

WHAT DRIVES CRYPTOCURRENCY VALUE? A VOLATILITY AND PREDICTABILITY ANALYSIS.

Master's Thesis of Economic and Corporate Decision-Making

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Abstract

This thesis describes how digital currencies have rose as a new interesting phenomenon in the financial markets and how the most popular of the digital currencies – BitCoin – have risen crucial questions about their exchange rates and also represents a field to study the dynamics of this market, which is strongly connected with speculative traders with no fundamentals as there is no fundamental value to the currency. Using a $GARCH(1, 1)$ model on daily data and focusing on two emerging phenomena of recent years – digital currencies, particularly Bitcoin, and web content provided by search queries on Google Trends and Wikipedia and tweets from Twitter– we discover that Bitcoin returns are driven primarily by its popularity. Thus, we analyze their relationship, the existence of volatility clustering and demonstrate that the web content and Bitcoin prices are connected and they exhibit some predictable power.

KEYWORDS: Bitcoin, GARCH, Cryptocurrencies, Google Trends, Wikipedia, Twitter

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1: Introduction

In a period of constant technological evolution, the way that we process payments changed considerably. Just by clicking, tapping or swiping, we can now complete a transaction. Processing electronic payments has seen its costs reduce significantly. The electronic banking and digital wallets grant individuals the capacity to transfer funds securely and the dissemination of smartphones has made it easier to make and receive payments in person with the e-banking features. Moreover, the development of inexpensive card-reading equipment has enabled basically anyone to comply with electronic payments.

Simultaneously, some of the most widely used currencies are under some pressure with some questions about their safety and stability. Successive rounds of quantitative easing in the United States or the instability in Europe cause fears of devaluation for both dollar and euro. Despite the recognition of its influence and the fact that many people continue to put their trust in dollars and euros, uncertainty thrives.

Under these conditions, some turned to cryptocurrencies, a possible digital substitute to conventional government-issued paper money. Cryptography intends to ensure that transactions are made in a safe and secure way, preventing users from spending the same balance more than once, and controlling the supply of digital notes in circulation. Because some cryptocurrencies can be decentralized, they allow the so-called anonymous transactions and complicates regulation by governments. Additionally, the use of cryptocurrencies across international borders is facilitated by its electronic essence.

The leading digital currency is Bitcoin, but others have emerged in the same time span, namely LiteCoin, DogeCoin and Ethereum.

Bitcoin is a decentralized digital currency that allows instant payments to anyone, anywhere in the world that has a Bitcoin account. Its biggest strength is that all transactions and validations are carried out collectively by the network, using a technology called Blockchain, that keeps a public ledger of all Bitcoin transactions. The “network” manages the transactions and money creation, by using peer-to-peer technology, to run

without central authority.

With its fast growth, Bitcoin attracted a growing interest by economists. Its price increased from zero value at the time of its inception in 2009 to around \$1100 at the end of 2013. The factors that affect Bitcoin price are studied in this thesis.

Quite recently, search queries provided by Google Trends and Wikipedia, or the public feeling extracted from tweets have proved to be a useful source of information in financial applications. We use them as a proxy to capture Bitcoin's attractiveness for investors, mainly: the volume of daily Bitcoin page views on english Wikipedia; the Google Trends data from search term "Bitcoin"; and the weighted score (bullish or bearish) of tweets referring Bitcoin hashtag. With these three components, we intend to measure investors' faith in Bitcoin. This will prove to be important given the fact that Bitcoin doesn't have any fundamental value.

How it reacts to news and what factors affect its ups and downs. By conducting our statistical tests, we will be able to assess, if there is a relationship between the price volatility of Bitcoin and the listed variables.

One of the properties of the volatility of financial assets is volatility clustering. That implies that volatility is not constant over time, a property that is easy to spot in Bitcoin price data. Periods of high volatility are usually followed by periods of similar high volatility. We will use the model developed by Bollerslev (1986) the General Autoregressive Conditional Heteroscedasticity (GARCH) on our daily data. This model takes into account the characteristics of series using the past errors in estimates. We can evaluate volatility clustering (the sum of ARCH and GARCH effects), the reaction to shocks and the explanatory power of our independent variables.

This thesis objective is to analyze the main drivers of Bitcoin price formation by evaluating four sets of determinants: supply-demand fundamentals; attractiveness; macroeconomics; and technicals (explained below). Whereas the main focus of our econometric models is the relationship between investors' interest in Bitcoin and how to proxy it, the attractiveness variables will be considered as more meaningful and therefore more relevant for us.

- supply-demand fundamentals like the amount of units in circulation and thus its scarcity on the market. The demand of Bitcoin is mainly determined by transac-

tion demand as a medium of exchange, Estimated output volume, Trade volume vs. transaction volume ratio. And a proxy for the network effects could be the unique Bitcoin addresses in the network or the number of transactions per day.

- attractiveness for investors that is driven also by investors' speculative behavior measuring Bitcoin wikipedia page views, google searches for the word Bitcoin and twitter sentiment analysis over Bitcoin
- macroeconomics indicators like Gold price
- technicals that provide a measure of system productivity mainly Hash Rate, which is reflected in the system Difficulty and the Average Transaction Block

Above all we will try to evaluate the impact of events on the price of Bitcoin and try to demonstrate if that price of Bitcoin can be predictable.

This thesis is divided into the following chapters:

Chapter 2 describes the problem that we want to study, chapter 3 reviews the literature, chapter 4 describes the data, chapter 5 describes the model used, chapter 6 describes the empirical results and Chapter 7 summarizes and concludes.

2: Cryptocurrencies and Bitcoin

2.1 *What are Cryptocurrencies?*

A computer currency whose implementation is based on the principles of cryptography¹, used both to certify the transactions and the production of new currency. To assure the protection of sellers from fraud, cryptocurrencies will typically use a proof-of-work scheme, recording all transactions in a public ledger. To prevent the inflation phenomena, that usually happens to fiat² currencies like Dollar and Euro, that don't have any fundamental value as well, and their value is not backed by a physical commodity but their value comes from government regulation or law, most cryptocurrencies are designed to have a ceiling on the total amount of currency in circulation, to gradually introduce new money.

Among several digital currencies, Bitcoin became the most notable, either in terms of a remarkable market capitalisation or on the price development.

Usually, by the interaction of supply and demand on the market, currencies are priced. Macroeconomic variables such as GDP, interest rates, inflation, unemployment, and others will drive the price. Considering that digital currencies don't have any macroeconomic fundamentals, the supply function is either fixed (if there is a ceiling) or it develops based on some publicly known algorithm, which is the case of the Bitcoin market. The expectation of profits of holding the currency and selling it later guide the demand side of the market (as there are no interest rates on digital currencies you cannot profit from holding the currency). Speculators, trend chasers, short-term investors and noise traders dominate the market and considering that there are no fundamen-

¹<http://sowmyabj.wix.com/msritcns2015#!> - Cryptography is the practice and study of techniques for secure communication in the presence of third parties (called adversaries). More generally, it is about constructing and analyzing protocols that block adversaries; various aspects in information security such as data confidentiality, data integrity, authentication, and non-repudiation are central to modern cryptography.

²https://en.wikipedia.org/wiki/Fiat_money - Fiat money is currency which derives its value from government regulation or law. It differs from commodity money. Commodity money is created from a good, often a precious metal such as gold or silver, which has uses other than as a medium of exchange (such a good is called a commodity)

tals, either for analysis or for setting a “fair” price, the strong belief of investors’ on perpetual growth becomes the main driver for the digital currency price. It is for this reason crucial to measure or proxy investors’ sentiment.

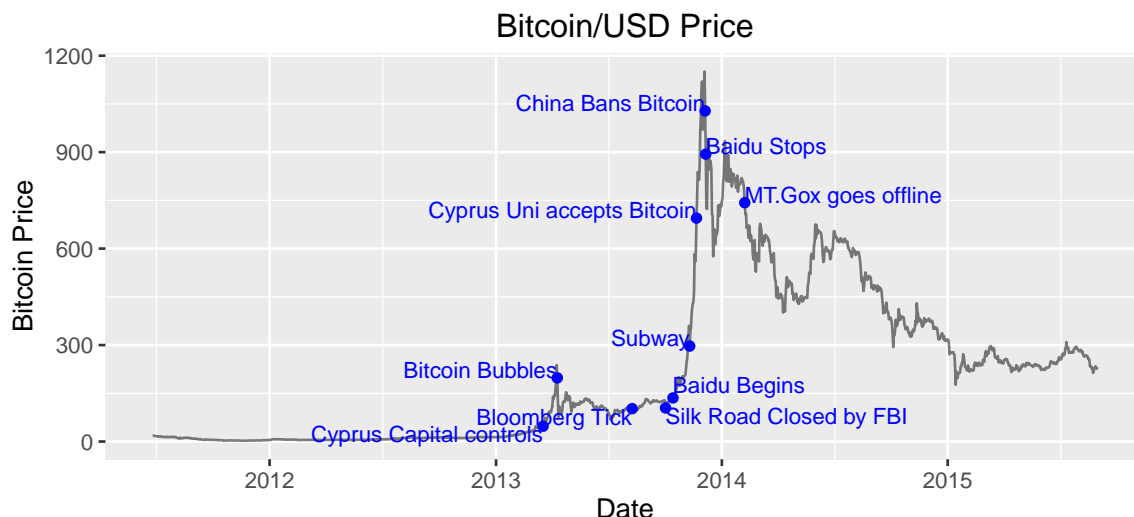


Figure 2.1: Bitcoin Price

2.2 What is Bitcoin?

Bitcoin is a digital currency that was created in 2009 by an anonymous person using the alias Satoshi Nakamoto. A decentralized system that allows transactions without a middle men – that is, no banks! No transaction fees (or extremely cheap) and no need to give your real name – only the wallet IDs, keeping the transactions private and anonymous, however, the Bitcoin network logs and validates every single transaction that ever happened in the network in a huge version of a general ledger, called the blockchain. More and more merchants are beginning to accept them. With no transaction fees, the international payments are easy and cheap since bitcoins are not bound to any country or subject to any regulation. Some people just use them because there are no credit card fees and others just buys bitcoins as an investment, expecting that their Bitcoin portfolio will increase in value. You can buy or sell Bitcoins in a “bitcoin exchanges” marketplace or you may try to “mine” Bitcoins using computers to solve complex math problems, the Bitcoin network allows that approximately every 10 minutes, the winner is rewarded with 25 bitcoins (up to November 2012 the reward was 50), the reward for solving a block is automatically adjusted so that: every four years

the reward for a mined block gets halved; the difficulty (adjusted every 2016 blocks) to solve the block allows one block each 10 minutes. Therefore, money supply occurs by solving problems and computing power limits supply in the long run as the amount of processing power directed at mining changes to adjust to the existing difficulty.

2.3 *What gives Bitcoins value?*

Bitcoin has shown several peaks and successive ups and downs since its inception in 2009, and since then the opinions from investors are still inconclusive. Speculative trap or a safe haven? Long-run promise or a short-term hedge? These questions are frequent and demonstrates the upmost importance of this phenomenon. We know that without any fundamental value the Bitcoin's price structure is suggests a highly sensitivity to investor sentiment, and a given set of events will likely lead to fluctuation in the Bitcoin price. As was displayed in Figure 2.1, the Bitcoin price exhibits very high volatility and historical prices do not reveal any specific pattern. We can conceive that specific events may contribute to the volatility of the Bitcoin price. The events chosen in table 2.1 are some of the most important for Bitcoin³.

Event	Description
Cyprus	Capital controls imposed and the financial crisis on Cyprus in of March 2013, is claimed to have increased interest for bitcoin as an alternative to the standard monetary system.
Silk Road	This American website was a known market place for illegal products such as drugs. In the beginning of October 2013 it was however shut down by the FBI.
Baidu	This Chinese competitor to Google announced in the middle of October 2013 that it would accept payments in Bitcoin
USA	The chairman of Federal Reserve, Ben Bernanke, said in an open letter to the Homeland Security in the middle of November 2013 that bitcoin "may hold long-term promise".
China	The Chinese government declared in the beginning of December 2013 that banks and payment companies are forbidden to deal with bitcoin.
MtGox	The largest bitcoin exchange, MtGox, declares bankruptcy in the end of February 2014, after being hacked and losing a great deal of investors' money .

Table 2.1: Important events for Bitcoin.

The impact of network effects is relevant as well, the Bitcoin value may be related to the amount of people using it and accept it as a form of payment, the more people start using Bitcoin, the more likely merchants will accept it (network effects won't be part of

³<http://historyofbitcoin.org/>

our model).

2.4 Is Bitcoin predictable?

The ability to predict the stock market has attracted much attention for some decades. But is it really possible to predict the stock market? The Efficient Market Hypothesis (EMH) and random walk theory were relevant for stock market prediction and according to the EMH stock market prices are generally driven by new information, i.e. news, and not to present and past prices. Like it was referred by Qian and Rasheed (2007), because news are unpredictable, the fluctuations of the stock market will reflect a random walk pattern and cannot be predicted with more than 50% accuracy. Since Bitcoin price market doesn't have any fundamentals the above theories of efficient markets and random walk will act as guidance to inspect Bitcoin predictability.

Besides news unpredictability, recent research also suggests that very premature indicators can be derived from online social media (blogs, Twitter feeds, RSS, Google, etc.) to predict changes in various economic and commercial indicators.

This thesis aims to estimate the predictable capabilities of social media sources like Google (Figure A.1), Wikipedia (Figure A.2) and Twitter (Figure A.3) on Bitcoin price and therefore if these sources are incorporated immediately into prices. Can we have a privileged position in the market by predicting the price in advance? We know that one of the attributes of efficient markets is that at any given time, the prices on the market already incorporate all available information and adjust quickly to reflect new information, therefore it shouldn't be possible to outperform the market by using the same information that is already known to all investors, except through luck.

The theory of efficient markets states that investors decide rationally. However, decision making can be irrational according to the behavioral finance, investors can be influenced by many factors. Malkiel (2003) states that new information spreads quickly and is instantaneously incorporated into prices this ensures that neither technical⁴ nor fundamental⁵ analysis can be used to predict future prices. Thus, without accepting

⁴Technical analysis uses past patterns of price and the volume of trading as the basis for predicting future prices. The random-walk evidence suggests that prices of securities are affected by news. Favourable news will push up the price and vice versa. It is therefore appropriate to question the value of technical analysis as a means of choosing security investments.

⁵Fundamental analysis involves using market information to determine the intrinsic value of securities

above-average risks, investors cannot earn above-average returns. Nevertheless, even though the release of new information is the cause of price changes, the no-arbitrage⁶ condition ensures that this new information cannot be used to infer predictable future returns (Shleifer, 2000).

Rational Expectations:

$$E_t \pi_{t+1} = E(\pi_{t+1} | I_t) \quad (2.1)$$

the expected price of Bitcoin, beginning month t , ${}_t\pi_{t+1}$ should incorporate all the available information, I , at beginning of month t and includes $\{\pi_t, \pi_{t-1}, \dots\}$ with corresponds to Bitcoin Price for period $t, t-1, \dots$. Also, $I_t \supseteq I_{t-1} \supseteq I_{t-2} \dots$. That is, agents participating in the market do not forget.

A possible Bitcoin Price Model, considering web sources, would be:

$$BC_{t+1} = \theta_0 + \alpha_1 BC_t + \alpha_2 Twitter_t + \alpha_3 Google_t + \alpha_4 Wiki_t + \varepsilon_t \quad (2.2)$$

Where BC is the Bitcoin price for period t , θ_0 is the constant, α is the coefficient, $Twitter$ represents the number of tweets referring “Bitcoin” for period t , $Google$ the number of searches using the term “Bitcoin” for period t , $Wiki$ the number of pageviews on the “Bitcoin” english wikipedia page and ε_t the error term.

As the Bitcoin price is not based on any fundamentals, it has implications for the applicability of the EMH on the Bitcoin market. Nevertheless, Bitcoin price has experienced a great deal of volatility (see Figure 2.1), and it is thus interesting to discuss its origin. Despite the thesis objective is not to study market efficiency of the bitcoin market, it forms an important basis to assess how information is incorporated into the price, for that reason essential for an analysis of the underlying causes of Bitcoin price volatility.

in order to identify undervalued (or overvalued) securities.

⁶In a perfectly smooth running market, you cannot find an opportunity that is risk free but still paying more than the risk-free interest rate (assume it as rate at which your bank pays for your savings deposits). This is called the no-arbitrage theory. Arbitrage means you can find an opportunity that is low-risk, high-reward. Financial research says that in theory that is impossible. If everyone know something is low-risk and high-reward everyone will jump on to it.

3: A Review of the Literature

3.1 *Cryptocurrencies*

With most weight on Bitcoin, there is a rise of academic research literature about cryptocurrencies. Most of them focus on the 'moneyness' literature of Bitcoin or if it is more comparable to a fiat versus commodity money like 'digital gold' (Harwick, 2014; Gertchev et al., 2013; Bergstra, 2014). Yermack (2013) note the weaknesses in Bitcoin as a currency and its moneyness and points out that cryptocurrencies have no intrinsic value.

By evaluating what adds to the value formation of cryptocurrencies Hayes (2015) said that the average amount of units which can be produced with a unit of hashing power is very important. A cryptocurrency may have a fixed rate set for unit formation over time, a ceiling, set into its code at its inception. The potential scarcity in terms of a fixed future 'money supply' did not play a role in the value development.

The peer-to-peer technology and cryptographic algorithms allow a decentralized organization and the information systems grant more operational security and are more transparent, thus against the centrally oriented and less transparent established monetary systems' structures (Glaser et al., 2014). The digital currencies propose then, a move from the traditional design of financial system infrastructures. The financial innovation, the internet and several other developments allowed alternative currencies that are exclusively electronic and built on peer-to-peer mechanism, supporting near real time transactions, transparent unit formation by open algorithm and store of transactions historical log. Moreover, Brezo and Bringas (2012) says that cryptocurrencies have the problem of being used for trafficking of illegal material and money laundering.

3.2 *Bitcoins*

As was defined by Nakamoto (2008), Bitcoin is an electronic financial mechanism that relies on a decentralized organizational structure providing features that are similar to a currency system, that has a specific money creation and transaction system. In contrast with the central bank's discretionary decision making, the money creation in the Bitcoin system is clear and transparently executed by a distributed and open algorithm, simplifying the expectations about the future amount of money. By storing all transaction history in a 'chain', the infrastructure grant near-real-time transaction monitoring using the public peer-to-peer network.

The Bitcoin's popularity intrigued several economists in general (e.g. Grinberg, 2011; Barber and Odean, 2008; Kroll et al., 2013; Moore and Christin, 2013), while Bitcoin's price formation intrigued in detail (e.g. Buchholz et al., 2012; Kristoufek, 2013; van Wijk, 2013). Previous literature showed that different factors may affect Bitcoin price: (i) market fundamentals like Bitcoin supply and demand (Buchholz et al., 2012); (ii) attractiveness for investors (Kristoufek, 2013); (iii) development of macroeconomic indicators (van Wijk, 2013). Buchholz et al. (2012) concluded that, as for of any currency, an important motive of Bitcoin price is the relation between Bitcoins' supply and demand. The supply of Bitcoin sets the amount of units in circulation and thus its scarcity on the market. The demand of Bitcoin is mainly set by transaction demand as a way of exchange. Kristoufek (2013) says that because supply-demand fundamentals don't exist on Bitcoin markets, which usually shape the ground of currency price formation, the price development of Bitcoin shouldn't be explained by classic economic theories. First, Bitcoin is not circulated by a specific government or central bank and thus is disconnected from the real economy. Second, the supply-demand for Bitcoin is compelled by investors' speculative behavior as well, because the lack of interest rate on digital currencies, thus profits can be earned only from price modifications. Additionally, van Wijk (2013) emphasizes this idea, in determining Bitcoin price, the role of macroeconomics development (stock exchange indices, exchange rates, gold and oil prices) measures. van Wijk (2013) concludes that the euro-dollar exchange rate, the Dow Jones index and oil price have a significant impact on the value of Bitcoin in the long run. In opposition

to this, Ciaian et al. (2014) do not support previous findings that the macroeconomics developments are driving Bitcoin price.

Bouoiyour et al. (2014) described Bitcoin value by regressing its market price against a number of independent variables like, the market price of gold, the occurrences of the word 'bitcoin' in Google searches, the number of transactions and so on. Generally, the variables when regressed, at the 5% level of significance, were not statistically significant. As for lags on the price of Bitcoin itself, they have some weight. Lagged Google search results were the only variable significant at the 1% level. This is an interesting finding, some variables that were expected to have value actually do not.

4: A Description of The Data

The data collected comes from many different sources. The data necessary to perform this research comes from Wikipedia¹, Twitter², Google³, Blockchain⁴ and Quandl⁵.

Time period: The time window to be analyzed in this study covers the range from 2011/26/06 through 2015/31/08 and includes a large fraction of early Bitcoin history and most importantly the growth phase of late 2012 and early 2014 to the more stable period of 2015.

4.1 Descriptive Statistics

Table A.1 shows some characteristics and properties that give us a better understanding of how to use the chosen variables in the model.

Figure A.6, which displays all our studied variables, offers a special view of the movement of the bitcoin price as well. The diagram for dBPI1, makes it clear that there is a great spread of return. We can see that in the end of 2013, December 7th and December 9th, an extreme example where bitcoin exhibits a -18.65% return and 20.5%, respectively. We can observe the volatility clustering effect that is typical for financial assets. Analyzing in more detail the return distribution for the dependent variable of our model, the dBPI1, we see a daily mean of 0.14\$, evidence of a relatively strong positive trend in the last 4 years and standard deviation of 16.9\$, consistent with a very volatile time-series. The kurtosis and skewness suggests that the distribution has a high leptokurtic characteristics and is negatively skewed. Indicating that the distribution is not normally distributed.

We consider 3 main grouping vectors for our data: Bitcoin attractiveness; Bitcoin Economics and Technicals; and Macroeconomics variables

¹<http://stats.grok.se/>

²<https://psychsignal.com/>

³<https://www.google.com/trends/explore#q=bitcoin>

⁴<https://blockchain.info/>

⁵<https://www.quandl.com/data/LBMA/GOLD-Gold-Price-London-Fixing>

4.2 Bitcoin Attractiveness

To measure attractiveness, information demand of Bitcoin, and its speculative value we use the search volume reported by search engines like Google and Wikipedia and a weighted score for a sample of tweets that refer Bitcoin. This value is provided by a scoring algorithm called Sentiment Analysis from PsychSignal⁶.

Without any fundamental value and a perceived sensitivity to investor sentiment (Kris-toufek, 2013); (Baker and Wurgler, 2006), it is likely that the information of certain events may lead to swings in the Bitcoin price.

As seen in Figure 2.1, the Bitcoin price exhibits extremely high volatility and with no specific pattern. It is then feasible to assume that particular events add volatility to the Bitcoin price. By browsing the information on the Internet⁷, and academic databases for information concerning Bitcoin, numerous events have been considered as important for the evolution of the Bitcoin market. Some of the chosen events are displayed in table 2.1.

Scanning the available information for reoccurring news, the ground of this selection is considered strong. However it is possible to perform an objective identification of other important events for the Bitcoin.

4.2.1 Search engines

The usage of Google searches using the word 'Bitcoin' and the page views on Wikipedia's Bitcoin page, were demonstrated by Mondria et al. (2010) and Moat et al. (2013), to be a useful source of information in financial applications. The frequency of searches of terms related to the digital currency can be a good measure of interest in the currency and it can provide a reliable proxy have a good explanatory power.

For this study, we want to evaluate the frequency of searches for the word 'bitcoin', this data is downloaded from Google Trend and Wikipedia and covers the whole period of interest, from June 26th 2011 to August 31st 2015.

Many scientific studies have been performed using search queries, suggesting an aca-

⁶<https://psychsignal.com/>

⁷<http://historyofbitcoin.org/>

demic acceptance of this specific method. Daily data was desired but due to the construction of Google Trend, it is only possible to extract daily data for the three most recent months, and earlier search queries are only displayed on a weekly basis, a specific adjustment factor was applied to transform it in daily data (ErikJJ, 2014). The data for Google searches uses a reference value of zero for the periods with very small amounts of search queries and 200 for the periods with very high amounts of search queries. As for Wikipedia, daily pageviews on the english Bitcoin page, are taken in consideration to evaluate the attractiveness of Bitcoin.

The investors' attractiveness based on Google searches (GOO): To proxy the investors' attractiveness to Bitcoin, we use daily Bitcoin searches from Google as it is capable of characterizing properly the speculative spirit of users, as it was stated by Kristoufek (2013). Additionally to that, it was chosen also by Bouoiyour et al. (2014), that used the number of times the key word Bitcoin is filed into the Google search engine. Google searches by day (normalized to 200) (see Figure A.1).

Total pageviews on Wikipedia (WIK): We adopt Wang (2012) that identified the group of specifically uninformed users, i.e., users who have only limited knowledge about Bitcoin, thus, search for initial information from an introductory source of information - Wikipedia. Like for GOO variable, we proxy the investors' attractiveness to Bitcoin by measuring the daily hits on the English Bitcoin Wikipedia. Figure A.2 provides an overview on that metric.

4.2.2 *Sentiment Analysis*

Recent articles from Bollen et al. (2011), Kaminski and Gloor (2014) and Rao and Srivastava (2012) defend the existence of a relationship between the volume of tweets and the market evolution. There is a good chance of success that tweets can forecast the market trend 3-4 days in advance (Bollen et al., 2011). Over the last years significant progress has been made on ways to derive indicators of public mood directly from social media content and in particular large-scale Twitter feeds and therefore create a sentiment tracking technique (Pak and Paroubek, 2010). We obtained a collection of public tweets that was recorded from June 26, 2011 to August 31st, 2015 and with that data we generated public mood time series using PsychSignal as a provider of real time

trader mood.

The tool acts by processing social media text, using a natural language engine that tries to assess the public's mood about Bitcoin. The technology analyzes millions of online tweets on a daily basis, the sentiment engine, for this thesis, is designed to measure the attitudes "bullishness" and "bearishness" over Bitcoin, is the sentiment positive or negative? Taking into account users input on Twitter, the studied and distinct theory is to mix millions of phrases in a way comparable to Google, that is, examining the internet web structure by ranking and aggregating the link structure, the PsychSignal method creates a structure of world feeling by aggregating and scoring emotions. Once identified and combined, the system regularly scores the attitude or emotion, setting a specific rate. This allows us to create a detailed picture of people mood regarding Bitcoin, providing clues on the "bull" and "bear" feeling.

Twitter number of messages (TWI_M): Total messages per day where the hashtag "#Bitcoin" is present.

Twitter Sentiment Analysis (TWI_I): To conclude the proxy on investors' attractiveness to Bitcoin, we apply, over the Twitter total number messages, the automatic Sentiment Analysis from PsychSignal (described above), on shared users tweets. Using the PsychSignal score, we automatically analyze people's opinions, feelings, evaluations and attitudes. Assessing the tweets in order to see if the sentiment is Bullish, Bearish or Null (see Figure A.3).

4.3 Bitcoin Economics and Technicals

We obtain transaction data via the web-based Bitcoin data provider Blockchain that aggregates trades on a daily basis. Here we collected the close prices of Bitcoin as well as other technical variables that are relevant for the Bitcoin network (see Figure A.4 to compare Bitcoin price with Bitcoin technical variables)

The Bitcoin price (BPI): The close price of Bitcoin, in US dollars, collected daily. This will be the dependent variable in our model.

The exchange-trade ratio (ETR): Ratio between volumes on the currency exchange market and trade. Kristoufek (2015a) says that can be considered as transactions proxy,

while Bouoiyour et al. (2014) address whether Bitcoin is business income or not.

The estimated output volume (EOV): The total value of all transaction outputs per day. Basically, Kristoufek (2015a), states that there is a negative relationship between the Bitcoin price and estimated output volume, i.e. an increase in output volume brings a drop in Bitcoin price notably in the long-run.

Bitcoins in Circulation (BC_Circ): Total number of bitcoins which have been mined up to August 31st, 2015 .

Average number of transactions per block (AVG_TR): As the difficulty of solving a block increases and the blocks get bigger so are the number of transactions occurring.

Miners Revenue(MINER): When a block is discovered, the finder (the miner) may award themselves a certain number of bitcoins, which is agreed-upon by everyone in the network, currently the award 25 bitcoins; this value will cut in half every 210,000 blocks, meaning each 4 years, because the network is designed to allow one block to be discovered each ten minutes.

Total number of unique Bitcoin transactions per day (TRAN): Is a transfer of Bitcoin value that is broadcast to the network and collected into blocks.

Number of unique Bitcoin addresses used per day (UA): Unique addresses in the network. Although addresses maybe generated all the time, it is still a relevant proxy for Bitcoin network size.

Difficulty (Diffic): Difficulty is a measure of how difficult it is to find a new block. This difficulty is adjusted by the network to guarantee that a block is discovered each ten minutes

Hash rate (HASH): It's a measure of the processing power of the Bitcoin network. For security goal and to solve blocks that get more and more complex, intensive mathematical operations are needed, leading to an increase in the hash rate that is connected to an increase in cost with hardware. Bouoiyour et al. (2014) says that the hash rate is correlated positively to Bitcoin price .

4.4 *Macroeconomics*

Gold Price (GP): its underlying value derives from production or consumption process. On the other hand, demand for Bitcoin is compelled by its value in a future transaction. The demand for commodity currency, like gold, is driven by its intrinsic value and its value in a future exchange. Moreover, the changes in production technology (e.g. mining technology for gold) and returns affect the supply of commodity currency, making it endogenous. While Bitcoin supply is exogenous as it is set by the software (ceiling) algorithm.

5: The Econometric Model

5.1 *Econometric methodology*

The asset returns are viewed as mean stationay by traditional models (standard and moving average deviation, among others) because it assumes that economic agents create their expectations the same way over time. It is of course well known that this allegation is far from reality, the variance-covariance of returns may be time-varying, during periods of great unrest (conflicting adjustments, crisis, political tensions, unforeseen shocks, etc.). The usage of statistical tests to evaluate stationarity, the application of significance tests about the parameters of the model, the correlation coefficients, the autocorrelations, the analysis of volatility sensitivity to shocks and the analysis of volatility persistence will drive us to the optimal model selection. Besides, we will more skillfully handle the great deal of volatility that has been experienced by the Bitcoin returns.

5.1.1 *First order difference*

By analysing Figure 2.1 we could immediately determine that Bitcoin price is not stationary, and to correct for stationarity first differences are applied, where Δy_t denotes the first-differenced series ¹:

$$\Delta y_t = y_t - y_{t-1} \tag{5.1}$$

Whenever we are exposed to a non-stationary time series, and to transform our time series in a stationary one, equation 5.1 will be used, e.g., Figure 5.1 exhibit Bitcoin price after applying first differences (see Equation 5.1).

¹The naming convention for order difference variables will be $d[\text{variable}][\text{number of order difference}]$

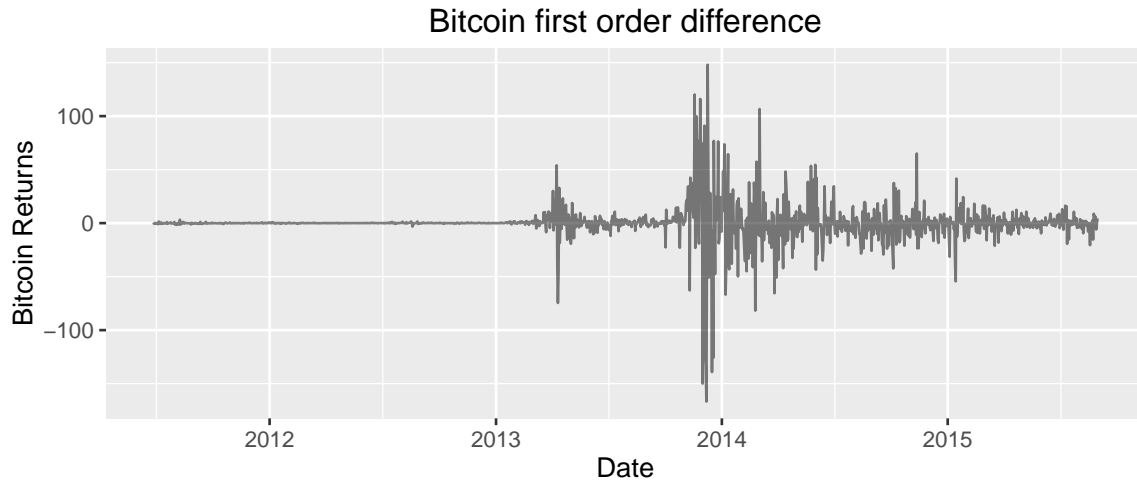


Figure 5.1: Bitcoin first order difference

The usage of unit root tests is a known method to find formal statistical evidence. Below we will see one of these tests in more detail.

5.1.2 Stationarity

The property of stationarity means that the first and second moment of time series, i.e., properties like the mean, variance and the autocorrelation function do not change over time. The stationarity is an important characteristic of the data, that for example, allows to reach conclusions about how a change in one time series variable impacts another one. Pindyck and Rubinfeld (1998) says that with stationarity it is feasible to model a process over an equation that has fixed coefficients and can be estimated with historical data. Because this thesis is concerned on how to model the Bitcoin price volatility using time series data, the existence of stationarity is of extreme importance. To test if a time series variable is $I(1)$ we use the unit root test, that consists on applying an autoregressive model.

$$y_t = \theta + \alpha y_{t-1} + \varepsilon_t \quad (5.2)$$

Where: y_t = current value of time series; θ = constant; α = real number (parameter); ε_t = independent random variable

We decided to use only one test in this study, the Augmented Dicker-Fuller (ADF) (Dickey and Fuller, 1979). The ADF test tests the null hypothesis that a time series

y_t is I(1), one difference is required to obtain a stationary series, against the alternative that it is I(0), the time series is stationary on trend-stationary. The error term is also assumed to be homoskedastic.

If the test p-value is smaller than the level of the test (e.g. 5%), the null hypothesis of a unit root is rejected, which suggests that the time series is stationary. If the time series are I(1), first differences referred in 5.1.1, should be applied in order to convert the time series into a stationary one.

The ADF results for stationarity are summarized in table A.3 (we assume the existence of an intercept and a time trend). The test show that the variables Hash, BC_Circ, Diffic and MINER appear to be I(1). There was the need to perform first differences (see equation 5.1) on the time series data from these variables and then we test to see if we achieved stationarity.

As for the dependent variable BPI, there are signs of I(1) as well. Equation 5.3 shows $\alpha = 0.997$, a figure very close to 1.

$$BPI_t = 0.716 + 0.997BPI_{t-1} + \varepsilon_t \quad (5.3)$$

Applying first differences, Equation 5.4, the dependent variable becomes stationary, with $\alpha = 0.149$.

$$dBPI_t = 0.119 + 0.149dBPI_{t-1} + \varepsilon_t \quad (5.4)$$

After applying the first order difference, the new variables list only displays values with a greater negative value, the correct conclusion is that after differencing Hash, BC_Circ, Diffic, MINER and BPI all variables are stationary time series. Figure A.6 shows a plot for all available time series.

5.1.3 Correlation Coefficient

To study the relationship between variables, the first differences variables are exposed to a correlation test. This test is important to detect collinearity, correlation between independent variables. Because we want to understand if our variables have an effect on Bitcoin price volatility, it is of major importance to study if there is collinearity between the variables included in our model.

The test outcome, shown in Figure A.5 and in table 5.1, suggests that there are several significant correlation between the available variables.

	1	2	3	4	5	6	7	8	9	10
Var1	TRAN	UA	UA	GP	GP	GP	UA	AVG_TR	TRAN	GP
Var2	AVG_TR	TRAN	AVG_TR	UA	TRAN	AVG_TR	ETR	ETR	ETR	ETR
Freq	0.9232607	0.9213660	0.8971774	-0.8659558	-0.8252932	-0.7799055	0.5381808	0.5298560	0.5073037	-0.4701057

Table 5.1: Person Correlation - Top 10

Examining the table generated and displayed above, we can see that TRAN and AVG_TR show the strongest relationship. This corresponds to the significant value of 0.9232. The second strongest relationship is between UA and TRAN, 0.9213. Thirdly, is UA and AVG_TR, with 0.8971.

This therefore suggests that the result of the correlation test is evidence of a weak relationship. Judging from these results, the risk for multicollinearity is considered high.

5.1.4 Returns

The usage of asset returns (Bitcoin price returns by applying 5.1) is well-known and is preferred within financial studies. Mainly because asset return have more appropriate statistical properties like normalization and most of the times they are independent and identically distributed (i.i.d.) something that asset prices are not. This offers another angle of the movement of the Bitcoin price, with returns it is possible to discern the clustering effect that is common for financial assets and observe the volatility, where volatility is set as the standard deviation of the return (Hull, 2012).

5.1.5 GARCH(1,1)

The GARCH model is usually recognized as the most adequate to study the conditional variance. It uses three weighted averages: the long run, the forecast that was made in previous period and the new information that was not available when the previous forecast was made. We test the ARCH appropriateness within an auxiliary regression as proposed by Asteriou and Hall (2007).

The GARCH model consists of two equations: a conditional mean equation

$$r_t = \alpha_0 + \alpha_1 r_{t-1} + \varepsilon_t \quad (5.5)$$

The conditional mean equation specifies the behavior of the returns, r_t , and its error term, ε_t , represents the unexpected return. This conditional mean equation generates an estimation of the error terms from information provided by previous period's return (Alexander, 2009).

The error term, ε_{t-1} , is then applied in the conditional variance equation. Together with the variance of previous period, σ_{t-1}^2 , it is then possible to estimate also the variance of the next period σ_t^2 . Where α_i , β_i and ω_0 are the parameters to estimate

$$\sigma_t^2 = \omega_0 + \sum_{i=1}^p \alpha_i \varepsilon_{t-i}^2 + \sum_{i=1}^q \beta_i \sigma_{t-i}^2 \quad (5.6)$$

α_i measures the magnitude to which variance reacts to shocks and therefore goes through into next period's volatility and ω_0 measures the weighted long run average variance.

Stationarity:

$$\alpha_i + \beta_j < 1 \quad (5.7)$$

and $\alpha_i + \beta_j$ measures the rate at which this effect disappears over time, closer to the unit, slower will be the conditional variance convergence to a marginal variance.

Since its inception, the GARCH model has been both extended and modified, but the simplest model, the $GARCH(1,1)$, is considered to be the most robust has claimed by Hansen and Lunde (2005).

5.2 The Econometric Model

The selected variables that come from applying stationarity tests, a time trend variable and correlation analysis generate the first econometric model. Conditional mean model:

$$\begin{aligned}
dBPI_t = & \mu_t + \alpha_1 dBPI_{t-1} + \alpha_2 GOO_t + \alpha_3 WIK_t + \alpha_4 TWI_t + \alpha_5 dHash1_t + \\
& \alpha_6 AVGTR_t + \alpha_7 dDiffic1_t + \alpha_8 dMINER1_t + \alpha_9 ETR_t + \alpha_{10} TRAN_t + \\
& \alpha_{11} UA_t + \alpha_{12} GP_t + \alpha_{13} dBCCirc1_t + \alpha_{14} EOVT_t + \varepsilon_t
\end{aligned} \tag{5.8}$$

And included in a $GARCH(1, 1)$ model that is then fitted to the Bitcoin volatility registered for the sample period and will thereby be able to state, how the variables affect the Bitcoin volatility.

5.3 Expected Results

Given that the Bitcoin market is mainly consist of non-professionals we expect strong connection with web media content, that we use as proxy to evaluate the users sentiment towards the currency. So Twitter, Google and Wikipedia should provide a positive influence on Bitcoin returns. Some technical variables like the total number of unique Bitcoin transactions per day (TRAN), Number of unique Bitcoin addresses used per day (UA) and the average number of transactions per block (AVG_TR), as seen in table 5.1 seem to have strong signs of correlation, and that occurs because of the technology behind Bitcoin market, where the more users come to the market more transactions will occur, moreover, as time passes it get harder to solve a block so more transactions are needed. The rational that we will be using is to remove from the model all the independent variables that have a high correlation.

It is our strong believe as well that the impact of web media content takes a distinct impact on the Bitcoin market, more specifically regarding the time it takes to the event occurring in GOO, WIK or TWI to influence Bitcoin returns.

Additionally, Gold Price (GP) is expected to have a positive sign, since usually this product is used has a save heaven that investor's turn to when there is an economic crisis, and as we have seen in Table 2.1, some of the most relevent events for the Bitcoin market are connected to periods of unrest.

6: The Empirical Results

6.1 GARCH(1,1)

The first output that we will analyze is the one coming from section 5.2, using the econometric model 5.8. After validating the variables for stationarity, we can now use them and study their ability to better understand the remarkable volatility of the Bitcoin price. As presented in section 5.1.5, we will use $GARCH(1, 1)$ model, as it is considered the most suitable option for this kind of market.

	Miu	ar1	GOO	WIK	TWIL	ETR	dHash1	TRAN	UA	GP	EOV	AVG_TR	dDiffic1	dMINER1	dBC_Circ1	omega	alpha1	beta1
Estimate	4.64	0.02	-0.06	-0.00	0.54	-0.03	-0.00	-0.00	-0.00	0.00	0.00	-0.00	0.00	0.00	-0.00	0.29	0.05	0.90
Std. Error	1.65	0.03	0.02	0.00	0.07	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.07	0.01	0.02
t value	2.82	0.48	-3.30	-0.64	7.73	-4.03	-1.24	-0.13	-1.28	0.52	0.32	-0.24	0.09	17.54	-6.58	4.39	9.60	50.49
Pr(> t)	0.00	0.63	0.00	0.52	0.00	0.00	0.21	0.89	0.20	0.60	0.75	0.81	0.93	0.00	0.00	0.00	0.00	0.00

Table 6.1: Results from GARCH(1,1) - Model 1

As expected some variables are not valid to our model (Table 6.1), TRAN, UA, EOV, AVG_TR and dDiffic1. Applying the high correlation rational referred in section 5.3 we will remove TRAN, UA and AVG_TR that correlate strongly with GP and ETR. Additionally, we pretend to find proof of predictability, to do that we need to understand if we can anticipate Bitcoin price. To achieve that we will lag social media data in one day.

$$\begin{aligned}
 dBPI_t = & \mu_t + \alpha_1 dBPI_{t-1} + \alpha_2 GOO_{t-1} + \alpha_3 WIK_{t-1} + \alpha_4 TWI_{t-1} + \alpha_5 dHash1_t + \\
 & \alpha_6 dDiffic1_t + \alpha_7 dMINER1_t + \alpha_8 ETR_t + \alpha_9 GP_t + \alpha_{10} dBCCirc1_t + \alpha_{11} EOV_t + \varepsilon_t
 \end{aligned} \tag{6.1}$$

	Miu	ar1	dGOO1	WIK_1	TWI_1_1	ETR	dHash1	GP	EOV	dDiffic1	dMINER1	dBC_Circ1	omega	alpha1	beta1
Estimate	-2.34	-0.01	0.00	0.00	0.09	-0.03	-0.00	0.00	0.00	0.00	0.00	-0.00	0.29	0.05	0.90
Std. Error	1.14	0.07	0.02	0.00	0.03	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.03	0.00	0.01
t value	-2.06	-0.09	0.16	0.07	3.18	-3.30	-1.24	4.13	0.25	0.04	17.00	-4.50	11.13	11.73	77.72
Pr(> t)	0.04	0.93	0.87	0.95	0.00	0.00	0.22	0.00	0.80	0.97	0.00	0.00	0.00	0.00	0.00

Table 6.2: Results from GARCH(1,1) - Model 2

The results in table 6.2 show that GOO and WIK when lagged in one day became non significant, with a p-value higher than 5%. We will change the GOO and WIK lags to 31 and 7 respectively (one month; one week). EOv, dHash1 and dDiffic1 will be removed from the model as well.

$$dBPI_t = \mu_t + \alpha_1 dBPI_{t-1} + \alpha_2 GOO_{t-31} + \alpha_3 WIK_{t-7} + \alpha_4 TWI_{t-1} + \alpha_5 dMINER1_t + \alpha_6 ETR_t + \alpha_7 GP_t + \alpha_8 dBCCirc1_t + \varepsilon_t \quad (6.2)$$

	Miu	ar1	GOO_31	WIK_7	TWI_1_1	ETR	GP	dMINER1	dBC_Circ1	omega	alpha1	beta1
Estimate	-0.04	0.06	-0.03	-0.00	0.01	-0.00	0.00	0.00	-0.00	0.00	0.15	0.85
Std. Error	0.27	0.04	0.01	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.01	0.01
t value	-0.13	1.65	-3.92	-0.03	1.03	-1.05	1.42	7.82	-3.96	3.12	15.81	89.05
Pr(> t)	0.89	0.10	0.00	0.97	0.30	0.30	0.16	0.00	0.00	0.00	0.00	0.00

Table 6.3: Results from GARCH(1,1) - Model 3

Table 6.3 gives evidences that WIK, ETR, GP and dMINER1 can be removed from this model. Keeping our focus in two variables (GOO and TWI) that act has an attractiveness proxy (see section 4.2) and one technical variable (BC_CIRC, see section 4.3).

$$dBPI_t = \mu_t + \alpha_1 dBPI_{t-1} + \alpha_2 GOO_{t-31} + \alpha_3 TWI_{t-1} + \alpha_4 dBCCirc1_t + \varepsilon_t \quad (6.3)$$

	Miu	ar1	GOO_31	TWI_1_1	dBC_Circ1	omega	alpha1	beta1
Estimate	0.12826200	0.15900404	-0.02546409	0.01361695	-0.00000738	0.00118106	0.15774186	0.84125814
Std. Error	0.02553776	0.03259479	0.00671383	0.00447652	0.00000280	0.00034953	0.01002751	0.00994862
t value	5.02244622	4.87820441	-3.79278442	3.04186323	-2.63429646	3.37895795	15.73091291	84.56029928
Pr(> t)	0.00000051	0.00000107	0.00014897	0.00235119	0.00843118	0.00072761	0.00000000	0.00000000

Table 6.4: Results from GARCH(1,1)

With a confidence level of 95%, it is thus highly unlikely that the result that we see in table 6.4 did happen merely by chance.

The time trend variable μ_t presents a positive coefficient of 0.12826200, showing a bullish behavior for the Bitcoin returns since its inception. The Google engine search variables exhibits a slightly negative value of -0.02546441 , suggesting a small effect on the Bitcoin return. When the google searches increases, there is a smoothing effect on the Bitcoin returns. More searches on Google for Bitcoin, higher is the knowledge of Bitcoin, then a decrease on volatility. The TWI_I has a similar coefficient, 0.01361695, suggesting a positive impact when the number and intensity increases so does the Bitcoin return. The number of Bitcoins in circulation report a small impact on the Bitcoin returns, -0.00000738 , as expected an increase in the quantity of Bitcoins suggests a negative impact on the digital currency returns. We conclude that the $GARCH(1,1)$ model will have the following conditional mean equation:

$$dBPI1_t = \mu_t + \alpha_1 dBPI1_{t-1} + \alpha_2 GOO_{t-31} + \alpha_3 TWI_{t-1} + \alpha_4 dBCCirc1_t + \varepsilon_t \quad (6.4)$$

Where $dBPI1_t$ represents Bitcoin returns for period t , $\mu_t = 0.12826200$, $\alpha_1 = 0.15900404$, $\alpha_2 = -0.02546441$, $\alpha_3 = 0.01361695$, $\alpha_4 = 0.00000738$

While the conditional variance equation is:

$$\sigma_t^2 = \omega_0 + \alpha_1 \varepsilon_{t-1}^2 + \beta_1 \sigma_{t-1}^2 \quad (6.5)$$

Where $\omega_0 = 0.00118106$, $\alpha_1 = 0.15774186$ and $\beta_1 = 0.84125814$

The calculation above, in table 6.1, 6.2, 6.3 and 6.4, were performed using the assumption of normal distribution.

6.2 Model Adequacy

The Ljung-Box test evaluates the presence of autocorrelation in the residuals of the $GARCH(1,1)$ model (see Equation 6.4), by displaying its ability to remove autocorrelation from the squared Bitcoin return.

6.2.1 Ljung-Box Test

Analysing Figure 6.1, were the correlograms of the squared residuals can be used to check autoregressive conditional heteroskedasticity (ARCH) in the residuals, no p-value is significant leading to not reject the null hypothesis.

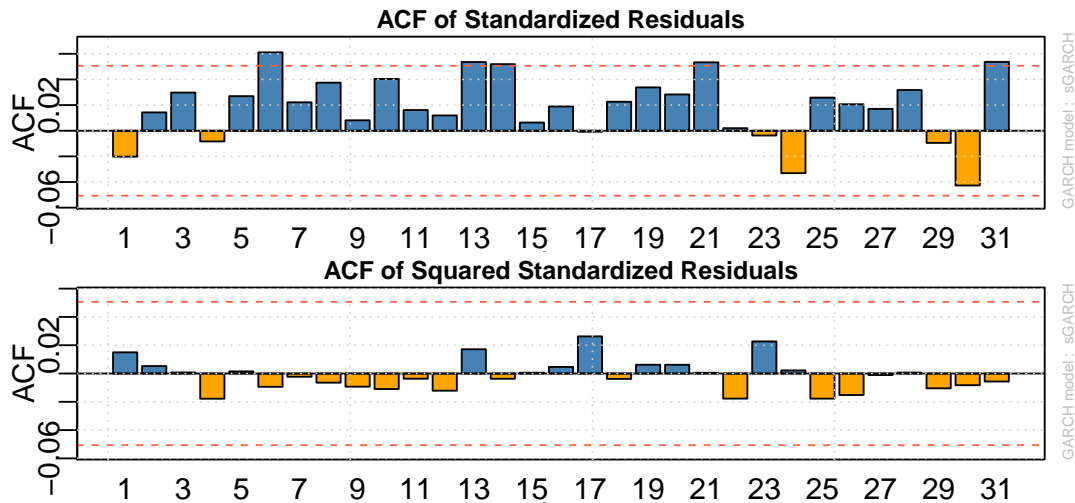


Figure 6.1: Time series $dBPI_t$ - ACF of Standardized Residuals

As for the returns, their unpredictability and the clustering of volatility can be concisely shown by looking at autocorrelations in the observations (Figure 6.2). As stated by Engle (1982), the predictability may show up as significant autocorrelations in returns, and volatility clustering will show up as significant autocorrelations in squared returns.

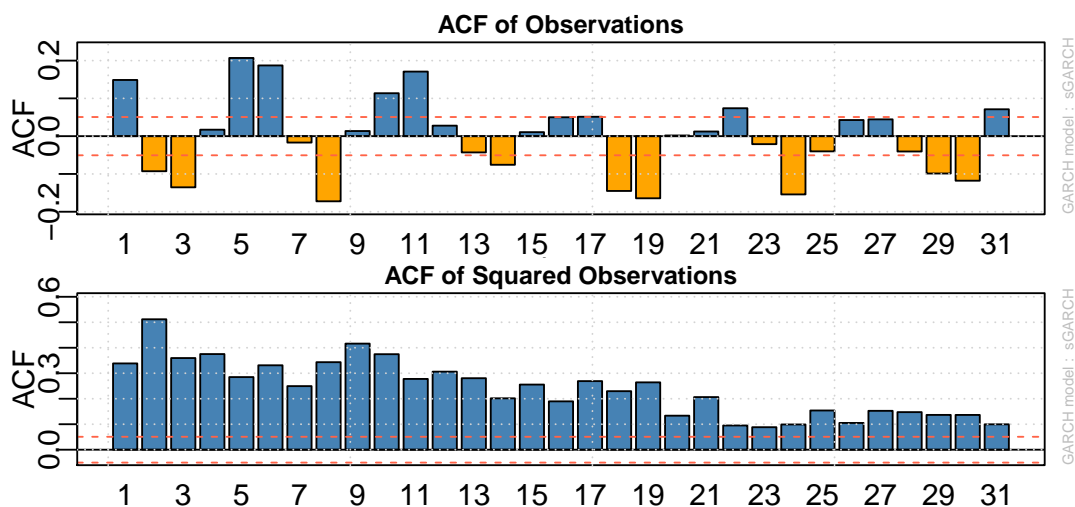


Figure 6.2: Time series $dBPI_t$ - ACF of Observations

The return autocorrelations are in some cases insignificant, while the square returns are all significant. This gives an evidence for some predictability of returns and volatility clustering. Furthermore, the squared return autocorrelations are all positive which is highly unlikely to occur by chance.

Using the $GARCH(1, 1)$ model referred in section 6.1 and supported by Figure 6.1, we can corroborate that this model is able to remove autocorrelation.

6.3 Analysis of Bitcoin prices - Predictability

As indicated by Fama (1965) and Malkiel (2003), prices should always reflect the fundamental value of the asset and that information should not affect an investor's capability to earn above-average returns. However, we know that Bitcoin has no fundamentals, and like it was argued in Chapter 2, supply and demand are the unique components that influence Bitcoin price.

With the existence of specific set of news that originates volatility and therefore indicating an increased dependence on information published about Bitcoin, we plan to understand how the web media data assist us on measuring the predictability of Bitcoin price.

The convergence between the conditional variance series and the unconditional variance line, Figure 6.3, its likely not to happen. The persistent parameters are too close to 1. Indicating that the conditional variance has a unit root, it is non-stationary, meaning that the mean and variance may change over time and may follow a trend.

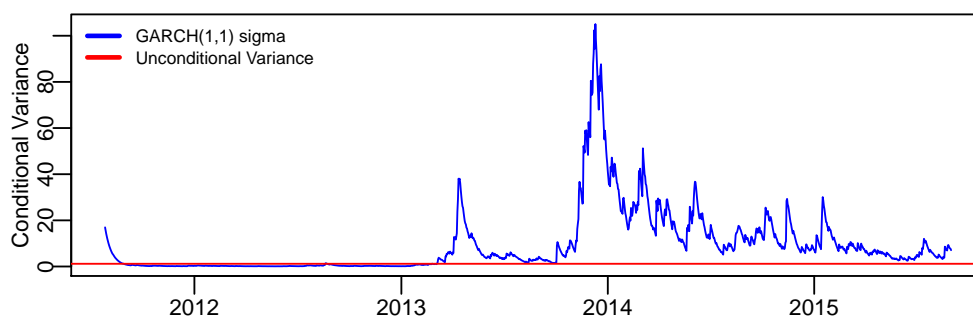


Figure 6.3: Model Adequacy: Conditional Variance

The rise in volatility started as stock prices got higher and higher, with it's peak around the end of 2013. Clearly, the Bitcoin market was risky from this perspective but investors were willing to take this risk because the returns were so good. Only at the end of the sample, do we see substantial declines in volatility. This same volatile period can also be spotted when we compare it the events referred in Table 2.1 and Figure 2.1, as it looks that spikes in Bitcoin price seem to correspond with major events. The first small peak coincides with the Cyprus Capital controls and the second one is related to the Chinese search engine, Baidu, and their decision to accept payments in Bitcoin and its antagonic decision, plus the fact that the Chinese government declared that banks were not allowed to deal with bitcoin motivated strong up and down movements on Bitcoin price.

It is our belief that Bitcoin investors are risk taking and this implies that is decisive for them to keep track with the information flow.

Our empirical results, see table 6.4, confirmed that web content has a strong impact on Bitcoin volatility. The relationship is slightly negative for Bitcoins in circulation, implying that as the number of coins in the market increase, the Bitcoin returns decrease, nevertheless the returns of Bitcoins in circulation moves quite close to Bitcoin returns. The Google engine search variables exhibits a slightly negative value, suggesting a small effect on the Bitcoin return. We may read this figure as, if Google searches increases, better is the knowleadge of Bitcoin, then a decrease on volatility. The TWI_I has a positive impact, suggesting a positive impact when the number and the positive comments intensity increases so does the Bitcoin return.

Moreover, the correlation between Bitcoin price and web content data give us some hints about the predictability power of these lagged variables, in reaction to positive and negative events. This can be considered as a logical reaction from investors to better understand the cause of the event and shorten the ambiguity produced by it.

The positive events seem to have lead Bitcoin price to a continuous increase and perhaps even to an overpricing as a result of the optimistic investor sentiment.

Such overpricing is referred by Kristoufek (2013) as congruent with the Bitcoin market because it resides essentially of non-professional noise traders, whose actions can cause bubble behavior of the Bitcoin price. This kind of trading means a higher probability

of market inefficiencies (Stambaugh et al., 2012), that then boost the not optimal decisions, therefore increasing volatility when compared with more established markets.

These unsophisticated noise traders are easily influenced by the behavior and expectations of others (Kristoufek, 2013). Consequently, the Bitcoin market is more likely to experience enthusiasm and mimetic contagion¹ (Topol, 1991). The bubble-behavior of the Bitcoin price could be a consequence of Bitcoin investors who overestimate the value of information and follow the behavior of others, originating a trading burst among investors. The presence of noise, high volatility and predictability acts as a disturbance to the theories of efficient markets and random walk.

As the Bitcoin price has experienced such extreme volatility, and we have seen that 31 days lagged Google search data and 1 day lagged Twitter data was statistically significant and with relative strong coefficients (see table 6.4), giving us the possibility to anticipate Bitcoin price. We can assume that Bitcoin price has evidence of predictability.

¹Topol (1991) shows that mimetic contagion provides a mechanism for excess volatility. Imitative behavior under the name “mimetic rationality,” by developing models of mimetic contagion of investors in the stock markets which are based on irreversible processes of opinion forming.

7: Conclusion

7.1 *What drives Bitcoin value?*

The Bitcoin currency, due to its extraordinary price growth, attracted the public attention. Investors increased their interest because of possible profits of hundreds percent in just a few weeks. The market value kept building up supported by its high volatility that invited risk taking investors. The strong network effects that cause a high positive trend, and the increased social media awareness, all this together, empowered the Bitcoin price, and, therefore, led the Bitcoin price.

By combining the information in the preceding chapters, we are able to discuss the circumstances that may affect bitcoins price volatility. Supported by both literature and our own empirical results we found that both web content data and previous Bitcoin price variables have a significant impact on Bitcoin volatility. In addition, we found that the economics sensitivity, section 4.3, of the Bitcoin market is perhaps lower than initially assumed after the extensive data check, whereas Miner revenue seems quite connected to Bitcoin returns, showing revenue alternatives to Bitcoin investors. However, our goal was to focus more on content provided by web content, through the proxies Google, Wikipedia and Twitter, and we found an explanatory power for the extreme Bitcoin price volatility on two of these variables.

We investigated how much the discussion on twitter precedes fluctuations on the stock market. To put it in other words, the question is how long it takes the stock market to react to the buzz on Twitter. How much investors anticipate their search in Google before investing, and how many days in advance do they express their sentiment about the Bitcoin phenomena on Twitter before going to the market. Our empirical analysis showed us that lagging 31 and 1 days, Google and Twitter, respectively, would be the wisest choice.

7.2 Why is Bitcoin volatile?

Our empirical research showed a close positive connection between web media content and Bitcoin price volatility. As we referred in the previous chapter, if investors are doubtful about their investment, they seek to decrease this ambiguity by increasing their knowledge/awareness. To measure that, we used proxies Google, Wikipedia and Twitter. As a consequence of this lack and pursue for knowledge, Bitcoin price volatility increases. Spikes on the online social media variables can be connected to the occurrence several significant events on the Bitcoin universe, see main news on Bitcoin in table 2.1 and Figure 2.1. The characteristics of the so called risk taking investor and the non-professional noise traders ensures a strong probability of such behavior and prejudice their decision making process. Popularity and rapid growth plus the realization that a Bitcoin investment could be lost instantly because of hacks and technological difficulties are considered as very important for the Bitcoin volatility.

As it was explained in section 6.3, our results imply high presence of noise traders. Increased trade volume and non-optimal decisions, can foment high volatility on Bitcoin price. Nevertheless, we believe that, like stated by Garcia et al. (2014), the positive trend of acceptance of Bitcoin should reduce its price volatility. During 2015 the Bitcoin market exhibited a more balanced price, suggesting that as the market gets more mature, it becomes less uncertain for the investor. So, the risk of fads, mimetic contagion and bubbles should decrease over time.

7.3 What is the ability of the GARCH(1,1) model on the Bitcoin price?

The significance and explanatory value of social media data and previous Bitcoin price were further examined through financial modeling using GARCH(1,1). The empirical study was inspired by the research by Stråle Johansson and Tjernström (2014) and Kristoufek (2013). Our model, based on equation 6.5, where $\omega_0 = 0.001187$, $\alpha_1 = 0.158687$ and $\beta_1 = 0.840313$, showed clearly that the bulk of the information comes from the previous day forecast β_1 .

This means a large σ_{t-1}^2 tends to be followed by another large σ_t^2 , generating, the well-known behavior, of volatility clustering in financial time series, the volatility is persistent or it “has” memory. Regarding α_1 coefficient, as it is relatively big, it means that the volatility reacts intensively to the stock market shocks, meaning, the reaction coefficient or heterogeneity is considerable.

The long run average variance ω_0 has a very small effect. Causing the unconditional or long run variance effect to be 1.228. Additionally, with a persistence, $\lambda = \alpha_1 + \beta_1$, close to 1, particularly 0.99, volatility remains long.

We assume that the conditional variance has a very slow convergence with the unconditional variance so that the process can be stationary with a finite variance. We could assume that this conditional variance model becomes non-stationary, see equation 5.7, originating an *IGARCH*(1, 1) model.

7.4 Is Bitcoin predictable?

News may be unpredictable but very early indicators can be extracted from online social media (blogs, Twitter feeds, etc.) to predict changes in various economic and commercial indicators. This may conceivably also be the case for the Bitcoin price.

However, the general notion of efficient markets “emphasizes a lack of return predictability as the criterion for efficiency” (Chordia et al., 2008). Therefore, efficiency can be measured by the relative availability or predictable outsized returns. A perfectly efficient market would not have any return predictability, and therefore investors could not expect to beat the market.

The analysis over Figure 6.2, where the autocorrelations of the observed returns give us some idea of predictability, makes us relatively sure that Bitcoin price can be anticipated. Additionally, the statistical significance of the lagged social media variables, shows how we can precede the Bitcoin price.

7.5 Recommendations For Future Research

There are several possibilities to extend the work presented in this thesis. Firstly, there is a small time frame in which the analysis is done due to the fact that the Bitcoin is

still quite new, which might render many conclusions made in this paper unsatisfying. Secondly, the independent variables used in this case may not effectively reflect the expectations and interests of agents in the currency. Other sources of web data could be used, like RSS feeds, Facebook posts, LinkedIn posts, Baidu trends, Wikipedia Bitcoin page in Chinese and YouTube video views. Using different kinds of variables, like different macroeconomic variables or data of other cryptocurrencies could also help us gaining a clearer interpretation on the Bitcoin phenomenon. Thirdly, we came across the idea that Bitcoin interest/attractiveness is affected by events. A more detailed study into this relation could prove informative, likely, the addition of binary variables to represent some of these events (i.e. events from table 2.1) or a more thorough approach on the existent network effects on the Bitcoin phenomena could have improve the explanatory power of our model.

Additionally, a better estimator than $GARCH(1, 1)$ could be used in the final analysis. For example, IGARCH, a restricted version of the GARCH model, is a highly suggested technique for analyzing data with serial correlation and where the persistent parameters sum up to one, and therefore the conditional variance becomes non-stationary in the GARCH process, or in our case, the convergence to a marginal/unconditional variance takes longer to achieve.

Therefore, if the Bitcoin market keeps maturing, evaluating these same variables or adding some of the proposed variables above, could be relevant. Also, comparing the differences and similarities between an emerging market and a mature market could be insightful.

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Appendix A: Appendix

	min	max	mean	median	sd	IQR	skewness	kurtosis
TWI_M	0.00	622.00	40.30	2.00	104.89	6.00	2.81	6.66
TWI_I	-40.78	198.78	1.28	0.00	7.35	0.00	14.40	353.99
WIK	0.00	847614.00	11428.61	5659.50	31846.22	5876.25	19.09	456.55
GOO	0.00	195.24	16.01	12.00	20.86	15.00	3.27	14.41
Hash	6639.29	458451590.73	89408281.04	278128.76	136990773.48	168187156.88	1.17	-0.33
ETR	0.36	92.23	10.86	7.33	10.74	10.72	2.31	8.07
EOV	39104.00	5825066.00	205615.52	160756.00	342376.82	114307.25	10.47	130.36
BC_Circ	6670150.00	14559975.00	11212309.96	11475200.00	2238850.82	3705831.25	-0.37	-1.01
AVG_TR	30.00	1483.00	343.70	319.00	239.94	279.25	0.84	0.73
Diffic	1090715.68	54256630327.89	12041406469.29	31256960.73	18669861494.61	19727779549.27	1.18	-0.36
MINER	12475.10	5117346.00	883647.50	526737.94	1021772.39	1224552.77	1.41	1.51
TRAN	4523.00	214487.00	52998.65	53448.00	34724.71	45113.00	0.54	0.40
UA	7701.00	295662.00	95683.92	63530.00	78340.21	134375.25	0.56	-1.07
GP	1080.05	1896.50	1435.65	1350.25	215.25	405.50	0.23	-1.45
BPI	2.29	1151.00	213.54	121.56	240.94	339.17	1.13	0.47
dHash1	-128964747.44	116587501.03	280831.79	323.43	18915564.88	70211.31	-0.21	9.86
dBC_Circ1	2600.00	9450.00	5166.88	4375.00	1708.03	3000.00	0.70	-0.95
dDiffic1	-2698788161.39	4831692799.94	35530616.33	0.00	324359440.52	0.00	8.20	97.99
dMINER1	-1226404.20	998061.07	515.83	184.56	169431.22	46995.96	-0.50	11.73
dBPI1	-166.71	148.01	0.14	0.00	16.99	2.36	-0.76	30.20

Table A.1: Variables Summary

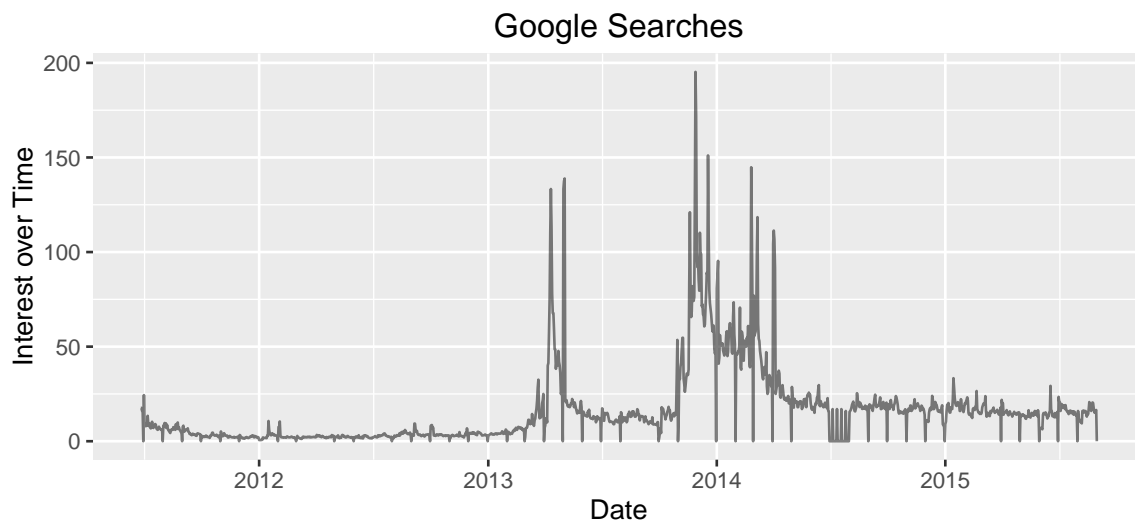


Figure A.1: Google Searches

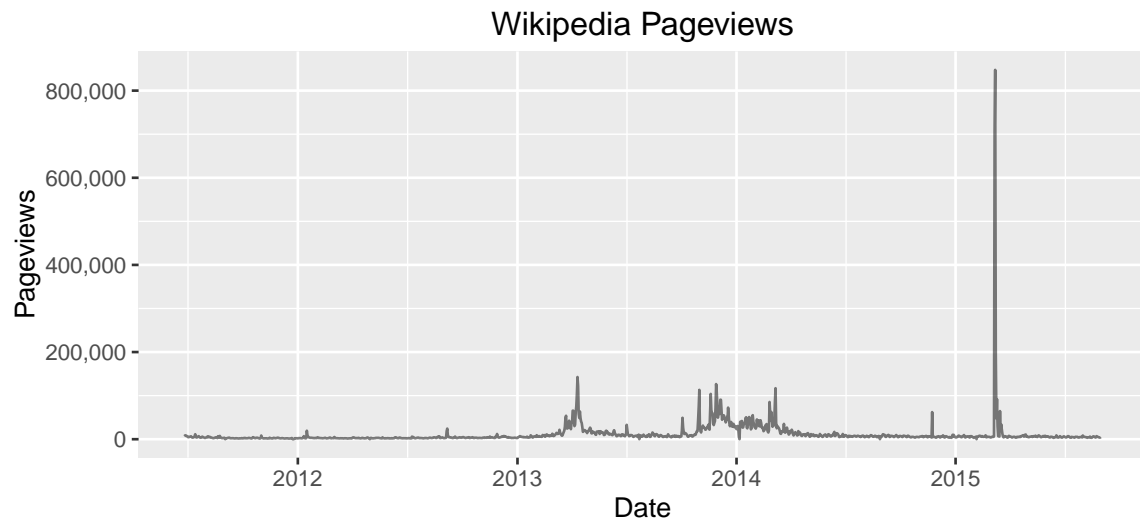


Figure A.2: Wikipedia Pageviews

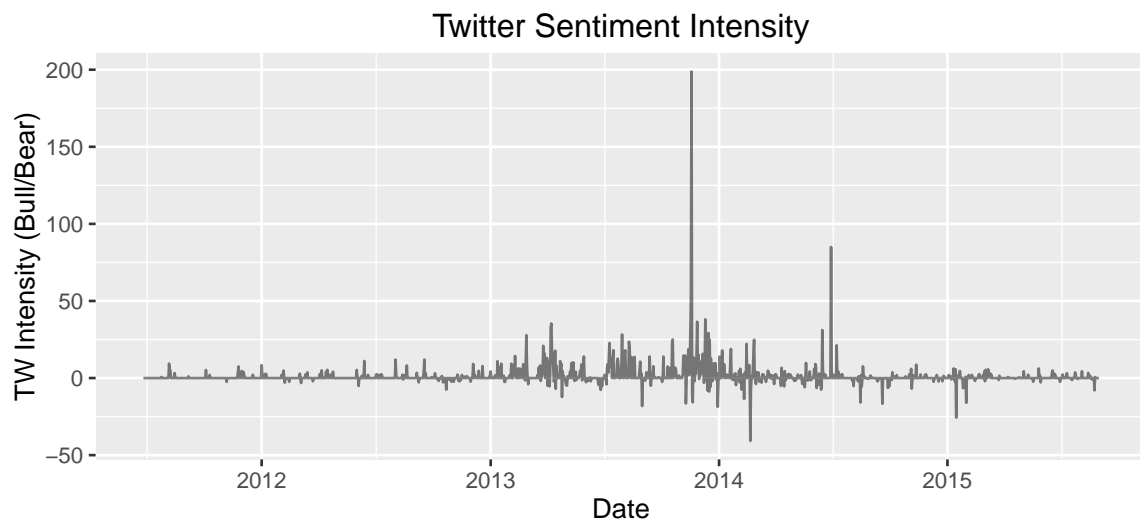


Figure A.3: Twitter Sentiment Intensity

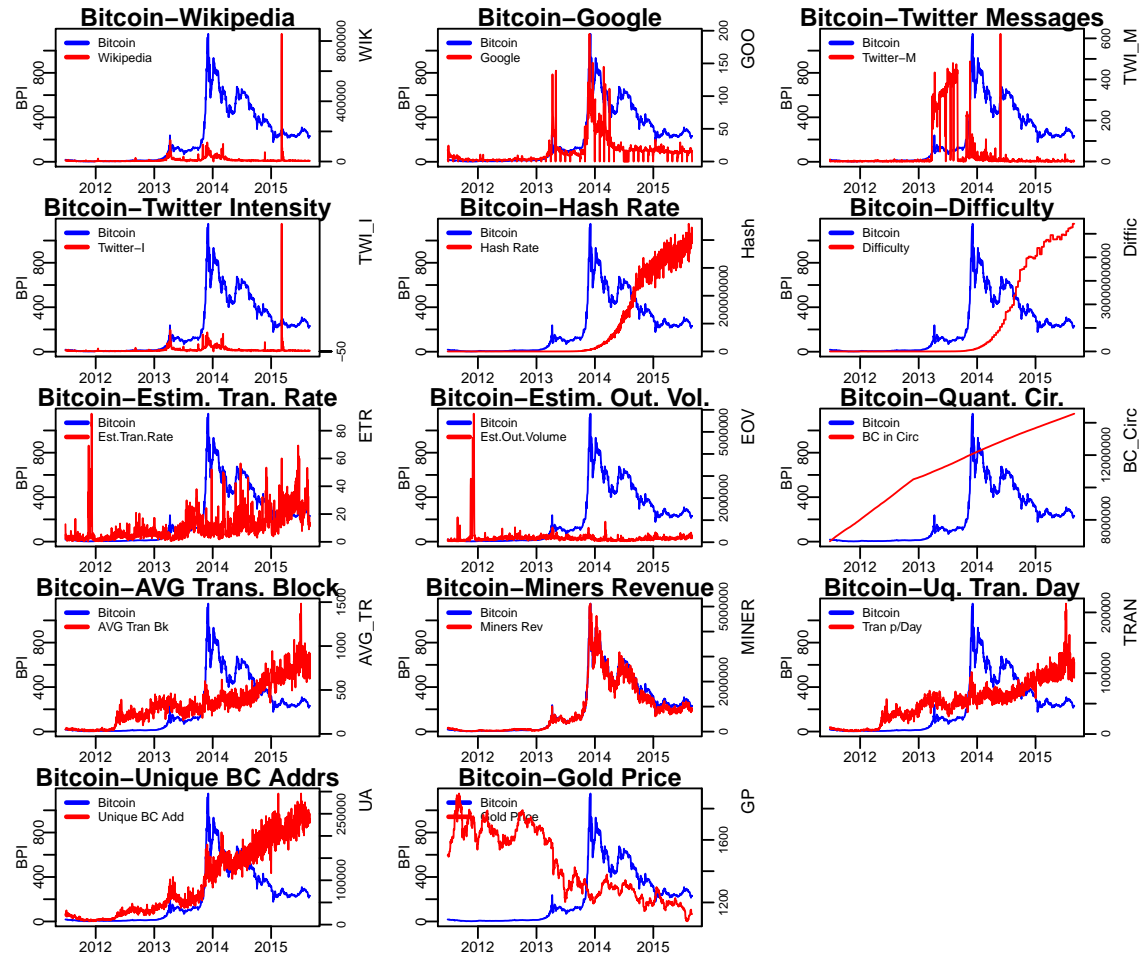


Figure A.4: Bitcoin Price and independent variables

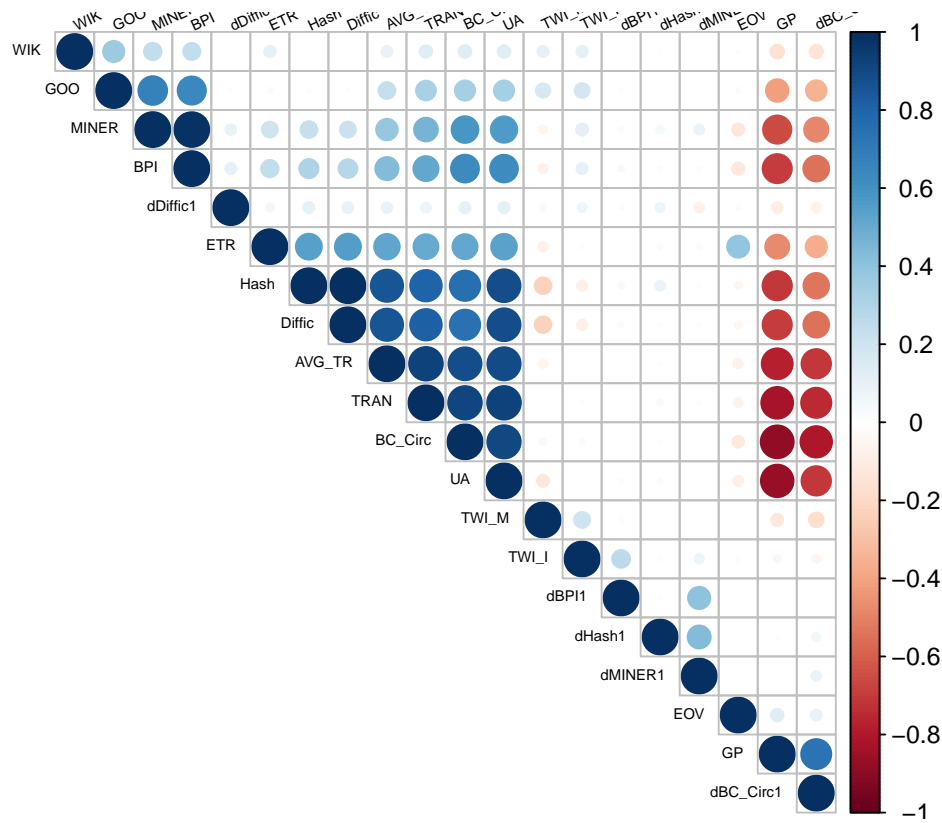


Figure A.5: Correlation Plot

	TWL_M	TWL_I	WIK	GOO	ETR	EOV	AVG_TR	TRAN	UA	GP	dHash1	dBC_Circ1	dDiffic1	dMINER1	dBPI1
TWL_M	1.00	0.21	0.10	0.17	-0.08	0.00	-0.06	-0.00	-0.12	-0.12	-0.01	-0.18	-0.03	-0.01	0.02
TWL_I	0.21	1.00	0.11	0.18	-0.01	0.02	-0.01	0.02	-0.01	-0.04	0.02	-0.06	0.07	0.07	0.26
WIK	0.10	0.11	1.00	0.37	0.11	0.01	0.10	0.13	0.13	-0.15	-0.01	-0.15	0.00	-0.00	-0.00
GOO	0.17	0.18	0.37	1.00	0.02	-0.02	0.23	0.32	0.34	-0.41	0.00	-0.35	0.01	0.00	-0.01
Hash	-0.23	-0.09	0.00	0.02	0.55	-0.05	0.85	0.81	0.88	-0.70	0.08	-0.53	0.10	0.02	-0.03
ETR	-0.08	-0.01	0.11	0.02	1.00	0.40	0.53	0.51	0.54	-0.47	0.02	-0.37	0.05	0.03	-0.00
EOV	0.00	0.02	0.01	-0.02	0.40	1.00	-0.07	-0.07	-0.09	0.13	0.01	0.10	-0.02	0.00	-0.01
BC_Circ	0.04	0.02	0.13	0.34	0.51	-0.11	0.88	0.92	0.90	-0.88	0.01	-0.81	0.10	-0.00	-0.01
AVG_TR	-0.06	-0.01	0.10	0.23	0.53	-0.07	1.00	0.92	0.90	-0.78	0.01	-0.71	0.09	-0.00	-0.00
Diffic	-0.23	-0.09	0.00	0.01	0.55	-0.04	0.85	0.81	0.88	-0.70	0.01	-0.54	0.10	-0.01	-0.03
MINER	-0.06	0.12	0.25	0.67	0.21	-0.12	0.38	0.46	0.57	-0.65	0.05	-0.48	0.10	0.08	0.02
TRAN	-0.00	0.02	0.13	0.32	0.51	-0.07	0.92	1.00	0.92	-0.83	0.03	-0.74	0.08	0.01	-0.00
UA	-0.12	-0.01	0.13	0.34	0.54	-0.09	0.90	0.92	1.00	-0.87	0.02	-0.71	0.10	0.00	-0.02
GP	-0.12	-0.04	-0.15	-0.41	-0.47	0.13	-0.78	-0.83	-0.87	1.00	-0.01	0.74	-0.10	-0.00	0.00
BPI	-0.07	0.10	0.24	0.65	0.25	-0.12	0.44	0.51	0.63	-0.69	0.01	-0.54	0.10	0.02	0.03
dHash1	-0.01	0.02	-0.01	0.00	0.02	0.01	0.01	0.03	0.02	-0.01	1.00	0.06	0.07	0.43	-0.02
dBC_Circ1	-0.18	-0.06	-0.15	-0.35	-0.37	0.10	-0.71	-0.74	-0.71	0.74	0.06	1.00	-0.08	0.08	-0.01
dDiffic1	-0.03	0.07	0.00	0.01	0.05	-0.02	0.09	0.08	0.10	-0.10	0.07	-0.08	1.00	-0.08	0.02
dMINER1	-0.01	0.07	-0.00	0.00	0.03	0.00	-0.00	0.01	0.00	-0.00	0.43	0.08	-0.08	1.00	0.41
dBPI1	0.02	0.26	-0.00	-0.01	-0.00	-0.01	-0.00	-0.00	-0.02	0.00	-0.02	-0.01	0.02	0.41	1.00

Table A.2: Correlation Table

	Dickey-Fuller	P-value	Type
TWI_M	-3.62352080568998	0.0304	with INTERCEPT and time TREND
TWI_I	-8.68572642322224	0.01	with INTERCEPT and time TREND
WIK	-8.62566611478799	0.01	with INTERCEPT and time TREND
GOO	-4.03024838353326	0.01	with INTERCEPT and time TREND
Hash	-0.3551119536656	0.9884	with INTERCEPT and time TREND
ETR	-7.02560876425668	0.01	with INTERCEPT and time TREND
EOV	-8.48101651154304	0.01	with INTERCEPT and time TREND
BC_Circ	-1.7797587088403	0.6715	with INTERCEPT and time TREND
AVG_TR	-4.91983523489371	0.01	with INTERCEPT and time TREND
Diffic	-0.305501224194358	0.99	with INTERCEPT and time TREND
MINER	-1.83813989771912	0.6468	with INTERCEPT and time TREND
TRAN	-5.63597336458813	0.01	with INTERCEPT and time TREND
UA	-3.60070019278943	0.0326	with INTERCEPT and time TREND
GP	-3.90930821876541	0.0135	with INTERCEPT and time TREND
BPI	-2.06227232721773	0.552	with INTERCEPT and time TREND
dHash1	-19.7417440323431	0.01	with INTERCEPT and time TREND
dBC_Circ1	-3.43599167785402	0.0485	with INTERCEPT and time TREND
dAVG_TR1	-17.0602939836471	0.01	with INTERCEPT and time TREND
dDiffic1	-14.1799495275105	0.01	with INTERCEPT and time TREND
dMINER1	-14.2322799328158	0.01	with INTERCEPT and time TREND
dTRAN1	-15.9706183323182	0.01	with INTERCEPT and time TREND
dUA1	-15.4790550493702	0.01	with INTERCEPT and time TREND
dGP1	-11.7836445682084	0.01	with INTERCEPT and time TREND
dBPI1	-10.3441464390466	0.01	with INTERCEPT and time TREND

Table A.3: ADF: Stationarity

	Description
TWI_M	Total messages per day where the hashtag #Bitcoin is present.
TWI_I	Score over the Twitter total number messages. Assessing people mood regarding Bitcoin. Based on their tweets.
WIK	Total pageviews on Wikipedias english Bitcoin page, per day.
GOO	Daily searches on Google search engine using the term Bitcoin.
Hash	It is a measure of the processing power of the Bitcoin network
ETR	Ratio between volumes on the currency exchange market and trade.
EOV	The total value of all transaction outputs per day.
BC_Circ	Total number of bitcoins which have been mined up to August 31/2015.
AVG_TR	Average number of transactions per block. As the difficulty of solving a block increases so are the transactions.
Diffic	Difficulty is a measure of how difficult it is to find a new block. This difficulty is adjusted by the network.
MINER	Miners Revenue. When a block is discovered, the finder receives a certain number of bitcoins.
TRAN	Total number of unique Bitcoin transactions per day
UA	Number of unique Bitcoin addresses used per day.
GP	Gold Price
BPI	The close price of Bitcoin, in US dollars, collected daily.
dHash1	First order difference for the Hash variable
dBC_Circ1	First order difference for the BC_Circ variable
dAVG_TR1	First order difference for the AVG_TR variable
dDiffic1	First order difference for the Diffic variable
dMINER1	First order difference for the MINER variable
dTRAN1	First order difference for the TRAN variable
dUA1	First order difference for the UA variable
dGP1	First order difference for the GP variable
dBPI1	First order difference for the BPI variable

Table A.4: Variables Description

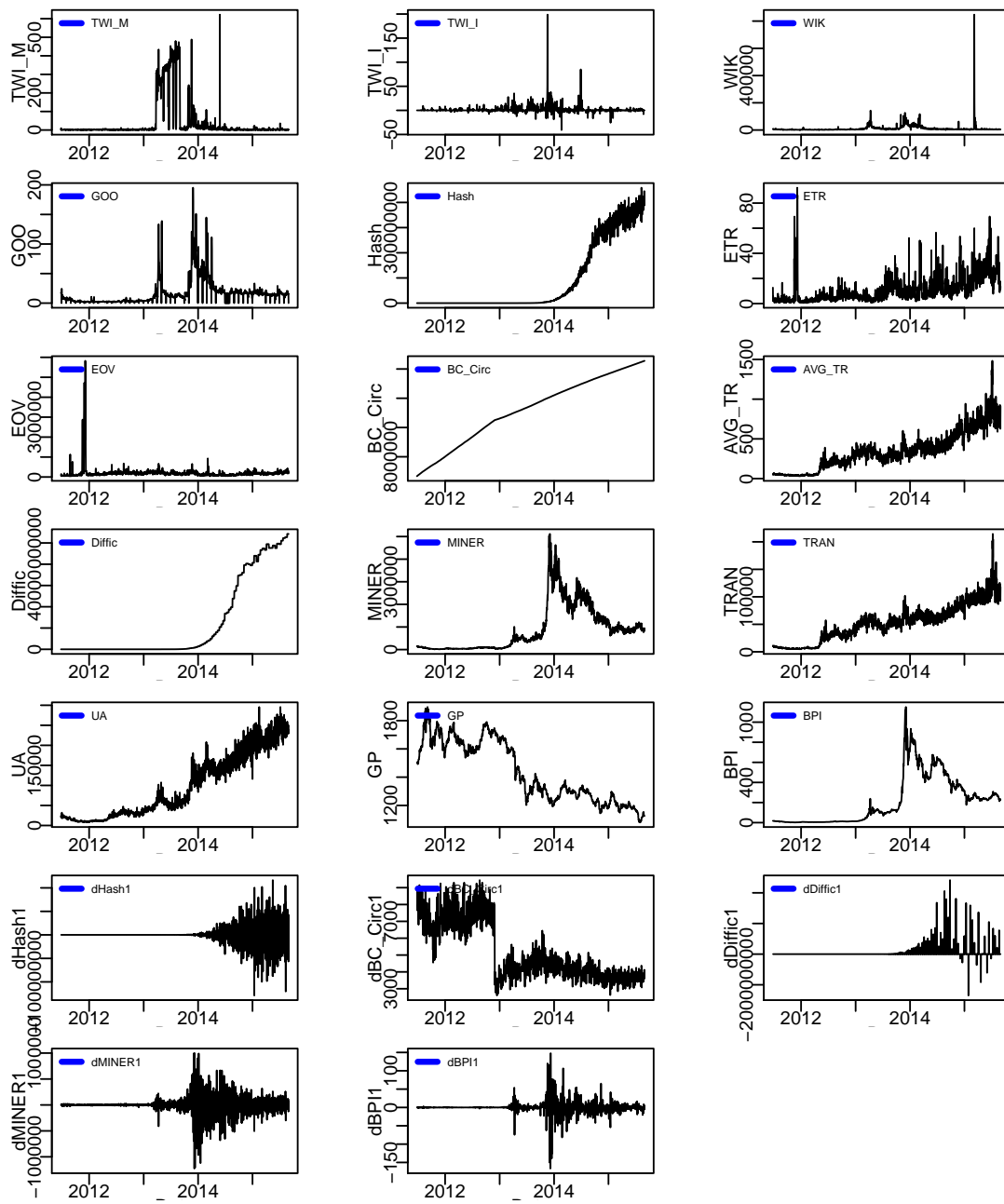


Figure A.6: All studied variables plots