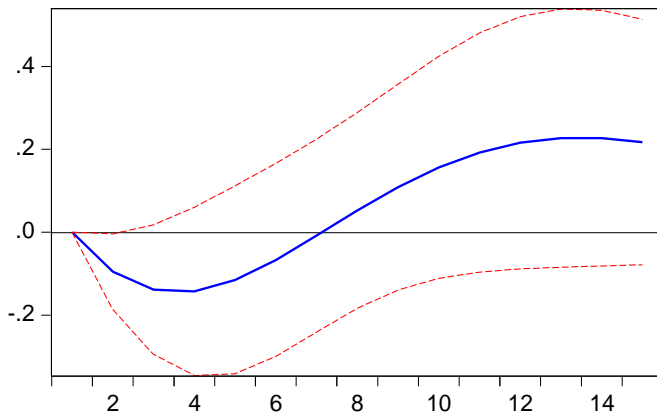
This way, from the analysis of the impulse response function, we can account for the relation between the credit and the business cycle given by the macroeconomic variables and to conclude that the credit it is important in explaining output fluctuations.

Response to Nonfactorized One S.D. Innovations ± 2 S.E.

Response of LGDP to LCC_TOTAL



Response of CPI to LCC_TOTAL



Response of EURIBOR to LCC_TOTAL

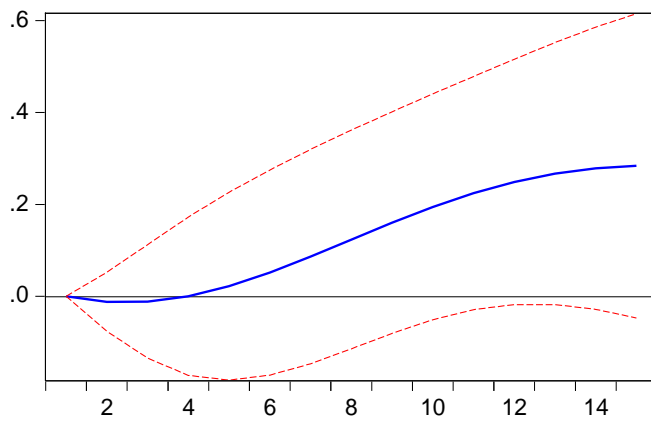


Figure 18 – Impulse Response Function LCC_TOTAL

CONCLUSION

This study focused on the credit channel theory in order to determine the effectiveness of transmissions mechanisms of monetary policy in Portugal during the last 16 years. To achieve this, the following variables were studied: Euro Interbank Offer Rate (EURIBOR), Consumer Price Index (CPI), Gross Domestic Price (GDP) and Households Consumer Credit, or consumer credit.

Looking to the graphic representation of the variables, the effects of the crisis is quite notable, even though, noticing in different periods/ ways for different variables. The consumer credit to households started to decrease in 2007, having an abrupt contraction until the end of 2008. This was due to the monetary policy barrier imposed, not for a declining in the demand. Ten years after and the consumer credit in Portugal is still below of the values before the crisis. The Euribor rate started to decrease after the crisis (more significantly in 2009) reaching, a never seen before, negative values in 2015, this was an unconventional monetary policy used to mitigate the financial crisis effects. The impact of the crisis in the GDP was first seen in 2008, however the lowest value of the same was in 2012, when the impact of the crisis already made itself felt in the Portuguese Economy and this reflects the status of the Portuguese Economy in the period followed by the crisis. The Index Price to Consumer had a tremendous decrease in the middle of 2009, followed by a turbulent period since 2013.

All the series are non-stationary while testing the stationarity of the same in levels (contains a unit root), however all variables are integrated of order 1, $I(1)$. A Vector Error Correction (VEC) model was used as there was one cointegration relationship between the variables Euribor and CPI.

All the variables are correlated and there were several causality relationships between the variables. It was studied the Granger causality and the conclusion was that GDP and Consumer Credit are the only two variables characterized by a bidirectional Granger causality and they are also the variables that have the higher correlation coefficient. There is a short time relationship between all the variables, given the causality effect between each other. The Johansen test confirmed that there is only one cointegration relation between variables.

From the Impulse response function, it was intended to verify how the endogenous variables respond to exogenous shocks effects applied to the Euribor and consumer credit variables. This way, we can account for the relation between the credit and the business cycle given by the macroeconomic variables and to conclude that the credit it is important in explaining output fluctuations.

In conclusion, it is important to mention that there are some points that can be explored in the continuation of this dissertation that would add more value to the same, as the analysis of the same methodology but for other countries within the Eurozone. This would enable to crosscheck the results with the Portuguese reality and analyse the impact of the variables in different countries. Moreover the separation of the consumer credit in demand and supply can also give more insight to the monetary policy and bank lending channels in the Portuguese economy.

REFERENCES

Aslandi, O., (2007), The optimal monetary policy and the channels of monetary transmission mechanism in CIS-7 countries: the case of Georgia, *Charles University*

Brinkmeyer, H., (2014), Drivers of Bank Lending; New Evidence from the crisis, *Springer Gabler*

Brockwell Peter J. and Davis, Richard (2002), Introduction to time series analysis and forecasting, *Springer*, N. York

Brooks, C., (2008), Introductory Econometrics for Finance, 2nd ed., *Cambridge University Press*.

Canh, N., (2016), *Monetary Policy Transmission and banks lending channel in Vietnam*. PHD Thesis's, University of Economics Ho Chi Minh City

Dickey, D. A., Fuller, W. A., (1979), Distribution of the estimators for autoregressive time series with a unit root, *Journal of the American Statistical Association* 74, 427-431

Engle, R. F., Granger, C. W. J., (1987), Co-integration and error correction: Representation, estimation and testing, *Econometrica* 55, 251-276.

Granger, C., (1969), Investigating causal relations by econometric models and cross-spectral methods, *Econometrica*, Vol. 37, No. 3, 424–438

Jacobson T, Jansson, P., Vredin A., and Warne A. (2001), A VAR Model for Monetary Policy Analysis in a small open Economy, *Journal of Applied Econometrics*, pages 487-520.

Johansen, S. (1992), Cointegration in Partial Systems and the Efficiency of Single Equation Analysis, *Journal of Econometrics*,

Juselius, K., (2007), The Cointegrated VAR model: Methodology and Applications, *Oxford Univ Press*.

Lavally, M., (2015), *Investigating the effectiveness of transmission mechanisms of monetary policy in Sierra Leone*. Master's Thesis, The University of Namibia

Lutkepohl, H., (2005). New Introduction to Multiple Time Series Analysis (2nd edn.).*Springer-Verlag: Berlin*.

Mills, T.C., and Markellos, R.N., (2008), *The Econometric Modelling of Financial Time Series*, Cambridge University Press.

Moreira, B., (2011) *Modelização de empréstimos bancários de empresas não financeiras na zona euro: uma abordagem VAR/VECM*. Master's Thesis, ISCTE University

Phillips, P. C., (1987), Time series regression with a unit root, *Econometrica* 55:277–301.

Pordata (2019), Statistics Database, Web Site:

<https://www.pordata.pt/Tema/Portugal/Macroeconomia-11>

Sims, C.A., (1972), Money, Income and Causality, *American Economic Review* 62, 540–552.

Sims, C. A. (1980). Macroeconomics and reality. “*Econometrica*” 48(1), 1–48

Sousa, J., (2017) *Breve ensaio sobre a cointegração dos mercados financeiros europeus: caso de Portugal, Espanha, França e Alemanha*. Master's Thesis, ISCTE University

Vestmann, A. and Viebrock, J., (2018) *The Influence of Credit Growth on Output Growth in Iceland: A VEC Model Approach*. Master's Thesis, Lund University

APPENDIX A

ADF, PP AND KPSS TESTS TO THE VARIABLES IN LEVELS

Null Hypothesis: LGDP has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-1.555905	0.4989
Test critical values: 1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*MacKinnon (1996) one-sided p-values.

Table 9 – Unit Root Test ADF of the variable LGDP in level

Null Hypothesis: LGDP has a unit root
 Exogenous: Constant
 Bandwidth: 5 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-1.270197	0.6383
Test critical values: 1% level	-3.538362	
5% level	-2.908420	
10% level	-2.591799	

*MacKinnon (1996) one-sided p-values.

Table 10 - Unit Root Test PP of the variable LGDP in level

Null Hypothesis: LGDP is stationary
 Exogenous: Constant
 Bandwidth: 6 (Newey-West automatic) using Bartlett kernel

	LM-Stat.
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.117859
Asymptotic critical values*: 1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 11 - Stationarity Test KPSS of the variable LGDP in level

Null Hypothesis: EURIBOR has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-1.402380	0.5756
Test critical values:		
1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*Mackinnon (1996) one-sided p-values.

Table 12 - Unit Root Test ADF of the variable EURIBOR in level

Null Hypothesis: EURIBOR has a unit root
 Exogenous: Constant
 Bandwidth: 4 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-1.279855	0.6338
Test critical values:		
1% level	-3.538362	
5% level	-2.908420	
10% level	-2.591799	

*Mackinnon (1996) one-sided p-values.

Table 13 - Unit Root Test PP of the variable EURIBOR in level

Null Hypothesis: EURIBOR is stationary
 Exogenous: Constant
 Bandwidth: 6 (Newey-West automatic) using Bartlett kernel

	LM-Stat.
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.723321
Asymptotic critical values*:	
1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 14 - Stationarity Test KPSS of the variable EURIBOR in level

Null Hypothesis: CPI has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-2.715835	0.0771
Test critical values:		
1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*Mackinnon (1996) one-sided p-values.

Table 15 - Unit Root Test ADF of the variable CPI in level

Null Hypothesis: CPI has a unit root
 Exogenous: Constant
 Bandwidth: 4 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-2.609756	0.0964
Test critical values:		
1% level	-3.538362	
5% level	-2.908420	
10% level	-2.591799	

*Mackinnon (1996) one-sided p-values.

Table 16 - Unit Root Test PP of the variable CPI in level

Null Hypothesis: CPI is stationary
 Exogenous: Constant
 Bandwidth: 5 (Newey-West automatic) using Bartlett kernel

	LM-Stat.
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.471588
Asymptotic critical values*:	
1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 17 - Stationarity Test KPSS of the variable CPI in level

Null Hypothesis: LCC_TOTAL has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-2.127194	0.2350
Test critical values:		
1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*MacKinnon (1996) one-sided p-values.

Table 18 – Unit Root Test ADF of the variable LCC_TOTAL in level

Null Hypothesis: LCC_TOTAL has a unit root
 Exogenous: Constant
 Bandwidth: 6 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-1.130045	0.6988
Test critical values:		
1% level	-3.538362	
5% level	-2.908420	
10% level	-2.591799	

*MacKinnon (1996) one-sided p-values.

Table 19 – Unit Root Test PP of the variable LCC_TOTAL in level

Null Hypothesis: LCC_TOTAL is stationary
 Exogenous: Constant
 Bandwidth: 6 (Newey-West automatic) using Bartlett kernel

	LM-Stat.
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.623313
Asymptotic critical values*:	
1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 20 – Stationarity Test KPSS of the variable LCC_TOTAL in level

APPENDIX B

ADF, PP AND KPSS TESTS TO THE VARIABLES – FIRST DIFFERENCES

Null Hypothesis: D(LGDP) has a unit root
 Exogenous: None
 Lag Length: 0 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-4.673449	0.0000
Test critical values:		
1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 21– Unit Root Test ADF of the variable LGDP – first differences

Null Hypothesis: D(LGDP) has a unit root
 Exogenous: None
 Bandwidth: 4 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-4.870870	0.0000
Test critical values:		
1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 22– Unit Root Test PP of the variable LGDP – first differences

Null Hypothesis: D(LGDP) is stationary
 Exogenous: Constant
 Bandwidth: 5 (Newey-West automatic) using Bartlett kernel

	LM-Stat.
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.166573
Asymptotic critical values*:	
1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 23– Stationarity Test KPSS of the variable LGDP – first differences

Null Hypothesis: D(EURIBOR) has a unit root
 Exogenous: None
 Lag Length: 0 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-4.985431	0.0000
Test critical values:		
1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 24– Unit Root Test ADF of the variable EURIBOR – first differences

Null Hypothesis: D(EURIBOR) has a unit root
 Exogenous: None
 Bandwidth: 0 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-4.985431	0.0000
Test critical values:		
1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 25– Unit Root Test PP of the variable EURIBOR – first differences

Null Hypothesis: D(EURIBOR) is stationary
 Exogenous: Constant
 Bandwidth: 3 (Newey-West automatic) using Bartlett kernel

	LM-Stat.
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.070910
Asymptotic critical values*:	
1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 26– Stationarity Test KPSS of the variable EURIBOR – first differences

Null Hypothesis: D(CPI) has a unit root
 Exogenous: None
 Lag Length: 0 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-5.540433	0.0000
Test critical values: 1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 27– Unit Root Test ADF of the variable CPI – first differences

Null Hypothesis: D(CPI) has a unit root
 Exogenous: None
 Bandwidth: 4 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-5.563568	0.0000
Test critical values: 1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 28– Unit Root Test PP of the variable CPI – first differences

Null Hypothesis: D(CPI) is stationary
 Exogenous: Constant
 Bandwidth: 4 (Newey-West automatic) using Bartlett kernel

	LM-Stat
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.049785
Asymptotic critical values*: 1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 29– Stationarity Test KPSS of the variable CPI – first differences

Null Hypothesis: D(LCC_TOTAL) has a unit root
 Exogenous: None
 Lag Length: 0 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-2.167513	0.0301
Test critical values:		
1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 30- Unit Root Test ADF of the variable LCC_TOTAL – first differences

Null Hypothesis: D(LCC_TOTAL) has a unit root
 Exogenous: None
 Bandwidth: 2 (Newey-West automatic) using Bartlett kernel

	Adj. t-Stat	Prob.*
Phillips-Perron test statistic	-2.255122	0.0244
Test critical values:		
1% level	-2.602794	
5% level	-1.946161	
10% level	-1.613398	

*MacKinnon (1996) one-sided p-values.

Table 31 – Unit Root Test PP of the variable LCC_TOTAL – first differences

Null Hypothesis: D(LCC_TOTAL) is stationary
 Exogenous: Constant
 Bandwidth: 6 (Newey-West automatic) using Bartlett kernel

	LM-Stat.
Kwiatkowski-Phillips-Schmidt-Shin test statistic	0.225301
Asymptotic critical values*:	
1% level	0.739000
5% level	0.463000
10% level	0.347000

*Kwiatkowski-Phillips-Schmidt-Shin (1992, Table 1)

Table 32- Stationarity Test KPSS of the variable LCC_TOTAL – first differences

APPENDIX C

ENGLE-GRANGER CORRELATION TEST

Null Hypothesis: R1 has a unit root
 Exogenous: Constant
 Lag Length: 4 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-1.557017	0.4980
Test critical values: 1% level	-3.546099	
5% level	-2.911730	
10% level	-2.593551	

*MacKinnon (1996) one-sided p-values.

Table 33 – R1: lcc_total c cpi

Null Hypothesis: R2 has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-2.056944	0.2625
Test critical values: 1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*MacKinnon (1996) one-sided p-values.

Table 34 – R2: lcc_total c euribor

Null Hypothesis: R3 has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-1.749262	0.4019
Test critical values: 1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*MacKinnon (1996) one-sided p-values.

Table 35 – R3: cpi c lgdp

Null Hypothesis: R4 has a unit root
 Exogenous: Constant
 Lag Length: 3 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-3.663439	0.0072
Test critical values: 1% level	-3.544063	
5% level	-2.910860	
10% level	-2.593090	

*Mackinnon (1996) one-sided p-values.

Table 26 – R4: cpi c euribor

Null Hypothesis: R5 has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-2.659078	0.0870
Test critical values: 1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*Mackinnon (1996) one-sided p-values.

Tabela 37 – R5: cpi c lgdp

Null Hypothesis: R6 has a unit root
 Exogenous: Constant
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-0.920617	0.7753
Test critical values: 1% level	-3.540198	
5% level	-2.909206	
10% level	-2.592215	

*Mackinnon (1996) one-sided p-values.

Table 38 – R6: Euribor c lgdp

APPENDIX D

VAR/VECM

VAR Lag Order Selection Criteria
 Endogenous variables: LCC_TOTAL EURIBOR LGDP CPI
 Exogenous variables: C
 Date: 07/23/19 Time: 08:28
 Sample: 2003Q1 2018Q4
 Included observations: 54

Lag	LogL	LR	FPE	AIC	SC	HQ
0	-74.80656	NA	0.000218	2.918762	3.066094	2.975582
1	245.6575	581.5829	2.76e-09	-8.357684	-7.621023	-8.073583
2	297.0257	85.61379	7.53e-10	-9.667620	-8.341631*	-9.156238
3	308.9630	18.12692	8.99e-10	-9.517147	-7.601829	-8.778484
4	334.7061	35.27760*	6.59e-10	-9.878003	-7.373357	-8.912059
5	342.9889	10.12337	9.54e-10	-9.592180	-6.498204	-8.398955
6	357.5067	15.59325	1.15e-09	-9.537285	-5.853982	-8.116779
7	385.0206	25.47581	9.15e-10	-9.963725	-5.691093	-8.315939
8	408.4448	18.21885	9.32e-10	-10.23870	-5.376736	-8.363629
9	447.2013	24.40221	6.18e-10	-11.08153	-5.630239	-8.979180
10	498.4932	24.69612	3.21e-10*	-12.38864*	-6.348019	-10.05901*

* indicates lag order selected by the criterion
 LR: sequential modified LR test statistic (each test at 5% level)
 FPE: Final prediction error
 AIC: Akaike information criterion
 SC: Schwarz information criterion
 HQ: Hannan-Quinn information criterion

Table 39 – Test Lags information criteria of Schwartz

Vector Error Correction Estimates
 Date: 09/01/19 Time: 20:12
 Sample (adjusted): 2003Q4 2018Q4
 Included observations: 61 after adjustments
 Standard errors in () & t-statistics in []

Cointegrating Eq:	CointEq1
LCC_TOTAL(-1)	1.000000
EURIBOR(-1)	-0.090580 (0.06871) [-1.31835]
LGDP(-1)	4.343800 (3.83756) [1.13192]
CPI(-1)	-0.527891 (0.09302) [-5.67526]

C	-48.19324			
Error Correction:	D(LCC_TOTA L)	D(EURIBOR)	D(LGDP)	D(CPI)
CointEq1	-0.011116 (0.00796) [-1.39584]	-0.091929 (0.11250) [-0.81714]	0.005010 (0.00138) [3.63667]	0.343699 (0.15775) [2.17874]
D(LCC_TOTAL(-1))	0.775072 (0.13378) [5.79366]	-0.695448 (1.88995) [-0.36797]	0.015326 (0.02314) [0.66228]	-0.583962 (2.65012) [-0.22035]
D(LCC_TOTAL(-2))	0.150520 (0.14222) [1.05839]	0.577219 (2.00915) [0.28730]	0.038385 (0.02460) [1.56031]	-2.302246 (2.81725) [-0.81720]
D(EURIBOR(-1))	0.002433 (0.01122) [0.21685]	0.315429 (0.15853) [1.98973]	0.011234 (0.00194) [5.78765]	0.411302 (0.22229) [1.85029]
D(EURIBOR(-2))	-0.026146 (0.01419) [-1.84202]	-0.345204 (0.20053) [-1.72148]	-0.001444 (0.00246) [-0.58812]	0.023109 (0.28118) [0.08218]
D(LGDP(-1))	-0.124879 (0.85713) [-0.14569]	17.10374 (12.1090) [1.41248]	-0.147844 (0.14827) [-0.99714]	17.36323 (16.9794) [1.02260]
D(LGDP(-2))	0.097586 (0.71962) [0.13561]	12.19128 (10.1664) [1.19918]	-0.117190 (0.12448) [-0.94142]	6.084382 (14.2554) [0.42681]
D(CPI(-1))	-0.010257 (0.00715) [-1.43496]	-0.015061 (0.10098) [-0.14914]	-0.001017 (0.00124) [-0.82232]	0.109004 (0.14160) [0.76979]
D(CPI(-2))	-0.005905 (0.00680) [-0.86834]	0.082752 (0.09608) [0.86130]	3.03E-05 (0.00118) [0.02574]	0.077749 (0.13472) [0.57711]
C	-0.004262 (0.00433) [-0.98518]	-0.082087 (0.06112) [-1.34300]	0.002440 (0.00075) [3.26004]	-0.058394 (0.08571) [-0.68132]
R-squared	0.817897	0.274882	0.681898	0.375364
Adj. R-squared	0.785761	0.146920	0.625763	0.265134
Sum sq. resids	0.035730	7.131096	0.001069	14.02118
S.E. equation	0.026469	0.373932	0.004579	0.524333
F-statistic	25.45124	2.148152	12.14734	3.405280
Log likelihood	140.4453	-21.08978	247.4738	-41.71095
Akaike AIC	-4.276896	1.019337	-7.786025	1.695441
Schwarz SC	-3.930851	1.365382	-7.439980	2.041486
Mean dependent	-0.009002	-0.039951	0.001392	-0.033238
S.D. dependent	0.057185	0.404854	0.007484	0.611650
Determinant resid covariance (dof adj.)		4.19E-10		
Determinant resid covariance		2.05E-10		
Log likelihood		334.1933		
Akaike information criterion		-9.514535		
Schwarz criterion		-7.991938		
Number of coefficients		44		

Tabela 40 - VECM